Radiative corrections to Higgs decays in various extended Higgs models

[Nucl. Phys B949 (2019) 114791] [1910.12769] [Phys.Lett. B783 (2018) 140-149]

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Osaka U. 2020/1/21

Outline

Introduction

- Motivation
- H-COUP program
- Renormalization
 - Renormalizations of THDMs
 - Gauge dependence for scalar mixings
- Calculation of Higgs decays at NLO
 - Numerical results for Higgs branching ratios



Motivation

Property of the Higgs boson has been measured at the LHC.

- Measurements of mass, *hVV* couplings, *hff* couplings, etc.
- Current measurements are consistent with predictions of the SM.
- The structure of Higgs sector remains unknown.
 - SM Higgs sector :
 - But, there is still a possibility of extended Higgs sectors

Number and multiplet?	Symmetry?
$\Phi + S$ (Singlet)	Discrete symmetry
$\Phi_1 + \Phi_2$ (Doublet)	Custodial symmetry
$\Phi + \Delta$ (Triplet)	etc.

Relation between BSM phenomena and extended Higgs sectors

→ Testing extended Higgs sectors is essential for exploring NP.

Our approach

Our approaches to the determination of the shape of the Higgs sector is following:



→ We studied on radiative corrections to branching ratios in 6 different extended Higgs models.

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Setup

We treat 6 simple extended Higgs models.

• Higgs singlet models (HSM) The potential has shift invariance $\rightarrow \langle S \rangle = 0$ [$S \rightarrow S + v'_{s}$]

 $V(\Phi,S) = m_{\Phi}^{2} |\Phi|^{2} + \lambda |\Phi|^{4} + \mu_{\Phi S} |\Phi|^{2}S + \lambda_{\Phi S} |\Phi|^{2}S^{2} + t_{S}S + m_{S}^{2}S^{2} + \mu_{S}S^{3} + \lambda_{S}S^{4}$

Physical state : h, H Free parameter : m_H , $\cos \alpha$, m_s^2 , μ_S , λ_S SM-like Higgs \bigwedge CP -even Higgs

• Two Higgs doublet models (THDMs) [softly broken Z₂ symmetry] \rightarrow 4types of Yukawa int. $V = m_1^2 |\Phi_1|^2 + m_2^2 |\Phi_2|^2 - m_2^2 (\Phi_1^{\dagger} \Phi_2 + h.c.)$

$$+\frac{1}{2}\lambda_{1}|\Phi_{1}|^{4} + \frac{1}{2}\lambda_{2}|\Phi_{2}|^{4} + \lambda_{3}|\Phi_{1}|^{2}|\Phi_{2}|^{2} + \lambda_{4}|\Phi_{1}^{\dagger}\Phi_{2}|^{2} + \frac{1}{2}\lambda_{5}[(\Phi_{1}^{\dagger}\Phi_{2})^{2} + \text{h.c.}]$$

Physical state : h, H, A, H^{\pm} Free parameter : $m_H, m_A, m_{H^{\pm}}, s_{\beta-\alpha}, t_{\beta}, M^2(=m_3^2/(s_\beta c_\beta))$

• Inert doublet model (IDM) [exact Z₂ symmetry] $V_{IDM} = V_{THDM} (m_3^2 \rightarrow 0, < \Phi_2 > \rightarrow 0)$ Dark matte candidate Physical state : $h_{,}H_{,}A_{,}H^{\pm}$ Free parameter : $m_{H}, m_{A}, m_{H^{\pm}}, \lambda_{2}, m_{2}$

Higgs couplings

 $\kappa_X = \frac{g(hXX)^{EX.}}{g(hXX)^{SM}}$

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$$\mathsf{HSM}: \quad \kappa_V = \kappa_f = \cos \alpha$$

THDMs:
$$\kappa_V = \sin(\beta - \alpha)$$
, $\kappa_f = \sin(\beta - \alpha) + \xi_f \cos(\beta - \alpha)$

	ξu	ξ_d	٤e
Type-I	$\cot \beta$	$\cot \beta$	$\cot \beta$
Type-II	$\cot \beta$	$-\tan\beta$	$-\tan\beta$
Type-X	$\cot \beta$	$\cot \beta$	$-\tan\beta$
Type-Y	$\cot \beta$	$-\tan\beta$	$\cot \beta$

IDM:
$$\kappa_V = \kappa_f = 1$$

7/30 Model discrimination by couplings



$$\kappa_f = \sin(\beta - \alpha) - \xi_f \cos(\beta - \alpha)$$

	ξu	ξd	ξe
Type-I	$\cot \beta$	$\cot \beta$	$\cot \beta$
Type-II	$\cot \beta$	$-\tan\beta$	$-\tan\beta$
Type-X	$\cot \beta$	$\cot \beta$	$-\tan\beta$
Type-Y	$\cot \beta$	$-\tan\beta$	$\cot \beta$

[Kanemura, Tsumura, Yagyu, Yokoya, PRD90 (2014) 075001]

Each extended Higgs model can give different pattern of deviations

Nondecoupling effects

In the alignment limit, the heavy Higgs masses can be commonly expressed as:

$$m_{\Phi}^2 \simeq M^2 + \lambda_i v^2$$
 ($\Phi = H, A, H^{\pm}$) $M^2 = \begin{cases} 2m_s & (\Pi SM) \\ m_3^2/s_\beta c_\beta & (THDMs) \\ \mu_2^2 & (IDM) \end{cases}$

There are two cases for large m_{Φ}^2 :

(1)
$$M^2 \gg \lambda_i v^2 \longrightarrow m_{\Phi}^2 \simeq M^2$$

Loop contributions of Φ decouple, obeying decoupling theorem.

[T. Appelquist, J. Carazzone, PRD 11 (1975) 2856]

 $\int \gamma_{m}$

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$$\kappa_X - 1 \simeq -\frac{1}{16\pi^2} \frac{1}{6} \sum_{\Phi} \frac{1}{m_{\Phi}^2} + \dots$$

(2) $M^2 \ll \lambda_i v^2 \longrightarrow m_{\Phi}^2 \simeq \lambda_i v^2$

Nondecoupling effects can be obtained.

$$\kappa_X - 1 \simeq -\frac{1}{16\pi^2} \frac{1}{6} \sum_{\Phi} \frac{m_{\Phi}^2}{v^2} + \dots$$

Nondecoupling effects

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[T. Appelquist, J. Carazzone, PRD 11 (1975) 2856]

 $\int 2m$

$$\kappa_X - 1 \simeq -\frac{1}{16\pi^2} \frac{1}{6} \sum_{\Phi} \frac{1}{m_{\Phi}^2} + \dots$$

(2) $M^2 \ll \lambda_i v^2 \longrightarrow m_{\Phi}^2 \simeq \lambda_i v^2$

Nondecoupling effects can be obtained.

 $\kappa_{X} - 1 \simeq -\frac{1}{16\pi^{2}} \frac{1}{6} \sum_{\Phi} \frac{m_{\Phi}^{2}}{v^{2}} \right\} \quad \text{In the case of THDMs, maximally} \\ \sim 2.5\% \text{ for } hVV \text{ [Kanemura, Okada, Senaha, Yuan, PRD70,115002]} \\ \sim 5\% \quad \text{for } hff \quad \text{[Kanemura, Kikuchi, Yagyu, PLB731, 27]}$

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Measurements accuracy of the Higgs couplings (prospect)



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• Sensitivity of most of couplings are improved by the ILC.

• Loop effects of extra Higgs is comparable with future sensitivities.

→ Evaluation of Higher order corrections is necessary.

Couplings → branching ratios

While the experimental data of Higgs couplings are not directly compared with predictions of models, the branching ratios can be done :

• Higgs couplings

Public tools

Here is a list of public tools to compute the Higgs decays for extended Higgs models.

(ewN)2HDECAY : [M. Krause, M. Mühlleitner, M. Spira, 1810.00768][M. Krause, M. Mühlleitner, 1904.02103]

- Model: 2HDMs, N2HDMs
- Calculations of two-body-Higgs decays with full 1-loop EW and state-of-the-art QCD corrections in 17 renormalization scheme for mixing parameters
- Prophecy4f: [L. Altenkamp, S. Dittmaier, H. Rzehak, JHEP 1803 (2018) 110]
 - Model: SM,2HDMs, HSM
 - · h \rightarrow WW/ZZ \rightarrow 4 fermions with NLO QCD and NLO EW corrections
- RECOLA2 : [A. Denner, J. N. Lang, S. Uccirati, CPC 224(2018)346]
 - Model: 2HDMs, HSM
 - Calculation to NLO amplitude for any process
- **2HDMC**: [D. Eriksson, J. Rathsman, O. Stal CPC. 181 (2010) 189]
 - Model: 2HDMs
 - Calculations of decays of Higgs bosons with NLO QCD
- SHDECAY : [R. Costa, M. Mühlleitner, M. Sampaio, R. Santos, JHEP 06 (2016) 034]
 - Model: HSM (real and complex)
 - Calculations of decays of Higgs bosons with NLO QCD
- H-COUP : [Kanemura, Kikuchi, KS, Yagyu, CPC 233 (2018) 134]

[Kanemura, Kikuchi, Mawatari, KS, Yagyu, 1910.12769]

H-COUP1.0(13.10.18~)

Model:

- Singlet extension of the SM
- 4 types of 2HDMs
- Inert doublet model

Evaluation:

- Higgs vertex functions (at 1-loop)

$$\begin{split} \hat{\Gamma}_{hVV}^{\mu\nu} &= \hat{\Gamma}_{hVV}^{1} g^{\mu\nu} + \hat{\Gamma}_{hVV}^{2} \frac{p_{1}^{\mu} p_{2}^{\nu}}{m_{V}^{2}} + i \hat{\Gamma}_{hVV}^{3} \epsilon^{\mu\nu\rho\sigma} \frac{p_{1\rho} p_{2\sigma}}{m_{V}^{2}}, \\ \hat{\Gamma}_{hff} &= \hat{\Gamma}_{hff}^{S} + \gamma_{5} \hat{\Gamma}_{hff}^{P} + p_{1} \hat{\Gamma}_{hff}^{V1} + p_{2} \hat{\Gamma}_{hff}^{V2} \\ &+ p_{1} \gamma_{5} \hat{\Gamma}_{hff}^{A1} + p_{2} \gamma_{5} \hat{\Gamma}_{hff}^{A2} + p_{1} p_{2} \hat{\Gamma}_{hff}^{T} + p_{1} p_{2} \gamma_{5} \hat{\Gamma}_{hff}^{PT} \end{split}$$

H-COUP1.0 (13.10.18~) Model:

- Singlet extension of the SM
- 4 types of 2HDMs
- Inert doublet model
- **Evaluation:**
 - Higgs vertex functions (at 1-loop)

Feature of the H-COUP:

H-COUP2.0(03.09.19~)

Model:

Same as ver. 1.0

Evaluation:

- Higgs vertex functions (at 1-loop)
- New Higgs branching ratios (with NLO EW and NNLO QCD)
- All decay processes for the Higgs boson with Higher order corrections can be evaluated in the same renormalization scheme for various models.
- Form factors of renormalized Higgs bosons can be evaluated.

In this talk

By using H-COUP, We have evaluated Higgs BRs with full 1loop corrections in 6 different models.

The predictions can be directory compared with exp. data

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Open questions:

- how is decoupling property of additional Higgs bosons for BRs?
- What is pattern of deviations from the SM for BRs for each model?
- We show size of additional Higgs boson loop cont. for BRs.
- We discuss if various extended Higgs models are discriminated by using precise measurements of Higgs BRs.

Introduction Motivation H-COUP program

Renormalization

- Renormalizations of THDMs
- Gauge dependence for scalar mixings

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Summary

16/30 Renormalization of the Higgs sector

We have used improved on-shell renormalization scheme in calculations for EW corrections for Higgs decay rates. [S. Kanemura, M. Kikuchi, KS, K. Yagyu, PRD96,035014]

Ex.) Higgs potential in the THDMs

 $\begin{pmatrix} w_i^+ \end{pmatrix}$

1. Count number of parameters and fields in Lagrangian:

• Parameters in Higgs potential : 8

$$v, m_h, m_H, m_A, m_{H^{\pm}}, M^2, \alpha, \beta$$

• Tadpoles : 2

 T_h , T_H

• Fields of Higgs sector : 8

h, H^{\pm} , H, A, G^{0} , G^{\pm}

- 2. Shift parameters and fields to introduce counter terms as same number these:
 - Parameter shift : $(\varphi = h, H^{\pm}, H, A)$

$$\begin{split} m_{\varphi} &\to m_{\varphi} + \delta m_{\varphi}, \, M \to M + \delta M, \, \alpha \to \delta \alpha, \, \beta \to \delta \beta, \\ T_h &\to T_h + \delta T_h, \, T_h \to T_H + \delta T_H \end{split}$$

• Field shift :

$$\begin{pmatrix} \varphi_1 \\ \varphi_2 \end{pmatrix} \rightarrow \begin{pmatrix} 1 + \delta \frac{1}{2} Z_{\varphi_1} & \delta C_{\varphi_1 \varphi_2} + \delta \theta \\ \delta C_{\varphi_1 \varphi_2} - \delta \theta & 1 + \frac{1}{2} \delta Z_{\varphi_2} \end{pmatrix} \begin{pmatrix} \varphi_1 \\ \varphi_2 \end{pmatrix}, \qquad (\varphi_1, \varphi_2, \theta) = (H, h, \alpha), (G^0, A, \beta) \text{ or } (G^{\pm}, H^{\pm}, \beta)$$

→ We get 19 counter terms :

 $\delta v, \delta m_h^2, \delta m_H^2, \delta m_A^2, \delta m_{H^{\pm}}^2, \delta M^2, \delta \alpha, \delta \beta, \delta T_h, \delta T_H$

 δZ_h , δZ_H , δZ_A , $\delta Z_{H^{\pm}}$, δZ_{G^0} , $\delta Z_{G^{\pm}}$, δC_{Hh} , δC_{GA} , $\delta C_{G^+H^-}$

3. Set renormalization conditions: Renormalization of tadpoles

• Standard scheme [W.F.L. Hollik, Fortschr. Phys. 38 (1990) 165.]

$$\frac{T_{h,H}^{1\text{PI}}}{(1\text{PI})} + \frac{\delta T_{h,H}}{(1\text{PI})} = 0$$

- Tadpole contributions don't appear in self-energy for vector boson and fermion.

$$\hat{\Pi}_{ij} = - 1 PI + - 2 PI$$

- Counter terms for physical parameters (e.g., mass) are gauge-dependent. Note: This is not a problem as longs as physical quantities are gauge independent.
- (Alternative) tadpole scheme [J. Fleischer and F. Jegerlehner, PRD23, 2001 (1981)]
 - In addition to above conditions, Shift of VEV is performed: $v_i \rightarrow v_i + \Delta v_i$, (i = 1,2)
 - \rightarrow Tadpole contributions appear in self-energy for all fields: $\hat{\Pi}_{ii}^{\text{Tad}} = \hat{\Pi}_{ii} + \hat{\Pi}_{ii}$
 - \rightarrow Gauge invariance for CT is restored.

We showed that $\Gamma_{h \to XX}^{\text{Tad}} = \Gamma_{h \to XX}^{\text{Stand.}}$ [Kanemura, Kikuchi, KS, Yagyu, PRD96,035014]

 \rightarrow We use the standard scheme.

Renormalization of mass, WFR and mixing angles

$$\begin{split} \delta m_{\phi} : \quad & \hat{\Pi}_{\varphi\varphi}(m_{\varphi}^2) = 0 \quad (\Phi = h, H, A, H^{\pm}) \\ \delta Z_{\phi} : \quad & \frac{d}{dp^2} \hat{\Pi}_{\varphi\varphi}(p^2) \big|_{p^2 = m_{\varphi}^2} = 0 \quad (\Phi = h, H, A, H^{\pm}, G^{\pm}, G^0) \end{split}$$

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 $\delta \alpha, \delta \delta, \delta C_{\phi_1 \phi_2}: \hat{\Pi}_{\phi_1 \phi_2}(m_{\phi_1}^2) = \hat{\Pi}_{\phi_1 \phi_2}(m_{\phi_2}^2) = 0 \quad (\{\Phi_1, \Phi_2\} = \{H, h\}, \{G^0, A\}, \{H^{\pm}, G^{\pm}\})$

Renormalization of another quantities

 δv : This counter term is determined in gauge sector.

 δM : It is determined such as UV divergence in *hhh* vertex becomes zero.

In this way, with above renormalization conditions, all counter terms are determined.

 \rightarrow any renormalized quantities are UV finite .

- Gauge dependence appears in the renormalization of the scalar mixing angles (even if in tadpole scheme). [Yamada, PRD64(2001)036008]
 - \rightarrow Physical quantities also become gauge dependent .

20/30 Gauge dependence on mixing angles

We consider unrenormalized mass matrix at the 1-loop in R_{ξ} gauge :

$$M_{Hh} = \begin{pmatrix} m_h^2 + \Pi_{hh}^{\text{Tad}} & \Pi_{Hh}^{\text{Tad}} \\ \Pi_{Hh}^{\text{Tad}} & m_H^2 + \Pi_{HH}^{\text{Tad}} \end{pmatrix}$$
$$\partial_{\xi} M_{Hh} = \begin{pmatrix} (p^2 - m_h^2) \tilde{\Pi}_{hh}^{\text{Tad}} & (2p^2 - m_h^2 - m_H^2) \tilde{\Pi}_{Hh}^{\text{Tad}} \\ (2p^2 - m_h^2 - m_H^2) \tilde{\Pi}_{Hh}^{\text{Tad}} & (p^2 - m_H^2) \tilde{\Pi}_{HH}^{\text{Tad}} \end{pmatrix}$$

Diagonal elements : $\hat{\Pi}_{hh}^{\text{Tad}}(m_h^2) = \hat{\Pi}_{HH}^{\text{Tad}}(m_H^2) = 0$

 $\rightarrow \delta m_h^2, \, \delta m_H^2$ are gauge independent.

Off-diagonal elements :

s:
$$\hat{\Pi}_{Hh}^{\text{Tad}}(m_h^2) = \hat{\Pi}_{Hh}^{\text{Tad}}(m_H^2) = 0$$

 $\rightarrow \delta \alpha, \delta \beta$ are gauge dependent.

→ amplitudes for Higgs process with $\delta \alpha$, $\delta \beta$ are also gauge dependent [M. Krause, R. Lorenz, M. Muhlleitner, R. Santos, H. Ziesche, JHEP 09 (2016) 143]

Pinch technique

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In order to remove the gauge dependence in $\delta \alpha$, $\delta \beta$ we utilize pinch technique [J. Papavassiliou, PRD50, 5958]

Basic idea:
$$(in \ \delta \alpha, \ \delta \beta)$$

 $\Pi_{Hh}^{Tad} \rightarrow \Pi_{Hh}^{Tad} + \Pi_{Hh}^{PT} \longrightarrow \partial_{\xi} \delta \alpha = 0, \ \partial_{\xi} \delta \beta = 0$
Pinch terms

Pinch terms can be extracted as follows: Considering S-matrix of 2 →2 fermions scattering

$$T = \left| \begin{array}{c} T \\ T \\ \end{array} \right| + \left| \begin{array}{c} T \\ \end{array} \right| + \left| \left| \begin{array}{c} T \\ \end{array} \right| + \left| \begin{array}{c} T \\ \end{array} \right| + \left| \left| \left| \end{array} \right| + \left| \left| T \\ + \left| \left| T \\ + \left| T \\ +$$

In this way, we can get gauge independent mixing counter terms.

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Summary

22/30 One-loop calculation of Higgs decay rates

Virtual corrections for $h \rightarrow ff$:

CP-conservation

h

Slavnov-Taylor identity [K. E. Williams, H. Rzehak, G. Weiglein, Eur.Phys.J. C71 (2011) 1669]

 $\Pi_{hG} + im_Z \Pi_{hZ} = 0$

Virtual corrections for $h \rightarrow VV^* \rightarrow Vf\bar{f}$: (V=Z,W)

For renormalization of WFR for the weak gauge boson, we do not impose that the residue is a unity. It is expressed as in terms of WFR for γ and γ-Z mixing.
[W.F.L. Hollik, Fortschr. Phys. 38 (1990) 165.]

IR structure between $h \rightarrow ZZ^*$ and $h \rightarrow WW^*$ are different.

 $h \rightarrow ZZ^*$: Only Vff vertex contains photon loop diagrams.

 $h \rightarrow WW^*$: All diagrams contain photon loop diagrams.

^{24/30} IR divergence for h→WW*

In order to get IR finate results for h→WW*, real photon emissions are needed. For the evaluation we make use of phase space slicing method. [B. Harris, J. Owens, ,PRD65(2002)094032]

$$\Gamma(h \to Wff'\gamma) = \Gamma(h \to Wff'\gamma)[\lambda, m_f, m_{f'}, \Delta E]^S + \Gamma(h \to Wff'\gamma)[m_f, m_{f'}, \Delta E]^H$$

 ΔE : cut off parameter, λ : regulator of soft div. $m_{f}, m_{f'}$: regulator of collinear div.

Adding contributions of the real photon to that of virtual photon, soft divergence and collinear divergence are cancelled.

$$\Gamma(h \rightarrow Wff') + \Gamma(h \rightarrow Wff'\gamma) = (\text{IR finite})$$

 \rightarrow We numerically checked the cancellation.

25/30 **Higgs branching ratios at the 1-loop**

Cause of deviations from SM : ① Mixing, loop effect of additional Higgs 2 Correlation of each mode

26/30 Higgs branching ratios at the 1-loop

In order to more clearly see the magnitude of additional Higgs bosons loop contributions, we evaluate the deviations in the branching ratios in 2HDMs.

 $m_{\Phi} \gg v$: Additional Higgs loop contributions decouple.

 $m_{\Phi} \sim v$: Non-decoupling effect can be appeared at few %.

Discrimination of the models

We discuss whether 6 different models are discriminated by precise measurements of Higgs branching ratios.

	1σ	2σ	
Βγγ	13%	26%	
B ^{zz}	6.7%	13.4%	
B _{MM}	1.9%	3.8%	
Βττ	1.4%	2.8%	
Bpp	0.89%	1.78%	
B ^{μμ}	27%	54%	

We consider situations that B^{ww} are measured with few % accuracy at the ILC.

[1710 07621]

\rightarrow We studied three cases:

①: $\Delta \mu_{WW} = 0 \pm 4\%$ ②: $\Delta \mu_{WW} = 5 \pm 4\%$ ③: $\Delta \mu_{WW} = -5 \pm 4\%$

Case ①: $\Delta \mu_{WW} = 0 \pm 4\%$

 $\Delta \mu_{XX} = \frac{\text{BR}(h \to XX)_{NP}}{\text{BR}(h \to XX)_{SM}} - 1$

- Plot of color : Predictions of each model
- Brightness of color : Value of mφ
 - Lighter colors: $m_{\Phi} < 600 \text{GeV}$
 - Darker colors: $m_{\Phi} > 600 \text{GeV}$

Lower bound from $b \rightarrow s\gamma$ (for Type-II,Y)

HL-LHC(2 σ): [ATLAS, CMS,1902.00134]

ILC(2 σ): [T. Barlow et al. 1710.07621] [Kanemura, Kikuchi, Mawatari, KS, Yagyu]

If $|\Delta \mu_{\tau\tau}| \gtrsim 5\%$, 4 types of THDMs can be separated.

- In both case, HSM and IDM are already excluded.
- In case2 models predictions of 2HDMs are completely separated.
- In case③, if m_{Φ} >600 GeV, we can distinguish all models

- We evaluated Higgs branching ratio with full 1-loop corrections in various extended Higgs models by H-COUP.
- the branching ratios will be precisely measured in the future collider experiments such as the HL-LHC and the ILC.

We investigated the deviations from the SM in the 3 cases:

	Constraint for $\Delta \mu_{WW}$	Discriminations of models
1	$\Delta\mu_{WW} = 0 \pm 4~\%$	Possible (if $ \Delta\mu_{\tau\tau} \gtrsim 5\%$)
\bigcirc	$\Delta\mu_{WW} = 5 \pm 4 \%$	Possible
3	$\Delta\mu_{WW} = -5 \pm 4\%$	Possible (if m_{Φ} >600 GeV)

→In any case, there are situations all models can be discriminated.