

# **Universal turbulence on branes in holography**

**Akihiko Sonoda**(Osaka univ.)

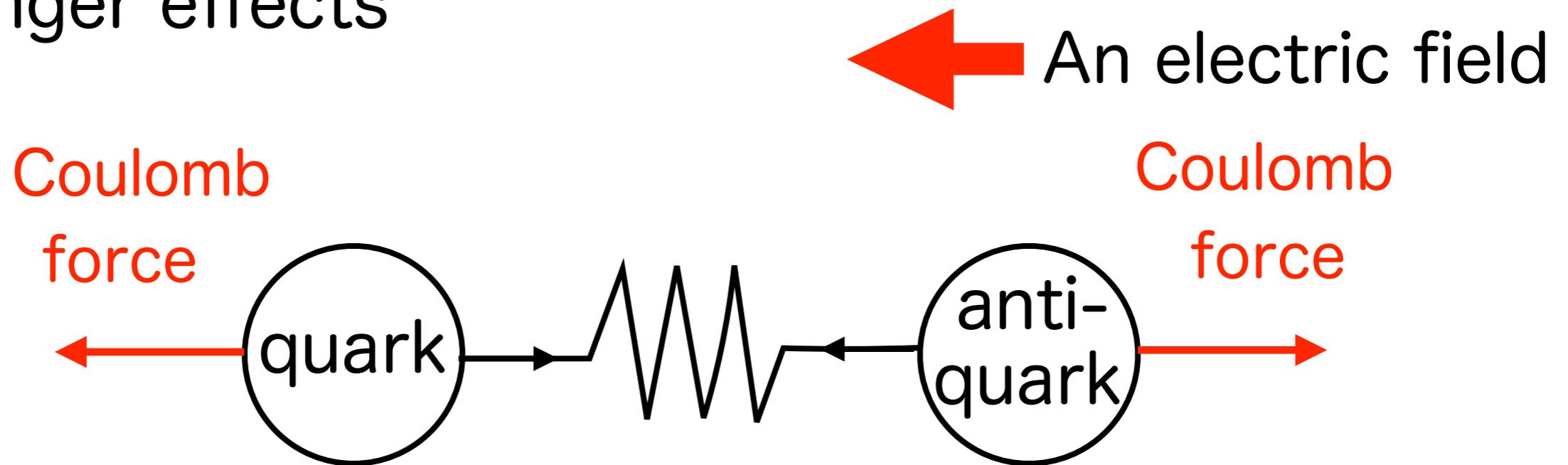
[arXiv:1504.XXXX(hep-th)]

Collaborators: Koji Hashimoto(Osaka univ.)  
Mitsuhiko Nishida(Osaka univ.)

## Introduction

# Power law scaling, universal phenomena

Schwinger effects



[K.Hashimoto, T.Oka (1307.7423)]

[K.Hashimoto, T.Oka, A.S (1403.6336)]

[K.Hashimoto, T.Oka, A.S (1412.4254)]

We evaluated **vacuum instability** induced by  
an electric field and a magnetic field.

→ Meson condensation at the phase boundary ?

## Introduction

# Power law scaling, universal phenomena

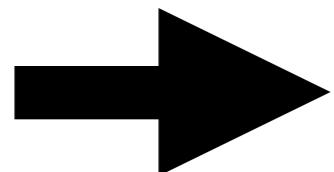
Power law scaling at the phase transition

ex1) Hagedorn transition in string theory

$$\rho(E_n) \exp\left(-\frac{E_n}{T}\right) \simeq E_n^\alpha \exp\left(\frac{E_n}{T_c}\right) \exp\left(-\frac{E_n}{T}\right) \text{ Power law}$$

ex2) Turbulent meson condensation

[Hashimoto, Kinoshita, Murata, Oka (1408.6293)]



Universality of turbulent meson ?

Weak turbulence in AdS space-time

[P.Bizon, A.Rostworowski(1104.3702 [gr-qc])]

Power law scaling:  $E_n \simeq n^\alpha$

## Problem

Universality of a **power law** on turbulent mesons condensation ?

## Methods

Gravity dual to D3-D5 brane(N=2 SQCD)

The fluctuation of the D5-brane by  
an electric field or a temperature



The spectrum of the scalar mesons

## Results

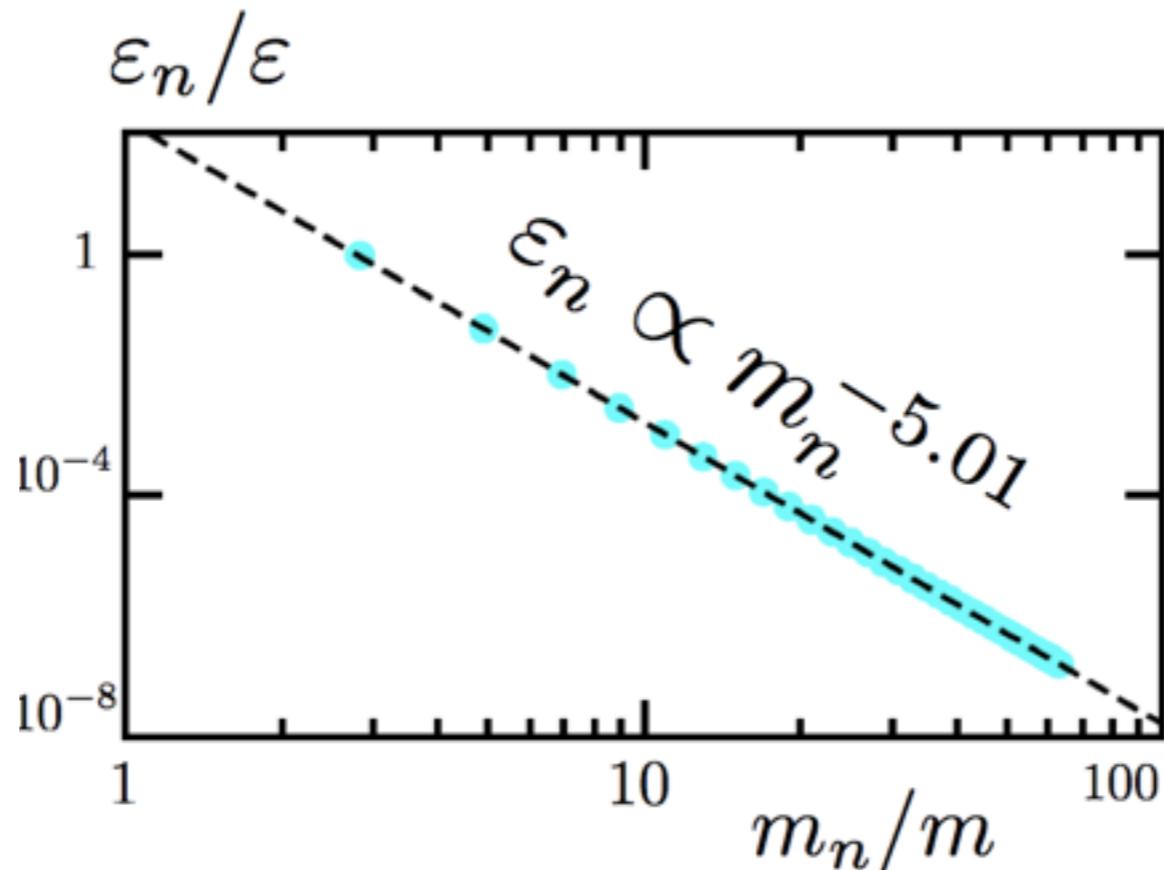
- The D5-branes have a **cusp** by the electric field or a temperature.
- (The energy of the n-th meson)  $\propto$  (mass)<sup>-4</sup>

# Problem

## Universality of a power law on turbulent mesons condensation ?

[Hashimoto, Kinoshita, Murata, Oka (1408.6293)]

In D3-D7 brane system(N=2 SQCD)



The power law of the n-th meson in  
the other brane systems ?

## Methods

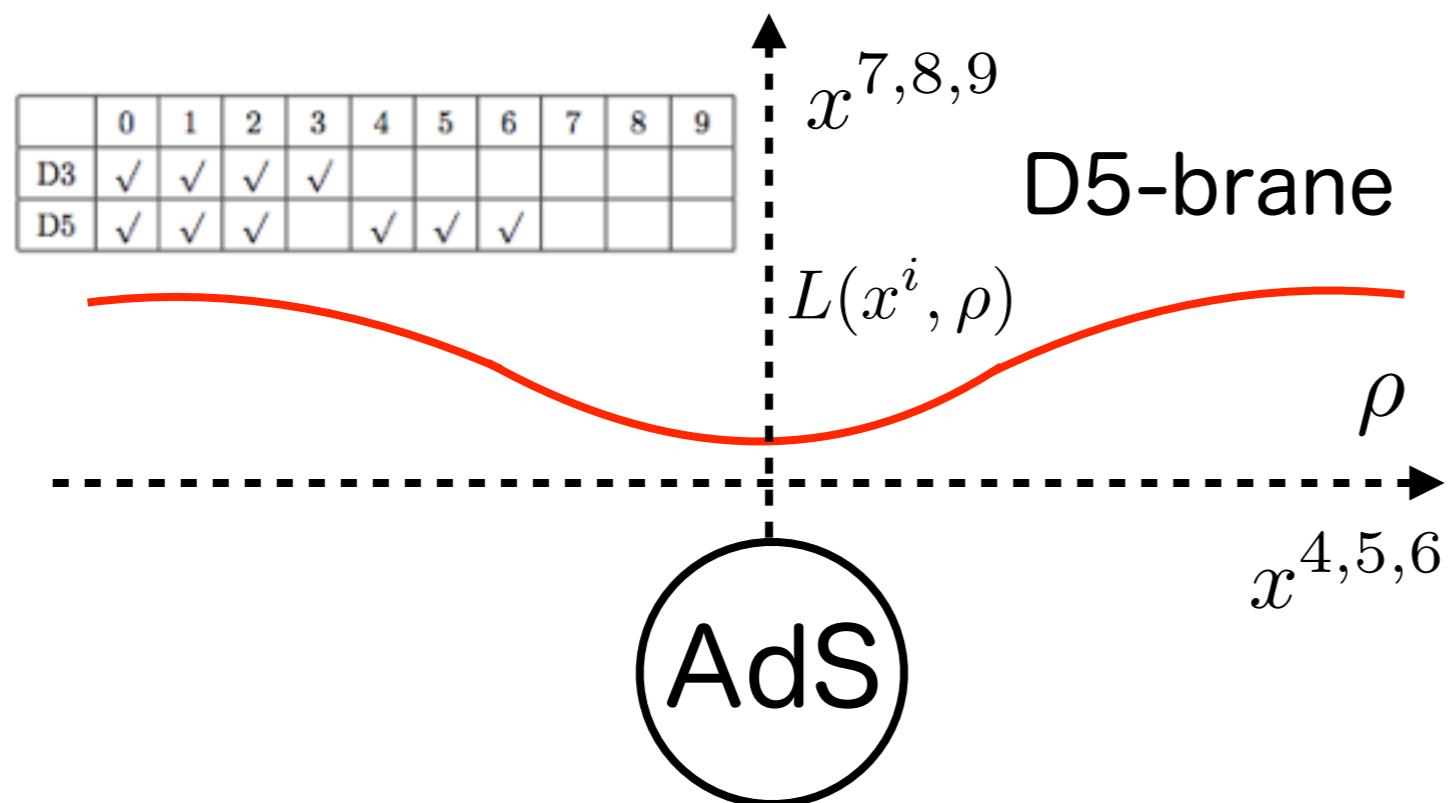
# Gravity dual to D3-D5 brane(N=2 SQCD)

The fluctuation of the D5-brane by  
an electric field or a temperature

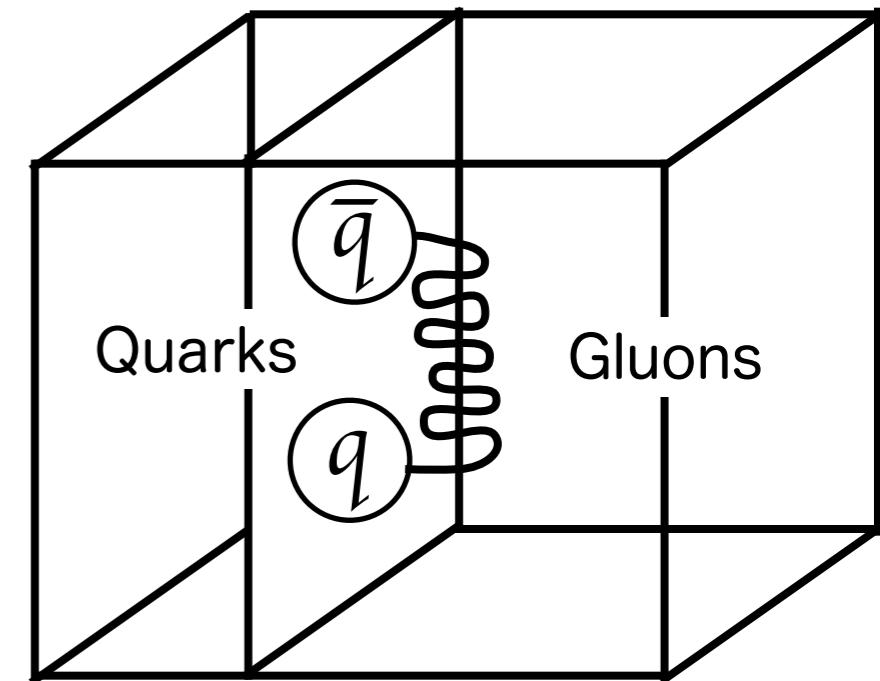


## The spectrum of the scalar mesons

D3-D5 brane(an electric field)



N=2 SQCD



The quarks on  
the domain wall

## Methods

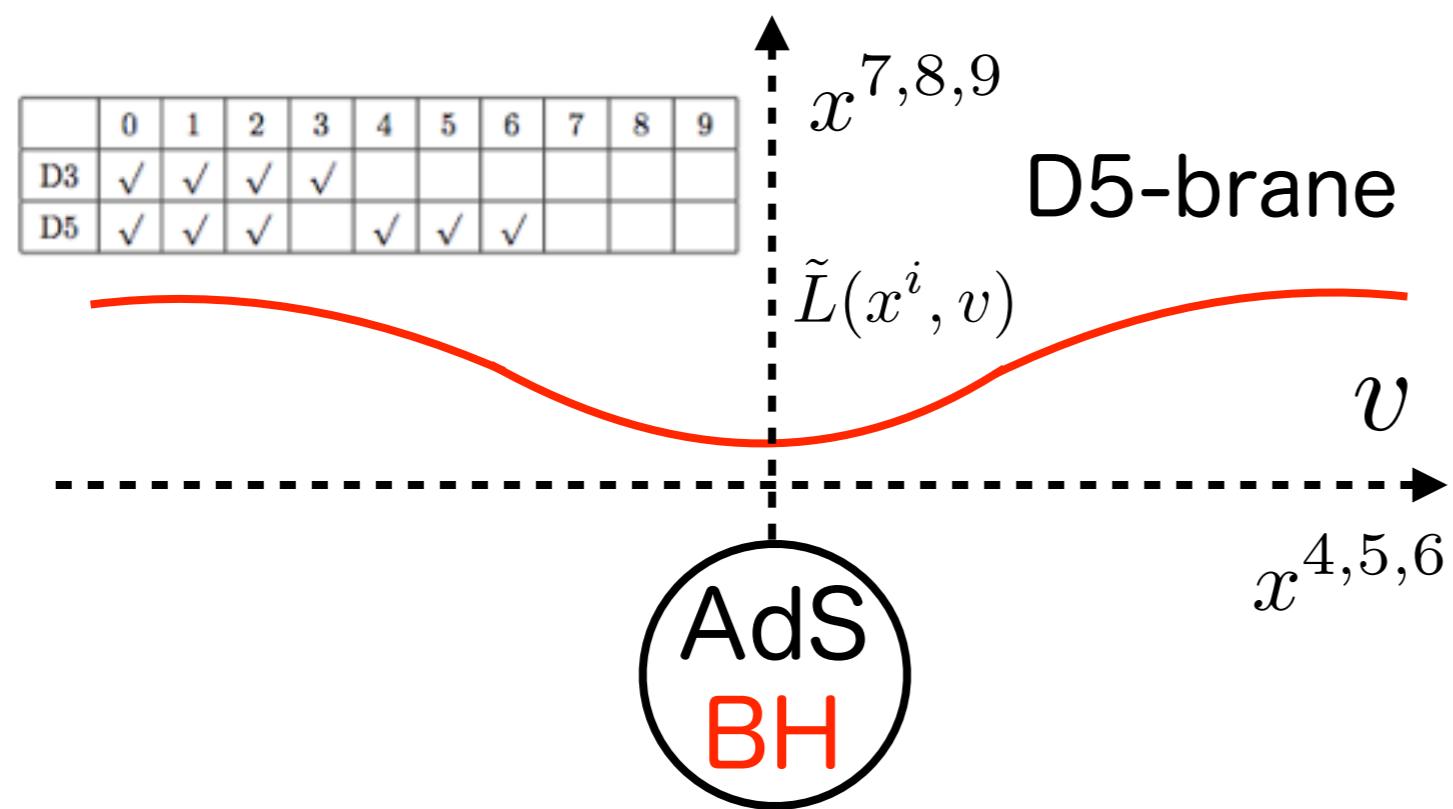
# Gravity dual to D3-D5 brane(N=2 SQCD)

The fluctuation of the D5-brane by  
an electric field or a temperature

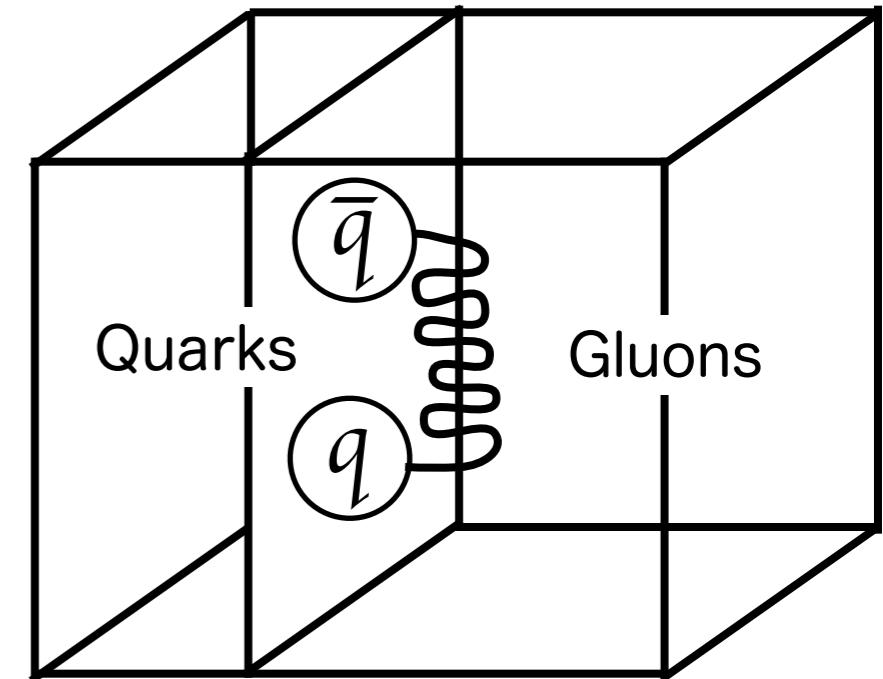


## The spectrum of the scalar mesons

D3-D5 brane(a temperature)



N=2 SQCD

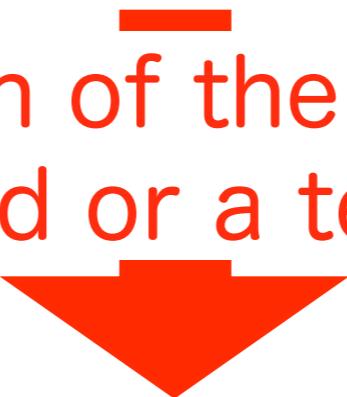


The quarks on  
the domain wall

# Methods

## Gravity dual to D3-D5 brane(N=2 SQCD)

The fluctuation of the D5-brane by  
an electric field or a temperature

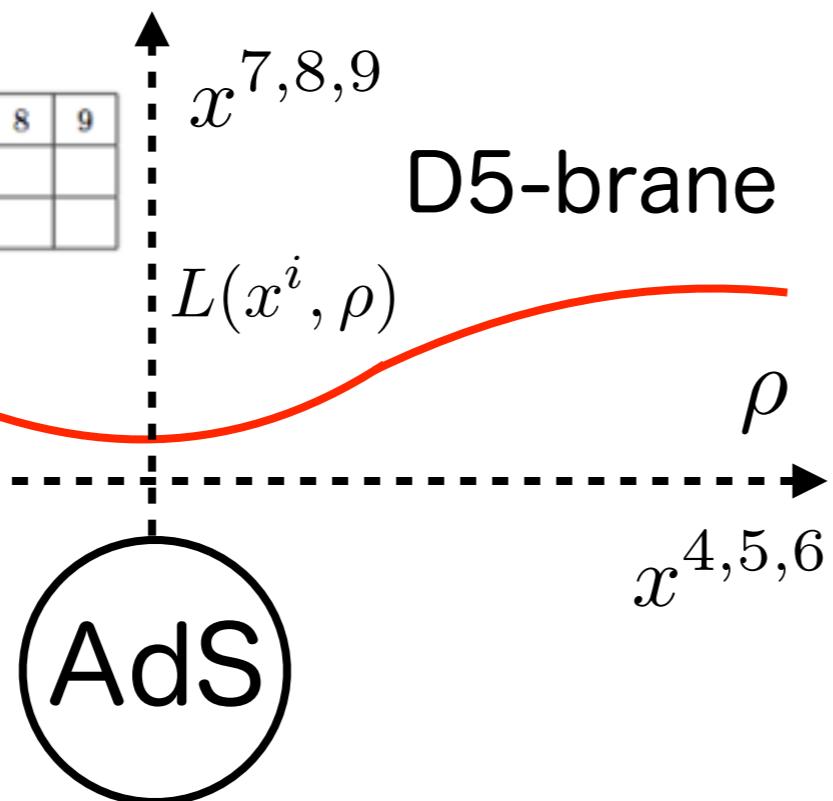


## The spectrum of the scalar mesons

### D3-D5 brane

	0	1	2	3	4	5	6	7	8	9
D3	✓	✓	✓	✓						
D5	✓	✓	✓		✓	✓	✓			

### D5-brane



### D5-brane action

$$S = -\tau_5 \int d^6\xi \sqrt{-\det(P[L(x^i, \rho)]_{ab} + 2\pi l_s^2 F_{ab})}$$

Scalar field:  $L(x^i, \rho)$   
 $(i = 0, 1, 2)$



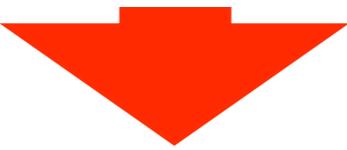
The energy and mass  
of the scalar meson

$$\epsilon_n, m_n \quad (n = 0, 1, 2, \dots)$$

# Methods

## Gravity dual to D3-D5 brane(N=2 SQCD)

The fluctuation of the D5-brane by  
an electric field or a temperature



## The spectrum of the scalar mesons

Meson effective action [R.C.Myers, R.M.Thomson (0605017)]

$$S = \int d^3x \int_0^\infty d\rho \frac{\rho^2 R^2 m}{2(\rho^2 + R^4 m^2)^2} \left[ (\partial_t \chi)^2 - \frac{(\rho^2 + R^4 m^2)^2}{R^4} (\partial_\rho \chi)^2 \right] + \mathcal{O}(\chi^3)$$

$$\left[ \frac{\partial^2}{\partial t^2} - \frac{(\rho^2 + R^4 m^2)^2}{\rho^2 R^2 m} \frac{\partial}{\partial \rho} \frac{\rho^2 m}{R^2} \frac{\partial}{\partial \rho} \right] \chi = 0 \quad \text{E.O.M.} \quad \chi = \sum_{n=0}^{\infty} c(t) e_n(\rho) \quad \text{Meson modes}$$

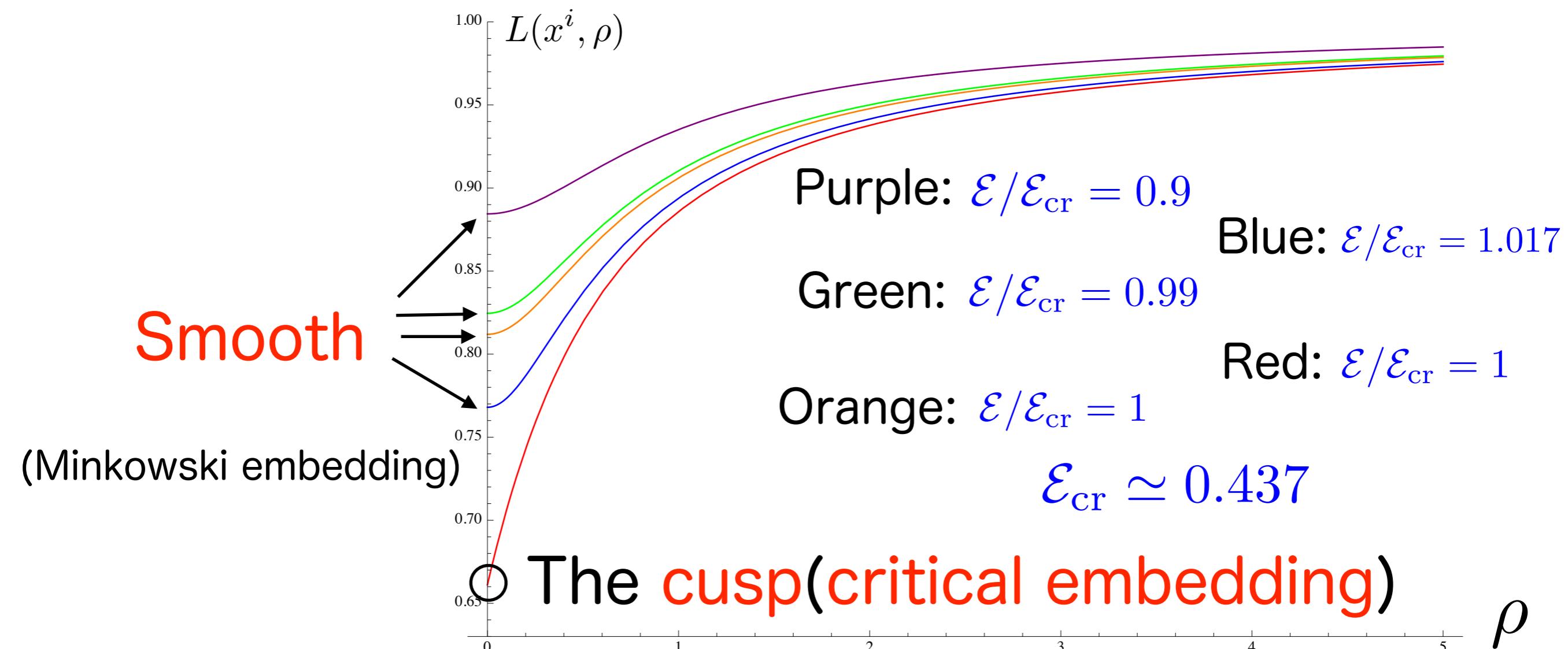
$$e_n(\rho) \equiv N_n F \left( -n, -1/2 - n, 3/2; -\frac{\rho^2}{R^4 m^2} \right) \quad \Omega_n \equiv 2 \sqrt{(1/2 + n)(3/2 + n)} m$$

$$S = \int d^3x \sum_{n=0}^{\infty} \left[ \frac{1}{2} \dot{c}_n^2 - \frac{1}{2} \Omega_n^2 c_n^2 \right] + \mathcal{O}(\chi^3) \quad \begin{matrix} \text{Meson} \\ \text{energy} \end{matrix} \quad \varepsilon_n \equiv \frac{1}{2} (\dot{c}_n^2 + \Omega_n^2 c_n^2)$$

# Results

- The D5-branes have a **cusp** by the **electric field** or a **temperature**.
- (The energy of the n-th meson)  $\propto$  (mass)<sup>-4</sup>

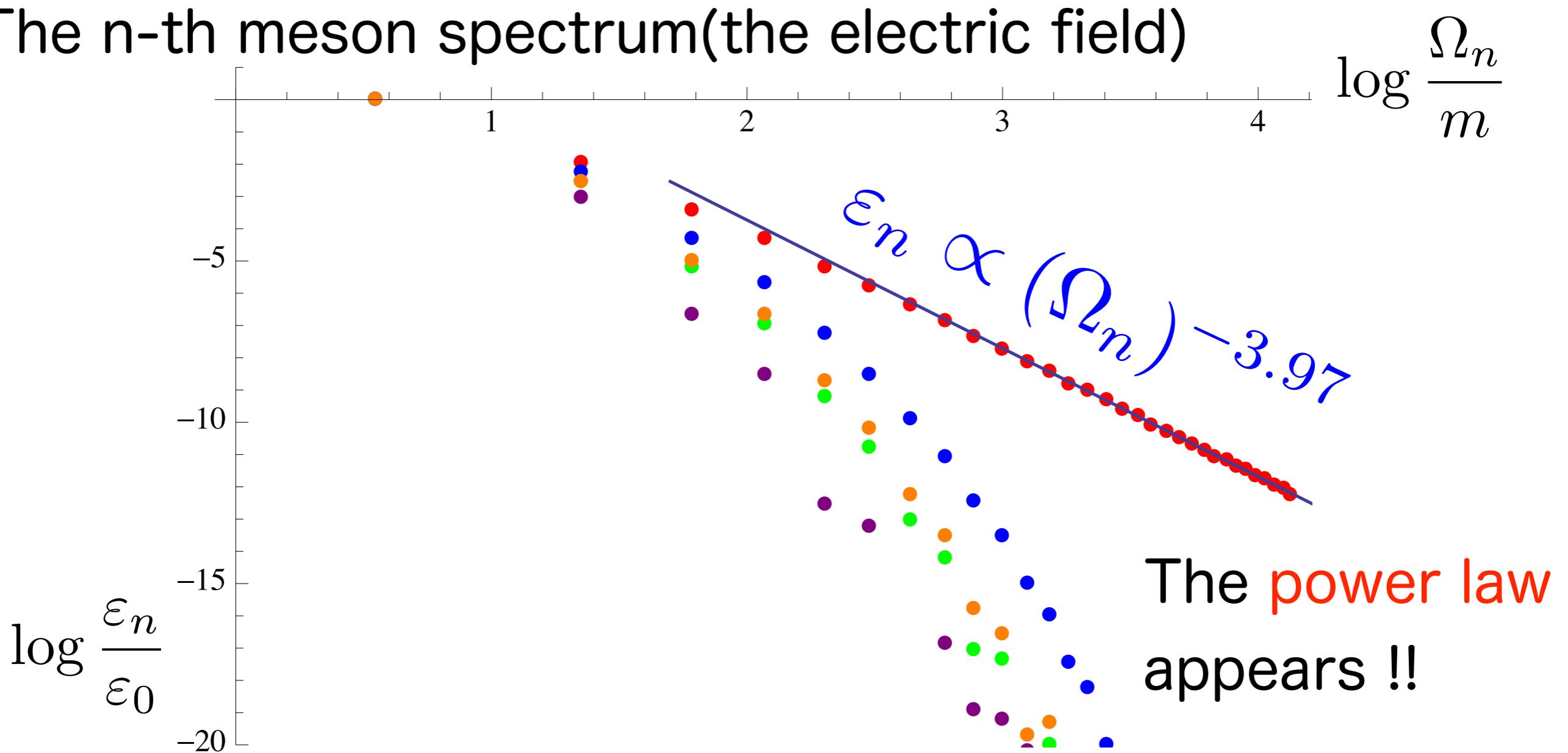
The shape of the D5-brane(the electric field)



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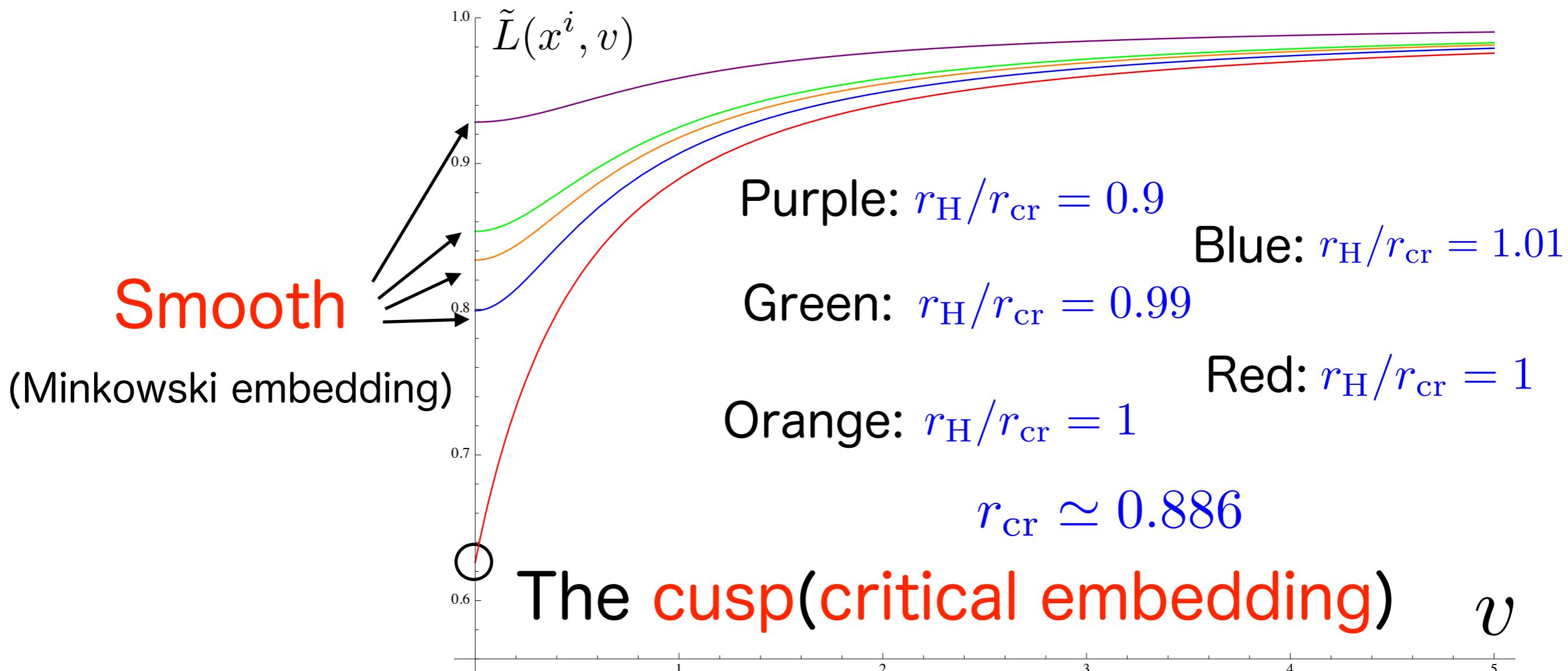
The n-th meson spectrum(the electric field)



# Results

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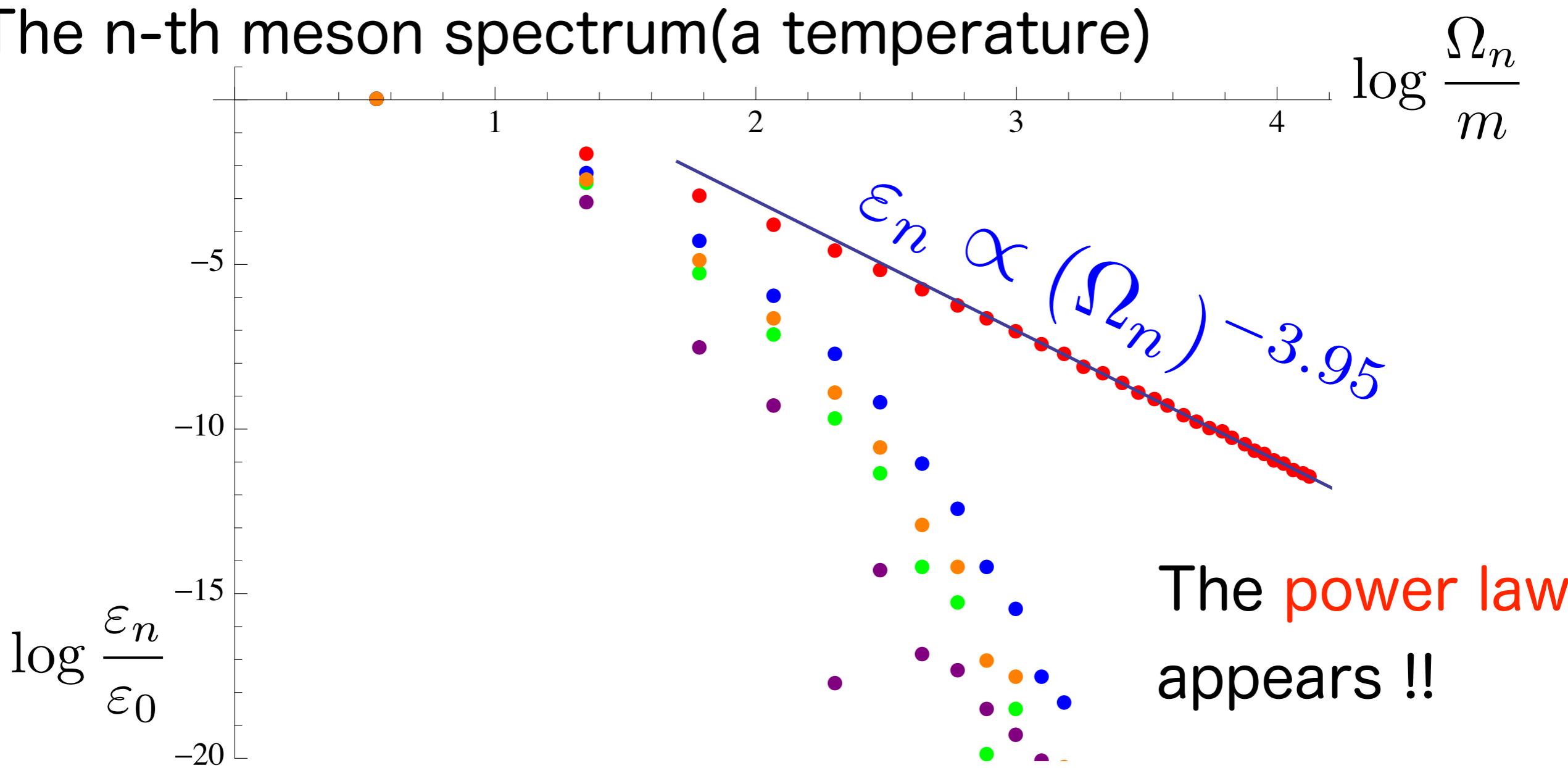
The shape of the D5-brane(a temperature)



# Results

- The D5-branes have a **cusp** by the **electric field** or a **temperature**.
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The n-th meson spectrum(a temperature)



# Conjectures

The power law  $\alpha$  depends on only the dimensionality of the brane cone:  $-(d_{\text{cone}} + 1)$

	0	1	2	3	4	5	6	7	8	9
D3	✓	✓	✓	✓						
D5	✓	✓	✓		✓	✓	✓			

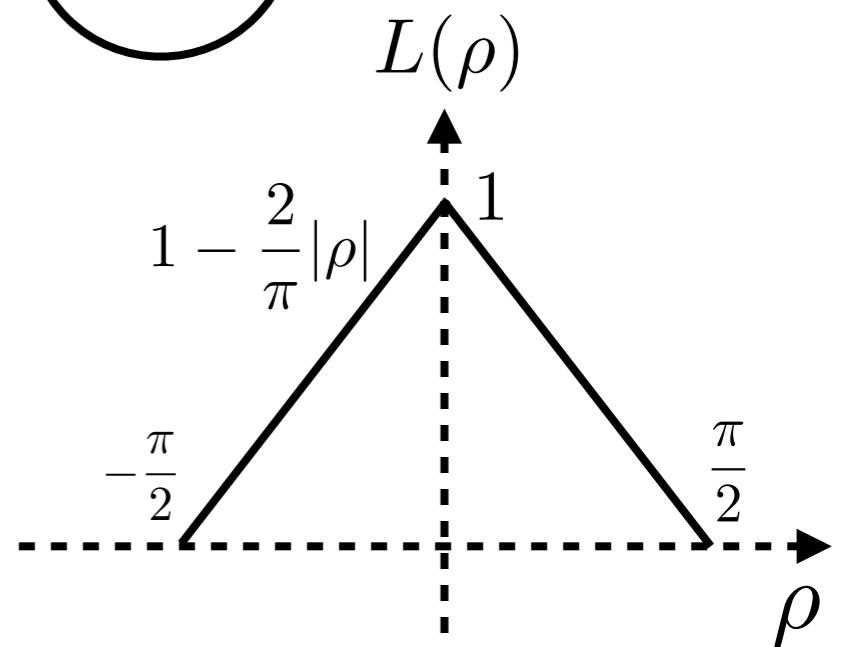
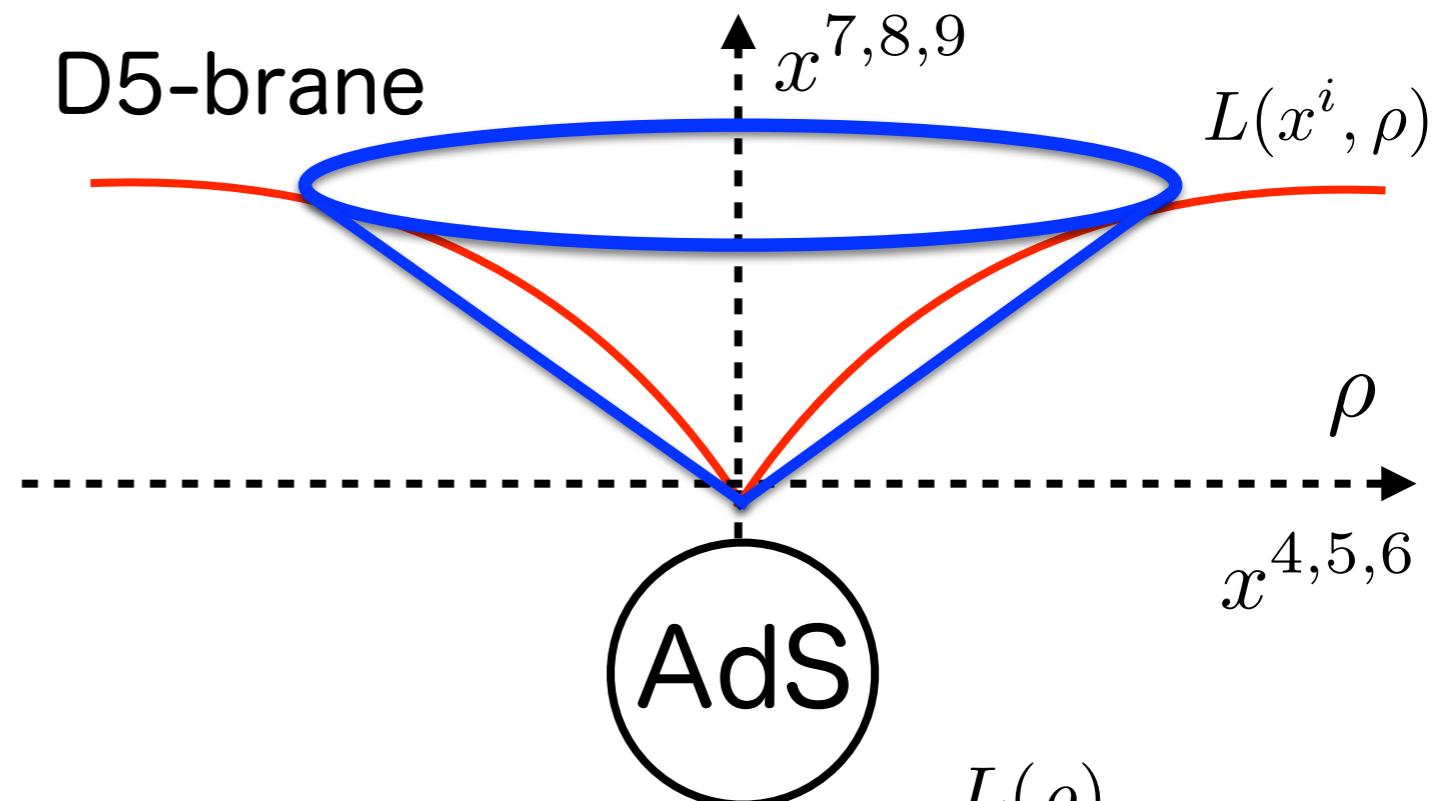
3-dimensional cone!!

Ex. 1-dimensional cone

$$L(\rho) = \sum_{n=0}^{\infty} c_n e_n(\rho)$$

$$\varepsilon_n \equiv \frac{1}{2} m_n^2 c_n^2 = \frac{2^4}{\pi^3} \frac{1}{(2n+1)^2} \quad \rightarrow \quad \varepsilon_n \sim n^{-2}$$

(Ex. 2-dimensional cone  $\varepsilon_n \sim n^{-3}$ )



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