

# Gauge couplings in $SO(5) \times U(1)$ Gauge-Higgs unification

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# Standard Model

W boson          up          charm

Z boson          down          bottom          top

光子          strange

グルーオン          電子          タウレプトン

ニュートリノ x3          ミューオン

ヒッグス粒子 (まだ見つかっていない)

# SO(5)xU(1) ゲージ・ヒッグス

W boson          up          charm

Z boson          down          bottom          top

光子          strange

グルーオン<sub>xSU(3)<sub>c</sub></sub>          電子          タウレプトン

ニュートリノ x3          ミューオン

ヒッグス粒子

+非常に重い粒子

## Custodial symmetry

Standard Model Higgs  $H$   $SU(2)_L$  doublet

$\epsilon H^*$  transforms in the same way as  $H$

$$\left( \begin{array}{c} \epsilon H^* \\ H \end{array} \right)$$

## Custodial symmetry

Standard Model Higgs  $H$   $SU(2)_L$  doublet

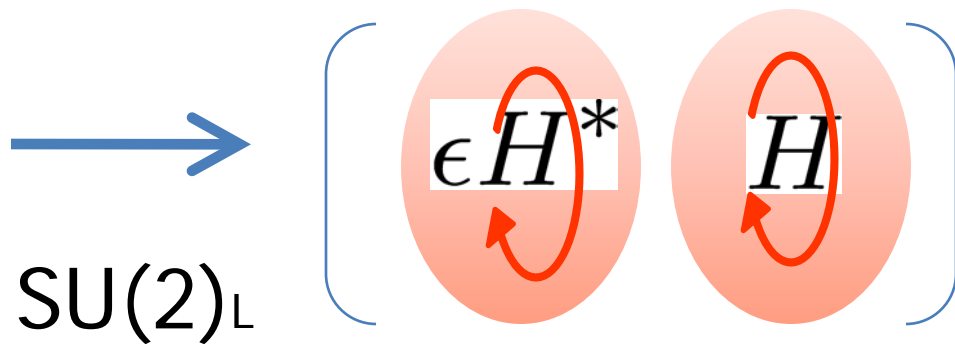
$\epsilon H^*$  transforms in the same way as  $H$

$$\begin{array}{c} \longrightarrow \\ SU(2)_L \end{array} \left( \begin{array}{cc} \epsilon H^* & H \end{array} \right)$$

# Custodial symmetry

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$\epsilon H^*$  transforms in the same way as  $H$



## Custodial symmetry

Standard Model Higgs  $H$   $SU(2)_L$  doublet

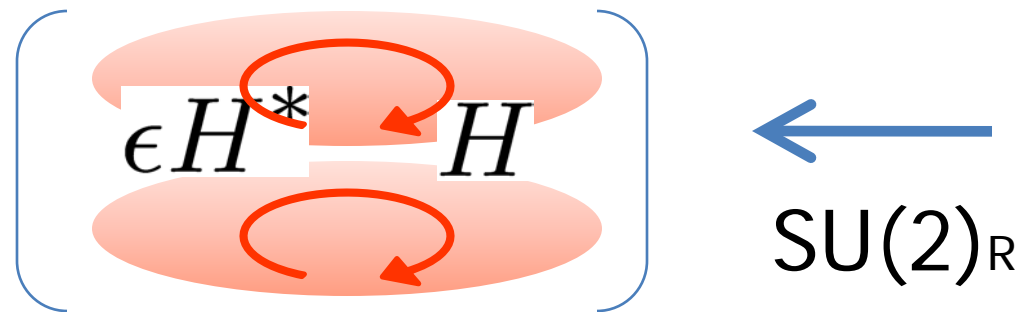
$\epsilon H^*$  transforms in the same way as  $H$

$$\left( \begin{array}{c} \epsilon H^* \\ H \end{array} \right) \leftarrow \text{SU}(2)_R$$

# Custodial symmetry

Standard Model Higgs  $H$   $SU(2)_L$  doublet

$\epsilon H^*$  transforms in the same way as  $H$





## Custodial symmetry

Standard Model Higgs  $H$   $SU(2)_L$  doublet

$\epsilon H^*$  transforms in the same way as  $H$

$$\left( \begin{array}{cc} \epsilon H^* & H \end{array} \right)$$

$$SU(2)_L \times SU(2)_R$$

## Custodial symmetry

Standard Model Higgs  $H$   $SU(2)_L$  doublet

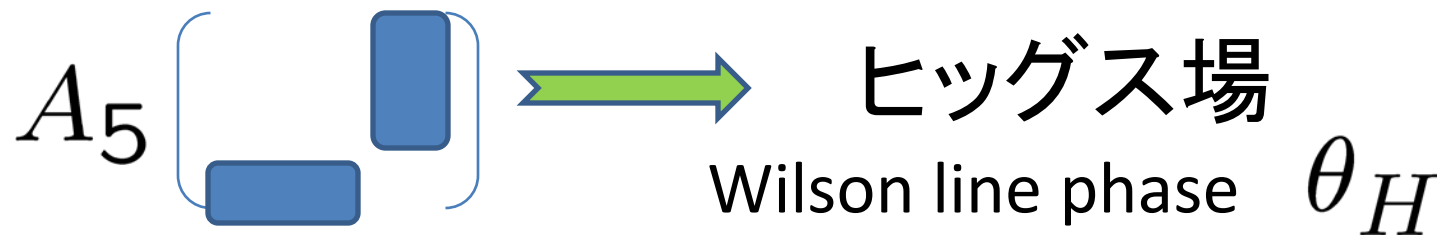
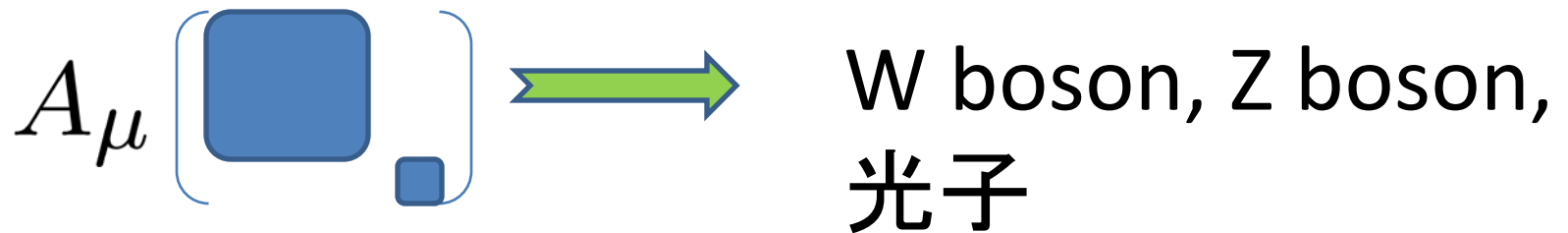
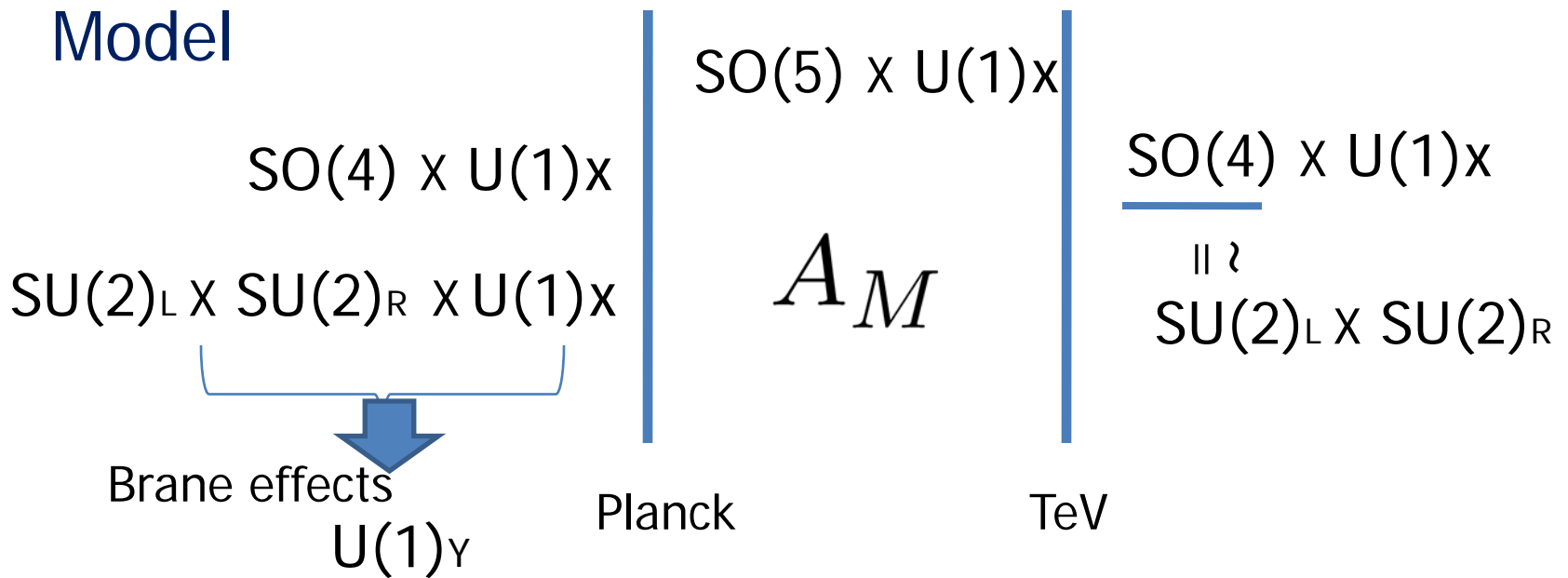
$\epsilon H^*$  transforms in the same way as  $H$

$$\left( \begin{array}{c} \mathbf{v}^* \\ H \\ \mathbf{v} \end{array} \right)$$

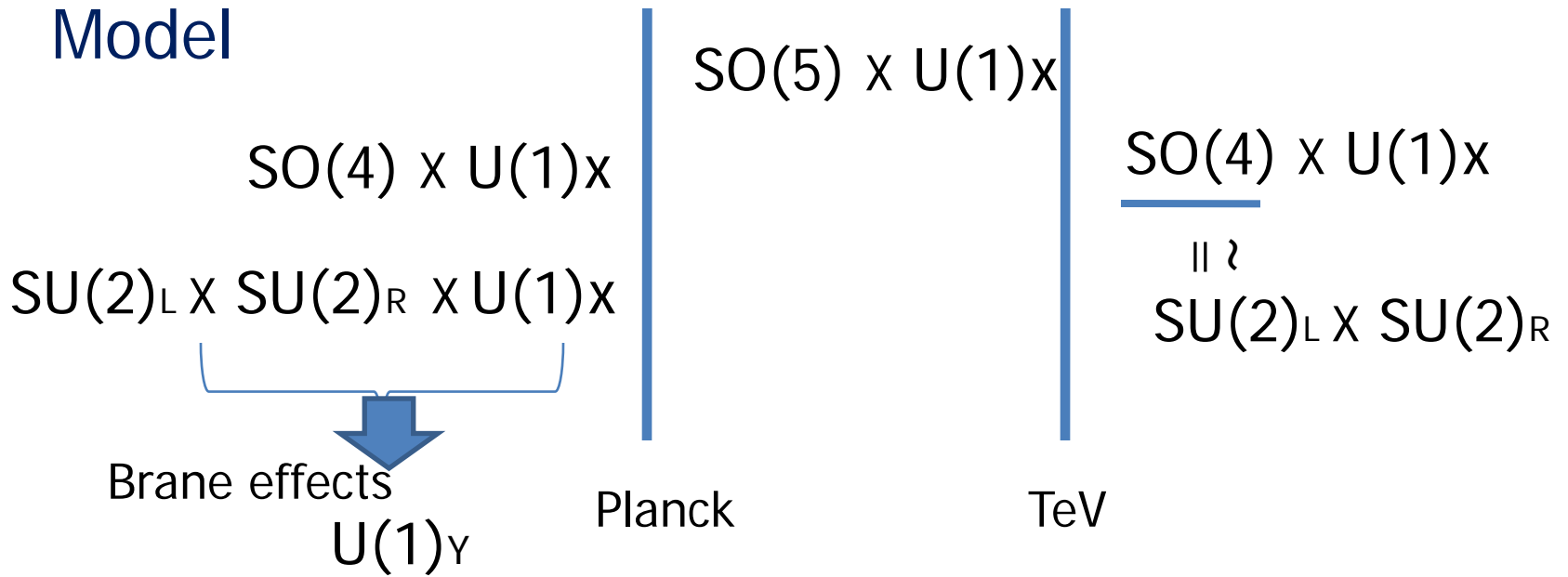
$SU(2)_L \times SU(2)_R$



$SU(2)_V$



# Model



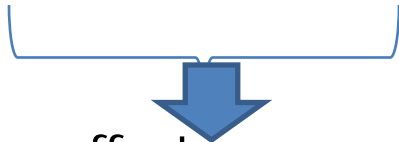
$$Q_X = 2/3 \quad \left( \begin{array}{cc} T & t \\ B & b \end{array} \right), \quad t'$$

$$Q_X = -1/3 \quad \left( \begin{array}{cc} U & X \\ D & Y \end{array} \right), \quad b'$$

# Model

$$SO(4) \times U(1)_X$$

$$SU(2)_L \times SU(2)_R \times U(1)_X$$



Brane effects  
 $U(1)_Y$

Planck

$$SO(5) \times U(1)_X$$

TeV

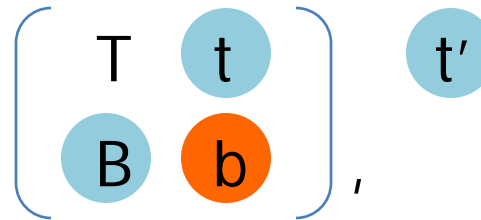
$$\underline{SO(4) \times U(1)_X}$$

$\cong$

$$SU(2)_L \times SU(2)_R$$

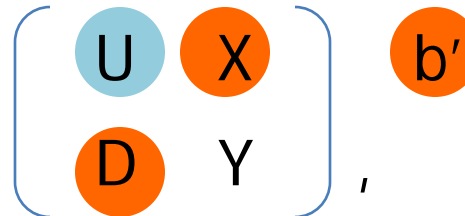
$$Q = T_L^3 + T_R^3 + Q_X$$

$$Q_X = 2/3$$



$$Q = 2/3$$

$$Q_X = -1/3$$



$$Q = -1/3$$

bulk	$Q_X$		$\frac{1}{2}Y$	$Q_E$	on the brane	$Q_X, \frac{1}{2}Y$	$Q_E$			
$\Psi_1$	$2/3$	$Q_1 = \begin{pmatrix} T \\ B \end{pmatrix}$	$7/6$	$5/3$	$\hat{\chi}_{1R} = \begin{pmatrix} \hat{T}_R \\ \hat{B}_R \end{pmatrix}$	$7/6$	$5/3$			
		$q = \begin{pmatrix} t \\ b \end{pmatrix}$	$1/6$	$2/3$						
		$t'$	$2/3$	$-1/3$						
$\Psi_2$	$-1/3$	$Q_2 = \begin{pmatrix} U \\ D \end{pmatrix}$	$1/6$	$2/3$	$\hat{\chi}_{2R} = \begin{pmatrix} \hat{U}_R \\ \hat{D}_R \end{pmatrix}$	$1/6$	$2/3$			
		$Q_3 = \begin{pmatrix} X \\ Y \end{pmatrix}$	$-5/6$	$-1/3$				$\hat{\chi}_{3R} = \begin{pmatrix} \hat{X}_R \\ \hat{Y}_R \end{pmatrix}$	$-5/6$	$-1/3$
		$b'$	$-1/3$	$-4/3$						
$\Psi_3$	$-1$	$\ell = \begin{pmatrix} \nu_\tau \\ \tau \end{pmatrix}$	$-1/2$	$0$	$\hat{\chi}_{1R}^\ell = \begin{pmatrix} \hat{L}_{1XR} \\ \hat{L}_{1YR} \end{pmatrix}$	$-3/2$	$-1$			
		$L_1 = \begin{pmatrix} L_{1X} \\ L_{1Y} \end{pmatrix}$	$-3/2$	$-1$						
		$\tau'$	$-1$	$-2$						
$\Psi_4$	$0$	$L_2 = \begin{pmatrix} L_{2X} \\ L_{2Y} \end{pmatrix}$	$1/2$	$1$	$\hat{\chi}_{2R}^\ell = \begin{pmatrix} \hat{L}_{2XR} \\ \hat{L}_{2YR} \end{pmatrix}$	$1/2$	$0$			
		$L_3 = \begin{pmatrix} L_{3X} \\ L_{3Y} \end{pmatrix}$	$-1/2$	$0$				$\hat{\chi}_{3R}^\ell = \begin{pmatrix} \hat{L}_{3XR} \\ \hat{L}_{3YR} \end{pmatrix}$	$-1/2$	$0$
		$\nu'_\tau$	$0$	$-1$						
			$0$	$0$			$-1$			

SU(2)<sub>L</sub> x SU(2)<sub>R</sub> x U(1) x anomaly free

# Quark

bulk	$Q_X$	$\frac{1}{2}Y$	$Q_E$	on the brane	$Q_X, \frac{1}{2}Y$	$Q_E$
$\Psi_1$	2/3	$Q_1 = \begin{pmatrix} T \\ B \end{pmatrix}$	$\begin{matrix} 7/6 & 5/3 \\ \leftarrow & \rightarrow \\ 2/3 & \end{matrix}$	$\hat{\chi}_{1R} = \begin{pmatrix} \hat{T}_R \\ \hat{B}_R \end{pmatrix}$	7/6	5/3
		$q = \begin{pmatrix} t \\ b \\ t' \end{pmatrix}$	$\begin{matrix} 1/6 & 2/3 \\ \leftarrow & \rightarrow \\ 2/3 & -1/3 \end{matrix}$			
$\Psi_2$	-1/3	$Q_2 = \begin{pmatrix} U \\ D \end{pmatrix}$	$\begin{matrix} 2/3 & 2/3 \\ \leftarrow & \rightarrow \\ -1/3 & \end{matrix}$	$\hat{\chi}_{2R} = \begin{pmatrix} \hat{U}_R \\ \hat{D}_R \end{pmatrix}$	1/6	2/3
		$Q_3 = \begin{pmatrix} X \\ Y \\ b' \end{pmatrix}$	$\begin{matrix} -1/3 & -1/3 \\ \leftarrow & \rightarrow \\ 5/6 & -1/3 \end{matrix}$			
$\Psi_3$	-1	$\ell = \begin{pmatrix} \nu_\tau \\ \tau \end{pmatrix}$	$\begin{matrix} 0 & -1 \\ \leftarrow & \rightarrow \\ -1 & -1 \end{matrix}$	$\hat{\chi}_{1R}^\ell = \begin{pmatrix} \hat{L}_{1XR} \\ \hat{L}_{1YR} \end{pmatrix}$	-3/2	-1
		$L_1 = \begin{pmatrix} L_{1X} \\ L_{1Y} \\ \tau' \end{pmatrix}$	$\begin{matrix} -3/2 & -1 \\ \leftarrow & \rightarrow \\ -1 & -1 \end{matrix}$			
$\Psi_4$	0	$L_2 = \begin{pmatrix} L_{2X} \\ L_{2Y} \end{pmatrix}$	$\begin{matrix} 1 & 1 \\ \leftarrow & \rightarrow \\ 0 & \end{matrix}$	$\hat{\chi}_{2R}^\ell = \begin{pmatrix} \hat{L}_{2XR} \\ \hat{L}_{2YR} \end{pmatrix}$	1/2	1
		$L_3 = \begin{pmatrix} L_{3X} \\ L_{3Y} \\ \nu'_\tau \end{pmatrix}$	$\begin{matrix} 0 & 1 \\ \leftarrow & \rightarrow \\ 0 & 0 \end{matrix}$			

Lepton

$\mu_3$

SU(2)<sub>L</sub> x SU(2)<sub>R</sub> x U(1) x anomaly free

# 4次元ラグランジアン

b クォークの Z boson coupling

$$\mathcal{L}_{Zb\bar{b}} = \frac{g_A Z_\mu}{\cos \theta_W} \left( \mathcal{B}_L \bar{b}_L \gamma^\mu b_L + \mathcal{B}_R \bar{b}_R \gamma^\mu b_R \right)$$

$$\mathcal{B}_{L,R} = -\frac{1}{2}\mathcal{B}_{L,R}^3 + \frac{1}{3}\mathcal{B}_{L,R}^Q \sin^2 \theta_W$$

$$\mathcal{B}_L^3 = \int_1^{z_L} dz [N_Z(z)(C_L(z; \lambda_b))^2 (a_b^2 + 2 \cos \theta_H a_{D+X} a_{D-X}) + 2 \sin \theta_H D_Z(z) C_L(z; \lambda_b) S_L(z; \lambda_b) a_{D+X} a_{b'}],$$

$$\mathcal{B}_L^Q = \int_1^{z_L} dz N_Z(z) [(C_L(z; \lambda_b))^2 (a_b^2 + a_{D+X}^2 + a_{D-X}^2) + (S_L(z; \lambda_b))^2 a_{b'}^2].$$



# 4次元ラグランジアン

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$$\mathcal{B}_{L,R} = -\frac{1}{2} \mathcal{B}_{L,R}^3 + \frac{1}{3} \mathcal{B}_{L,R}^Q \sin^2 \theta_W$$

$$\mathcal{B}_L^3 = \int_1^{z_L} dz [N_Z(z)(C_L(z; \lambda_b))^2 + 2 \sin \theta_H D_Z(z) C_L(z; \lambda_b) S] \mathcal{B}_L \xrightarrow{\text{SM}} -\frac{1}{2} + \frac{1}{3} \sin^2 \theta_W$$

$$\mathcal{B}_L^Q = \int_1^{z_L} dz N_Z(z) [(C_L(z; \lambda_b))^2] \mathcal{B}_R \xrightarrow{\text{SM}} \frac{1}{3} \sin^2 \theta_W$$

## Standard Modelからのずれ

$$Zt_L\bar{t}_L \quad Zt_R\bar{t}_R \quad Zb_L\bar{b}_L \quad Zb_R\bar{b}_R$$

$$7\% \quad 18\% \quad 0.3\% \quad 0.9\%$$

$$\frac{\text{coupling in } SO(5)\times U(1) \text{ model}}{\text{coupling in standard model}} - 1$$

そのほかも、1%以下

## universality の破れ (W boson coupling)

$$\mu-e$$

$$10^{-8}$$

$$\tau-e$$

$$10^{-6}$$

$$t-e$$

$$2.3\%$$

## Currents and custodial symmetry

$$\frac{g}{\cos \theta_w} Z_\mu \bar{f} \gamma^\mu (I_f^3 - Q_f \sin^2 \theta_w) f$$

# Currents and custodial symmetry

$$\frac{g}{\cos \theta_w} Z_\mu \bar{f} \gamma^\mu (I_f^3 - Q_f \sin^2 \theta_w) f$$

↑ conserved

Symmetry and conserved charges

non-universal? after EWSB

- $SU(2)_L \times SU(2)_R \times P_{LR} \longrightarrow SU(2)_V \times P_{LR}$
- subgroup  $U(1)_L \times U(1)_R \times P_{LR} \longrightarrow U(1)_V \times P_{LR}$

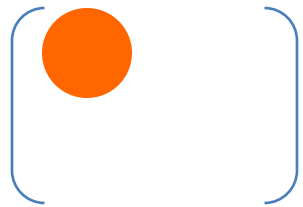
$$U(1)_V \quad Q_V = Q_L + Q_R \longrightarrow Q_L \quad \overset{\text{red arrow}}{\curvearrowright} \quad I_f^3$$

$P_{LR}$

L ↔ R 入れ替え対称なら、  
non-universal なずれは小さいはず

Agashe, Contino, Da Rold,  
Pomarol 06

(Isospin<sub>L</sub>, T<sub>L</sub><sup>3</sup>; Isospin<sub>R</sub>, T<sub>R</sub><sup>3</sup>)

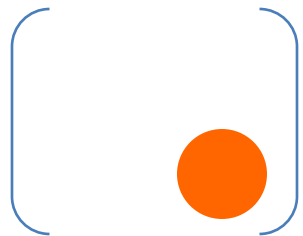


0

$$\left(\frac{1}{2}, +; \frac{1}{2}, +\right)$$

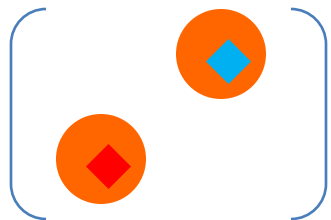


(0; 0)



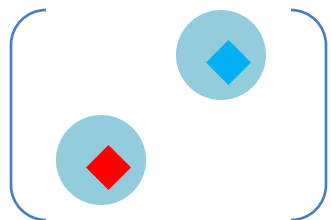
0

$$\left(\frac{1}{2}, -; \frac{1}{2}, -\right)$$



0

$$\left(\frac{1}{2}, -; \frac{1}{2}, +\right) + \left(\frac{1}{2}, +; \frac{1}{2}, -\right)$$



0

$$\left(\frac{1}{2}, -; \frac{1}{2}, +\right) - \left(\frac{1}{2}, +; \frac{1}{2}, -\right)$$

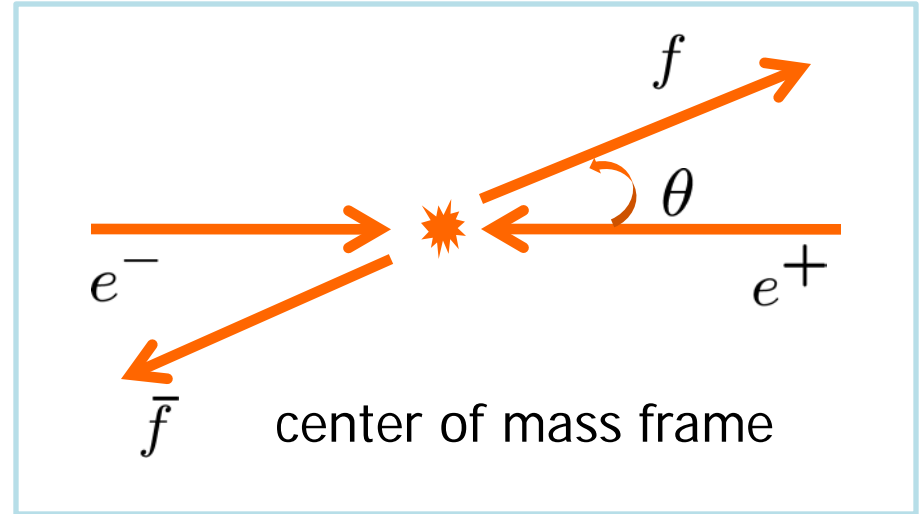
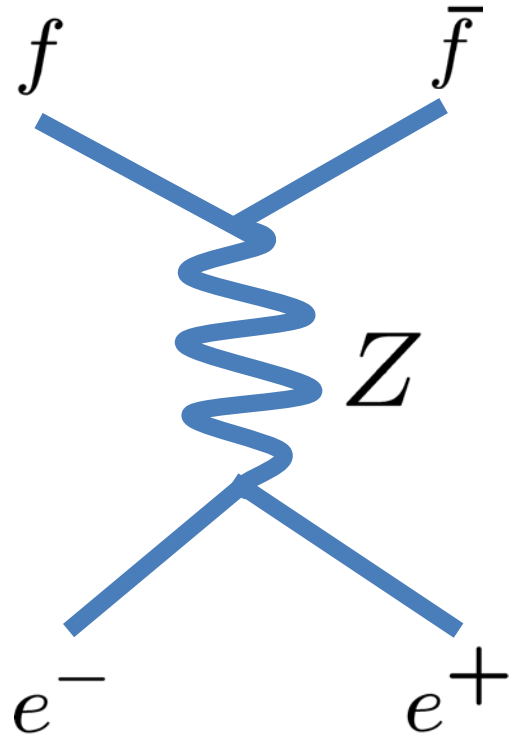
$$\propto \cos \theta_H$$

$$\theta_H = \frac{\pi}{2}$$

L ↔ R 非対称

部分がゼロ

# 散乱過程で引き出す物理量



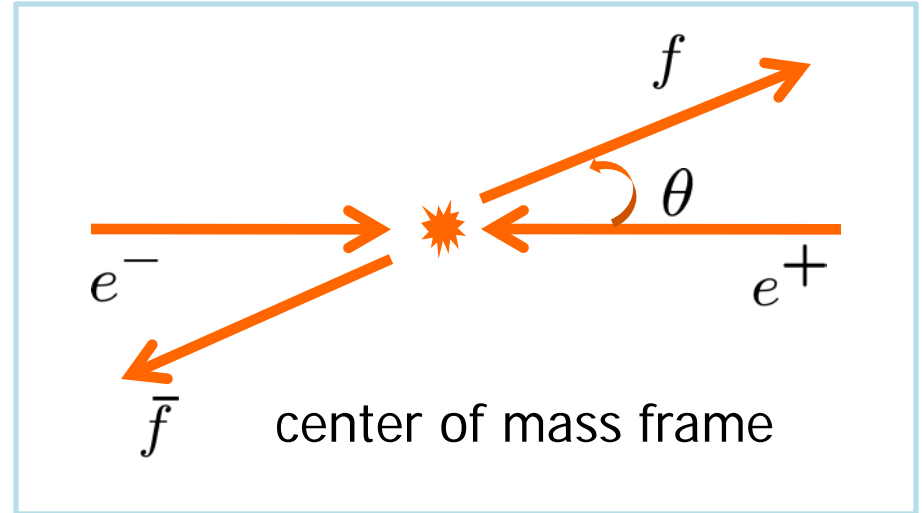
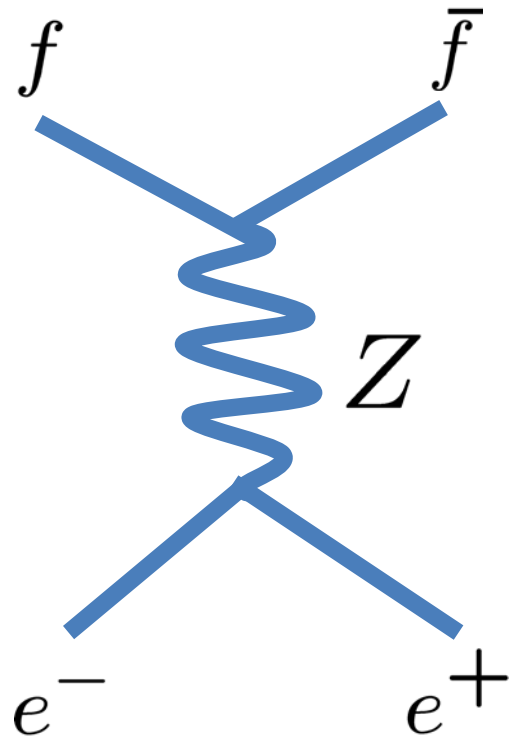
$$\frac{d\sigma}{d\Omega}(e_R^- e_L^+ \rightarrow f_R \bar{f}_L) = \frac{\alpha^2}{4E_{cm}^2} (1 + \cos\theta)^2 (g_R^e)^2 (g_R^f)^2$$

$$\frac{d\sigma}{d\Omega}(e_R^- e_L^+ \rightarrow f_L \bar{f}_R) = " (1 - \cos\theta)^2 (g_R^e)^2 (g_L^f)^2$$

$$\frac{d\sigma}{d\Omega}(e_L^- e_R^+ \rightarrow f_R \bar{f}_L) = " (1 - \cos\theta)^2 (g_L^e)^2 (g_R^f)^2$$

$$\frac{d\sigma}{d\Omega}(e_L^- e_R^+ \rightarrow f_L \bar{f}_R) = " (1 + \cos\theta)^2 (g_L^e)^2 (g_L^f)^2$$

# 散乱過程で引き出す物理量



Forward-backward asymmetry

$$A_{FB}^f = \frac{(\int_0^1 - \int_{-1}^0) d \cos \theta \frac{d\sigma(e^-e^+ \rightarrow f\bar{f})}{d \cos \theta}}{(\int_0^1 + \int_{-1}^0) d \cos \theta \frac{d\sigma(e^-e^+ \rightarrow f\bar{f})}{d \cos \theta}} = \frac{3}{4} A_{LR}^e A_{LR}^f$$

Polarization asymmetry of decay  $Z \rightarrow f\bar{f}$

$$A_{LR}^f = \frac{(g_L^f)^2 - (g_R^f)^2}{(g_L^f)^2 + (g_R^f)^2}$$

# 16コパラメータがある。

- バルク質量パラメータ  $c$

計6コ クォーク3、レプトン3

- 相対的なブレイン結合パラメータ

$$|\tilde{\mu}/\mu_2|, |\mu_3^\ell/\tilde{\mu}^\ell|$$

計6コ クォーク3、レプトン3

- ゲージ結合定数

計2コ  $SO(5)$ と $U(1)$

- 時空の曲率  $k$ , 余剰次元長さ  $L$



# 16コパラメータがある。

- バルク質量パラメータ  $c$

クォークの  
質量  
6コ

レプトンの  
質量  
6コ

- ゲージ結合定数  
 $\sin \theta_W, m_Z$

- 時空の曲率  $k$ , 余剰次元

ワープ因子

$$z_L = e^{kL}$$

Xing-Zhang-Zhou '07, Fusaoka-Koide '97, Particle Data Group '08 (in unit of MeV)

	$m_u$	$m_d$	$m_s$	$m_c$	$m_b$	$m_t$	$m_e$	$m_\mu$	$m_\tau$
XZZ	1.27	2.90	55	619	2890	171700	0.486570161	102.7181359	1746.24
FK	2.33	4.69	93.4	677	3000	181000	0.48684727	102.75138	1746.69
PDG	2.4	4.75	104	1270	4200	171200	0.510998910	105.658367	1776.84

$$\sin^2 \theta_W = 0.2312 \text{ (}\overline{\text{MS}} \text{ in PDG)}$$

$$m_Z = 91.1876 \text{ GeV}$$

$$z_L = (10^{18} \text{ GeV}) / (1 \text{ TeV}) = 10^{15}$$

$$k = 4.7 \times 10^{17} \text{ GeV}$$

such that the value of  $m_W$  is appropriately reproduced

$$A^b_{FB}$$

**実験データ**      **0.0992**  $\pm$  0.0016

Standard Model  
(PDG review)      0.1033  $\pm$  0.0007

Standard Model      0.10496 (tree)

XZZ, FK      **0.09952**      **中心値**  
PDG      **0.09941**      **に近い!**

$$A_{FB}^c$$

**実験データ** **0.0707**  $\pm$  0.0035

Standard Model  
(PDG review) 0.0738  $\pm$  0.0006

Standard Model 0.07500 (tree)

XZZ, FK **0.07073** **中心値**  
PDG **0.07065** **に近い!**

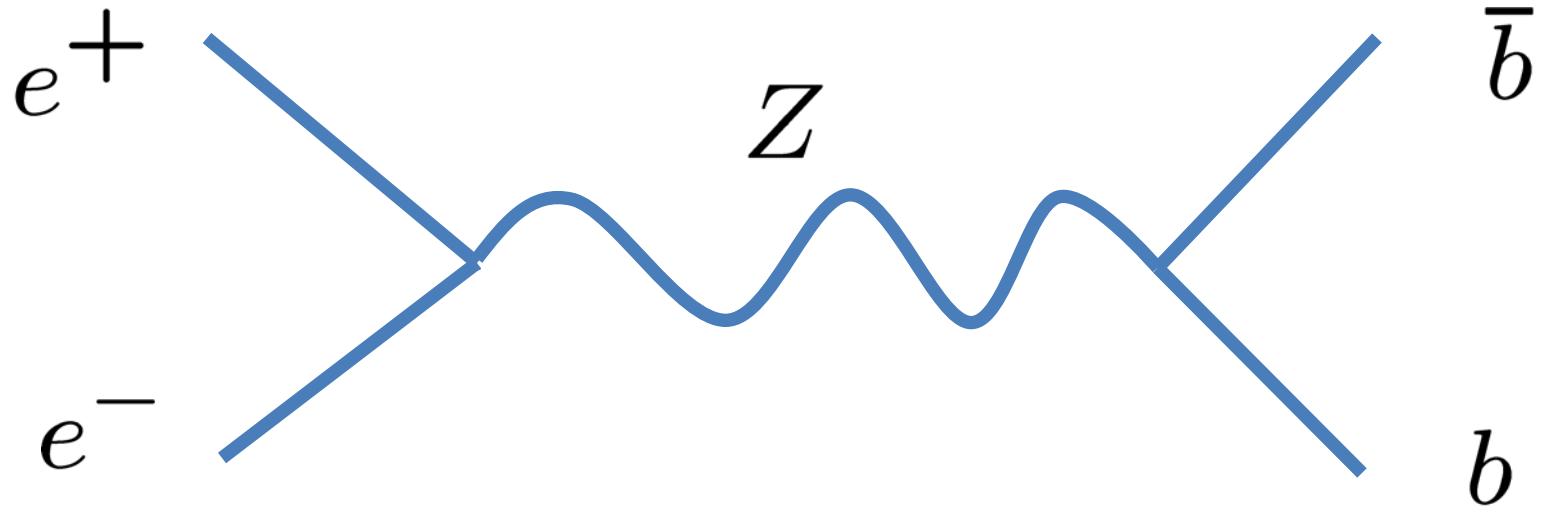
$$\begin{array}{ccc}
 z_L = 10^{15} & \xrightarrow{100\text{倍}} & z_L = 10^{17} \\
 k = 4.7 \times 10^{17} \text{ GeV} & & k = 5.0 \times 10^{19} \text{ GeV}
 \end{array}$$

$$\begin{array}{ccc}
 0.09952 & A_{FB}^b & 0.10019
 \end{array}$$

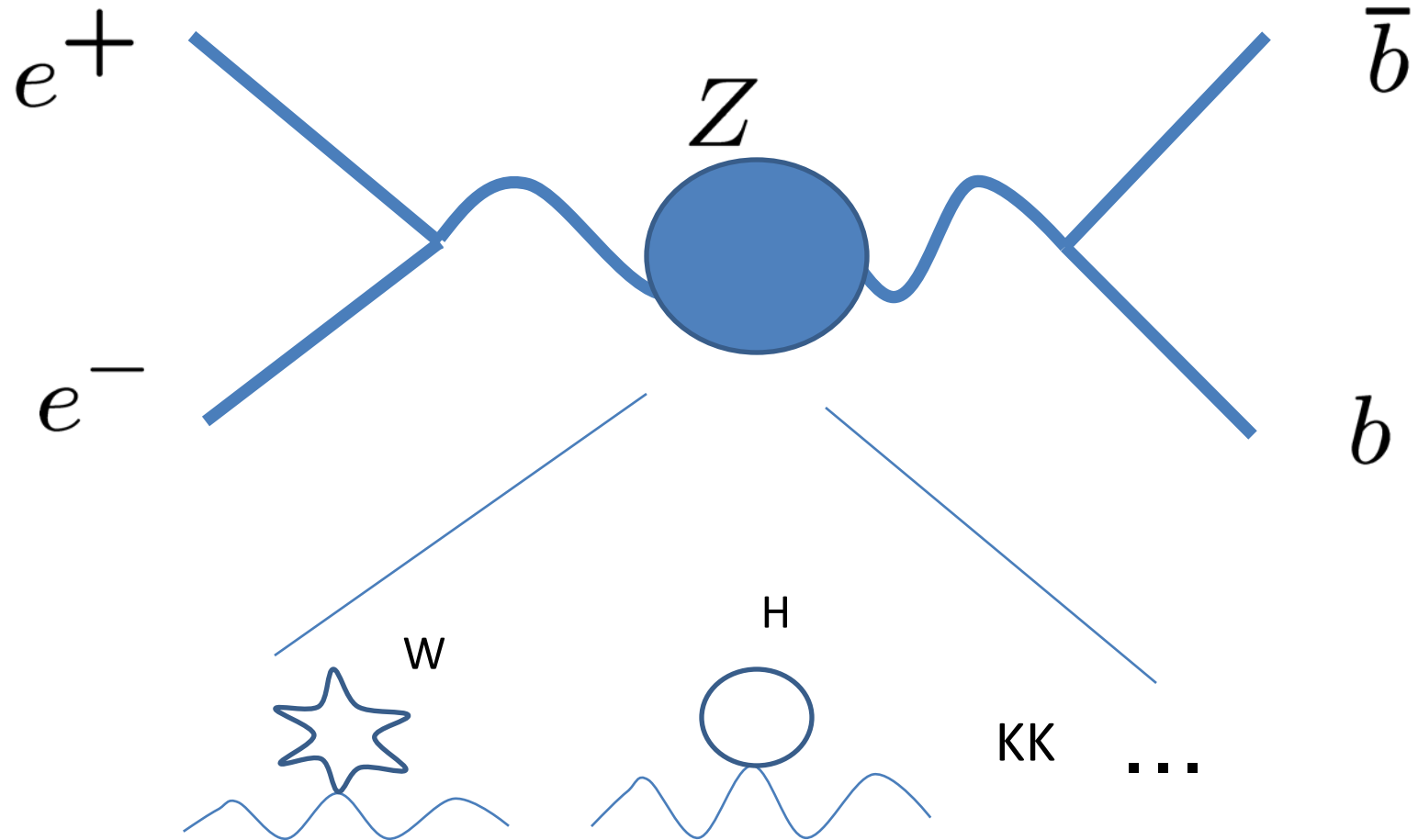
$$\begin{array}{ccc}
 0.07073 & A_{FB}^c & 0.07125
 \end{array}$$

パラメータを100倍しても、Standard Model  
より中心値に近い

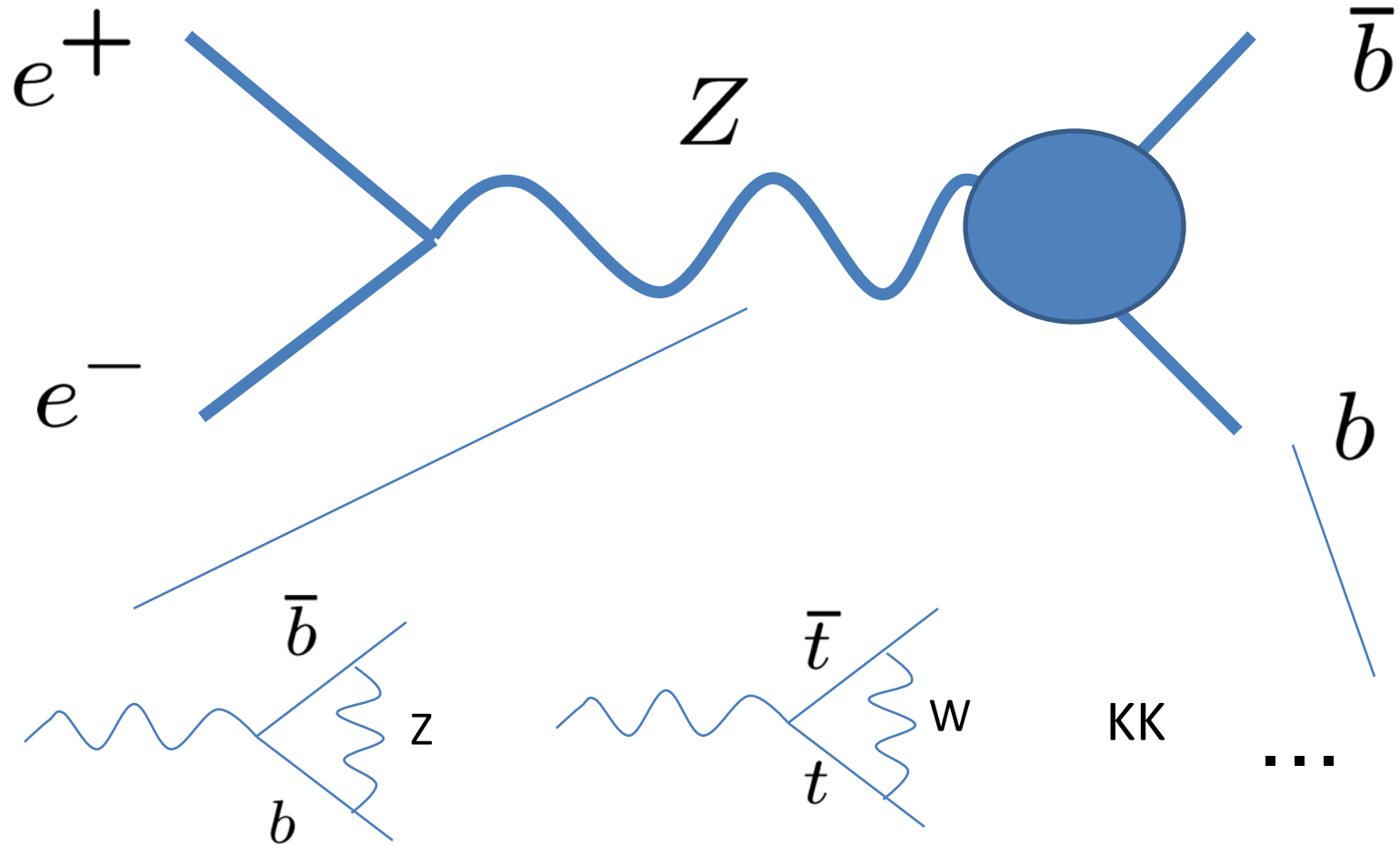
# Radiative corrections



# Radiative corrections



# Radiative corrections





# SUMMARY

実験データ  
中心値

SO(5)xU(1)  
tree-level 予言

$A_{FB}^b$

0.0992

0.09952

$A_{FB}^c$

0.0707

0.07073

● top はStandard Modelから最もずれる

$Zt_L\bar{t}_L$

7%

$Zt_R\bar{t}_R$

18%

そのほか、

1%以下

$\mu-e$

$10^{-8}$

$\tau-e$

$10^{-6}$

$t-e$

2.3%