

Phenomenological aspects of a light pseudoscalar in Type-X 2HDM

PLB 774 (2017), PRD 98 (2018)
PLB 802 (2020), JHEP (2020)

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BSM Models often involve extended Higgs sector :

- $U(1)_{B-L}$, Some DM models : SM Higgs + Scalar singlet
- MSSM : SM Higgs + Scalar doublet (**2HDM**)
- LR model, type-II seesaw : SM Higgs + Scalar triplet

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Motivations for 2HDM:

- Explaining baryon asymmetry of the Universe
- PQ symmetry
- Radiative neutrino mass generation, Dark matter etc.
- Muon anomalous magnetic moment.

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Type-X 2HDM

- Can explain Muon $g - 2$ with a light pseudoscalar & large $\tan \beta$
- I will discuss some of the phenomenological aspects of a light pseudoscalar in Type-X 2HDM.

The Model : 2HDM Type X

The 2HDM scalar potential

The scalar potential

$$\begin{aligned}
 V_{2\text{HDM}} = & m_{11}^2 \Phi_1^\dagger \Phi_1 + m_{22}^2 \Phi_2^\dagger \Phi_2 - [m_{12}^2 \Phi_1^\dagger \Phi_2 + \text{h.c.}] \\
 & + \frac{1}{2} \lambda_1 (\Phi_1^\dagger \Phi_1)^2 + \frac{1}{2} \lambda_2 (\Phi_2^\dagger \Phi_2)^2 + \lambda_3 (\Phi_1^\dagger \Phi_1) (\Phi_2^\dagger \Phi_2) \\
 & + \lambda_4 (\Phi_1^\dagger \Phi_2) (\Phi_2^\dagger \Phi_1) + \frac{1}{2} \lambda_5 \{ (\Phi_1^\dagger \Phi_2)^2 + (\Phi_2^\dagger \Phi_1)^2 \}
 \end{aligned}$$

- The doublets contain 4 real fields each \Rightarrow 8 total fields.

$$\Phi_i = \begin{pmatrix} \phi_i^\pm \\ \frac{v_i}{\sqrt{2}} + \phi_i^r + i\phi_i^i \end{pmatrix}$$

- After SSB we have 5 physical scalar fields : H^\pm, h, H, A .

The scalars of 2HDM

Masses of the scalars and quartic couplings

$$\lambda_1 = \frac{m_H^2 c_\alpha^2 + m_h^2 s_\alpha^2 - m_{12}^2 \tan \beta}{v^2 c_\beta^2},$$

$$\lambda_2 = \frac{m_H^2 s_\alpha^2 + m_h^2 c_\alpha^2 - m_{12}^2 \cot \beta}{v^2 s_\beta^2},$$

$$\lambda_3 = \frac{(m_H^2 - m_h^2) c_\alpha s_\alpha + 2m_{H^\pm}^2 s_\beta c_\beta - m_{12}^2}{v^2 s_\beta c_\beta},$$

$$\lambda_4 = \frac{(m_A^2 - 2m_{H^\pm}^2) s_\beta c_\beta + m_{12}^2}{v^2 s_\beta c_\beta}, \quad \lambda_5 = \frac{m_{12}^2 - m_A^2 s_\beta c_\beta}{v^2 s_\beta c_\beta}.$$

$$m_H^2 \approx m_A^2 + \lambda_5 v^2, \quad m_{H^\pm}^2 \approx m_A^2 + \frac{1}{2}(\lambda_5 - \lambda_4) v^2.$$

If $\lambda_5 \approx -\lambda_4$ we will have $m_A \ll m_H \simeq m_{H^\pm}$

Since we have two doublets the general Yukawa structure will be :

$$\begin{aligned}\mathcal{L} &= y_{ij}^1 \bar{\psi}_i \psi_j \Phi_1 + y_{ij}^2 \bar{\psi}_i \psi_j \Phi_2 \\ \Rightarrow m_{ij}^f &= y_{ij}^1 \frac{v_1}{\sqrt{2}} + y_{ij}^2 \frac{v_2}{\sqrt{2}}\end{aligned}$$

In general both y_{ij}^1 and y_{ij}^2 will not be simultaneously diagonalizable which leads to couplings like $(\bar{d} s \phi)$. **FCNC**

- Experimental limit on FCNC scalar mass ~ 10 TeV.
- So we demand : No tree level FCNC.

Paschos-Glashow-Weinberg Theorem

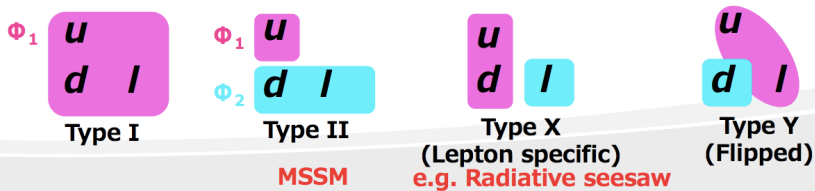
A necessary and sufficient condition for the absence of FCNC at tree level is that all fermions of a given charge and helicity transform according to the same irreducible representation of SU(2), correspond to the same eigenvalue of T_3 and that a basis exists in which they receive their contributions in the mass matrix from a single source.

or

RH fields with same quantum number should couple to only one type of Higgs.

Paschos-Glashow-Weinberg Theorem

RH fields with same quantum number should couple to only one type of Higgs.



Model	u_R^i	d_R^i	e_R^i
Type I	$\bar{\Phi}_2$	$\bar{\Phi}_2$	$\bar{\Phi}_2$
Type II	$\bar{\Phi}_2$	$\bar{\Phi}_1$	$\bar{\Phi}_1$
Lepton-specific	$\bar{\Phi}_2$	$\bar{\Phi}_2$	$\bar{\Phi}_1$
Flipped	$\bar{\Phi}_2$	$\bar{\Phi}_1$	$\bar{\Phi}_2$

$$\mathcal{L}_Y = -Y^u \bar{Q}_L \tilde{\Phi}_2 u_R + Y^d \bar{Q}_L \Phi_2 d_R + Y^e \bar{\ell}_L \Phi_1 e_R + h.c.$$

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After symmetry breaking in terms of physical scalars the Yukawa couplings are

$$\begin{aligned} \mathcal{L}_{\text{Yukawa}}^{\text{Physical}} = & - \sum_{f=u,d,\ell} \frac{m_f}{v} \left(\xi_h^f \bar{f} h f + \xi_H^f \bar{f} H f - i \xi_A^f \bar{f} \gamma_5 A f \right) \\ & - \left\{ \frac{\sqrt{2} V_{ud}}{v} \bar{u} \left(m_u \xi_A^u P_L + m_d \xi_A^d P_R \right) H^+ d \right. \\ & \left. + \frac{\sqrt{2} m_l}{v} \xi_A^l \bar{\nu}_L H^+ l_R + h.c. \right\}, \end{aligned}$$

ξ_h^u	ξ_h^d	ξ_h^ℓ	ξ_H^u	ξ_H^d	ξ_H^ℓ	ξ_A^u	ξ_A^d	ξ_A^ℓ
$\frac{C_\alpha}{S_\beta}$	$\frac{C_\alpha}{S_\beta}$	$\frac{-S_\alpha}{C_\beta}$	$\frac{S_\alpha}{S_\beta}$	$\frac{S_\alpha}{S_\beta}$	$\frac{C_\alpha}{C_\beta}$	$\cot \beta$	$-\cot \beta$	$\tan \beta$

Table: The multiplicative factors of Yukawa interactions

- Gauge-Higgs sector :

$$g_{hVV} = \sin(\beta - \alpha)g_{hVV}^{\text{SM}}, \quad g_{HVV} = \cos(\beta - \alpha)g_{hVV}^{\text{SM}}, \quad g_{AVV} = 0,$$

where $V = Z, W^\pm$.

- Relevant vertices

$$hAZ_\mu : \frac{g_Z}{2} \cos(\beta - \alpha)(p + p')_\mu, \quad HAZ_\mu : -\frac{g_Z}{2} \sin(\beta - \alpha)(p + p')_\mu,$$

$$H^\pm AW_\mu^\mp : \frac{g}{2}(p + p')_\mu$$

where p_μ (p'_μ) : outgoing four-momenta of the first (second) scalars.

Interesting parameter space in 2HDM-X : Muon $(g - 2)$ and other constraints

2HDM-X : Muon ($g - 2$) and other constraints

- **Muon $g - 2$**
- Higgs signal strength
- $B_s \rightarrow \mu^+ \mu^-$ or $B_s \rightarrow X_s \gamma$
- EWPD
- Lepton universality

2HDM-X : Muon ($g - 2$) and other constraints

- $a_\mu^{\text{exp}} = (11659209.1 \pm 6.3) \times 10^{-10}$
- $a_\mu^{\text{th}} = a_\mu^{\text{QED}} + a_\mu^{\text{EW}} + a_\mu^{\text{had,VP}} + a_\mu^{\text{had,LbL}}$
- $\{(11658471.9 \pm 0.007) + (15.36 \pm 0.1)\} \times 10^{-10}$
- $\{(684.68 \pm 2.42) + (9.8 \pm 2.6)\} \times 10^{-10}$
- $\Delta a_\mu = (27.06 \pm 7.26) \times 10^{-10}$ Ref: 1802.02995

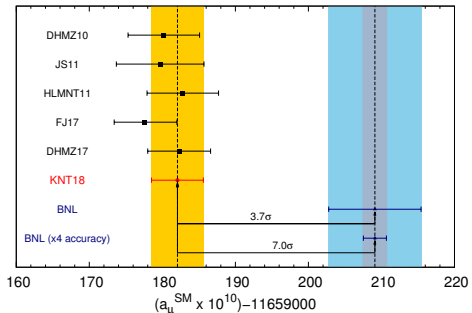
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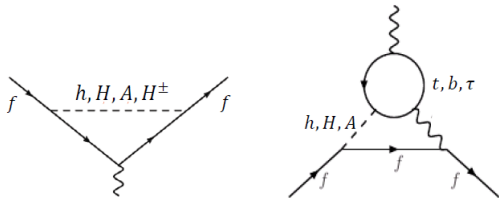
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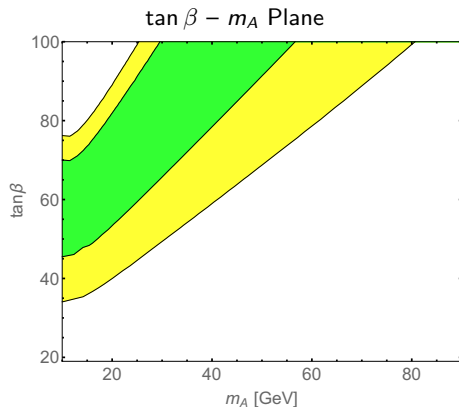
Muon $g - 2$ in 2HDM

- **Muon $g - 2$**
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- 1loop: contribution from h, H are positive and **A contributes negatively.**
- $m_H < 5 \text{ GeV}$ to explain experimental data.
- Barr-Zee 2-Loop contribution with τ loop and low m_A comes to rescue.

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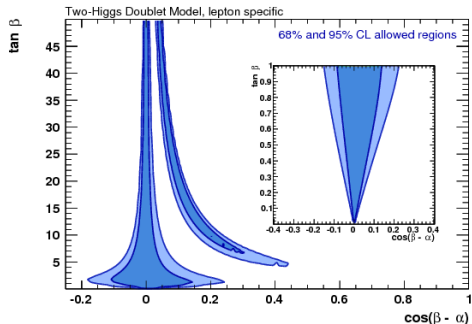


JHEP 11 (2014) 058, JHEP 05 (2015) 039, JHEP 07 (2015) 064,
 JHEP 11 (2015) 099, JHEP 02 (2016) 097, JHEP 01 (2017) 007

and many more

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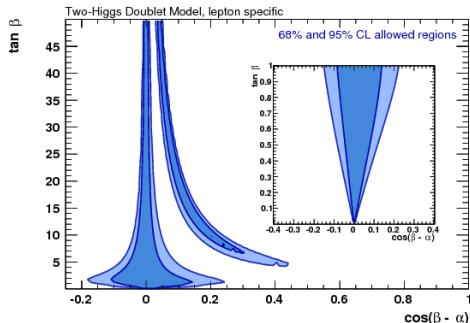
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GFitter : 1803.01853

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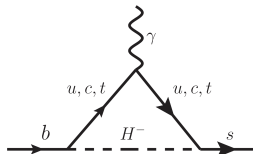
Wrong Sign Limit

$$hll \text{ coupling : } \frac{-s_\alpha}{c_\beta} \simeq \sin(\beta - \alpha) - \tan \beta \cos(\beta - \alpha)$$

So, when $\tan \beta \cos(\beta - \alpha) \sim 2$ Higgs coupling to leptons flip sign.

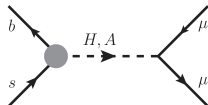
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$$\frac{m_t}{t_\beta} P_L - \frac{m_b}{t_\beta} P_R \quad (X, I)$$

$$\frac{m_t}{t_\beta} P_L + m_b t_\beta P_R \quad (II, Y)$$

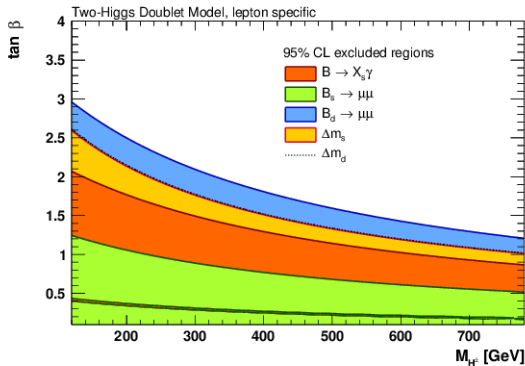
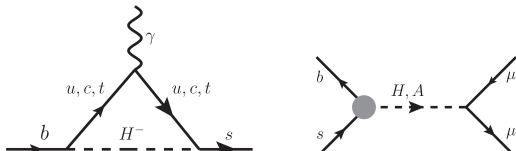


For type X : ~ 1
 For type II : $(\tan \beta)^2$

- 2HDM-II : $b \rightarrow s \gamma$: $m_{H^\pm} > 580 \text{ GeV}$. BELLE, 1608.02344
- $BR(B_s \rightarrow \mu\mu) = (3.0 \pm 0.6_{-0.2}^{+0.3}) \times 10^{-9}$ LHCb, 1703.05747
- Limit on type-II 2HDM : $\tan \beta < 7$ for $m_A < 70 \text{ GeV}$

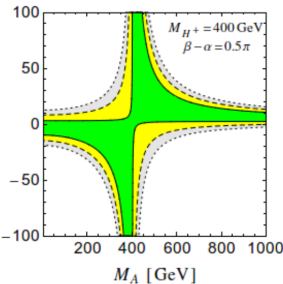
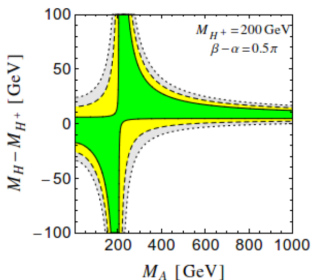
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- M_{H^\pm} should be very close to either M_H or M_A .

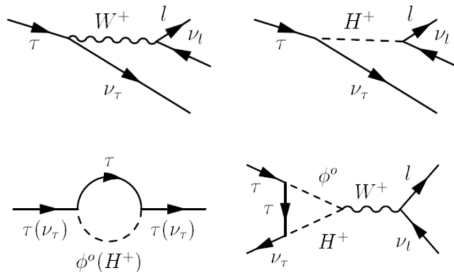
JHEP 11 (2014) 058

GFitter : 1803.01853

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τ Decay



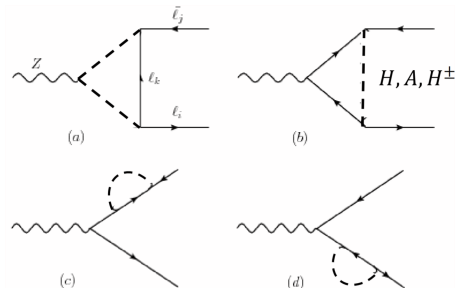
Limits coming from :

$$\frac{\Gamma(\tau \rightarrow \mu \nu \nu)}{\Gamma(\tau \rightarrow e \nu \nu)}, \quad \frac{\Gamma(\tau \rightarrow e \nu \nu)}{\Gamma(\mu \rightarrow e \nu \nu)} \text{ etc}$$

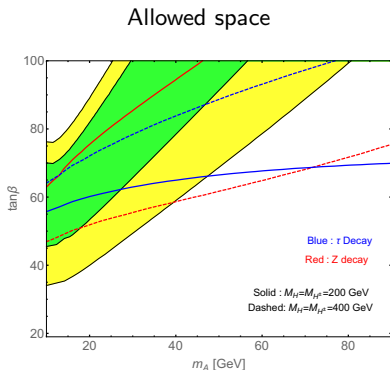
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Z Decay



- Muon $g - 2$
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- EWPD
- **Lepton universality**



Z Phys. C 51 (1991) 695

JHEP 1507 (2015) 064

JHEP 07 (2016) 110

2HDMX at LHC

- No direct production of the new scalars since the coupling to quarks are suppressed.
- All the signals will be tau rich.
- Different multi tau signal has been studied

$$pp \rightarrow W^\pm \rightarrow H^\pm H/A \rightarrow (\tau^\pm \nu)(\tau^+ \tau^-)$$

$$pp \rightarrow Z/\gamma \rightarrow HA \rightarrow (\tau^+ \tau^-)(\tau^+ \tau^-)$$

$$pp \rightarrow Z/\gamma \rightarrow H^+ H^- \rightarrow (\tau^+ \nu)(\tau^- \nu)$$

S.Kanemura et.al. (1111.6089), E.J.Chun et.al. (1507.08067)

- However, it is not possible to reconstruct the masses of the scalars from tau only final states.
- Also for light A only tau-rich final state is hard to trigger.
- We proposed to look for 2HDM-X signal at the LHC and reconstruct the light pseudoscalar in $2\mu 2\tau$ final state.
- Also we have shown how to reconstruct the heavy charged/neutral scalars.

Chun,Dwivedi,TM,Mukhopadhyaya PLB 774 (2017)

Chun,Dwivedi,TM,Mukhopadhyaya,Rai PRD 98 (2018) 7

- We can produce a pair of pseudoscalars from Higgs decay.
- Since coupling of A to leptons is proportional to mass of the leptons, A will predominantly decay to a pair of taus leading to 4τ signal.
- As argued, we can't reconstruct mass of A from this final state.
- However a very small portion of A decays to muons with $\text{BR}(A \rightarrow \mu\mu) \simeq 0.35\%$
- This channel can be used to estimate mass of the pseudoscalar.

Signal of a light A : An analysis for the LHC

Parameters	M_A (GeV)	$\tan \beta$	$\cos(\beta - \alpha)$	λ_{hAA}/v
BP1	50	60	0.03	0.02
BP2	60	60	0.03	0.03

$$pp \rightarrow h \rightarrow AA \rightarrow \mu^+ \mu^- \tau^+ \tau^- \rightarrow \mu^+ \mu^- j_\tau j_\tau + MET$$

$$\sigma \sim 0.021 \text{ pb}$$

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Backgrounds:

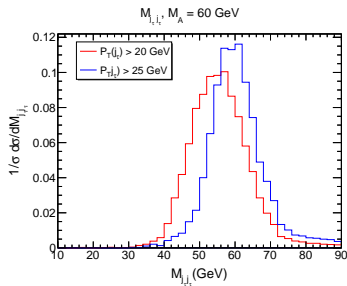
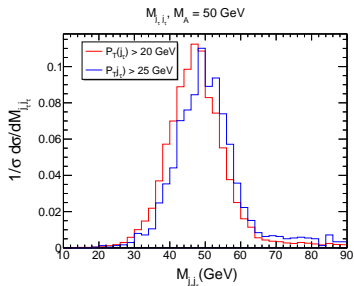
- $pp \rightarrow \mu^+ \mu^- + jets$ $\sigma \sim 2100 \text{ pb}$
- $pp \rightarrow VV + jets (V = Z, W, \gamma^*)$ $\sigma \sim 6.2 \text{ pb}$
- $pp \rightarrow t\bar{t} + jets.$ $\sigma \sim 0.03 \text{ pb}$

Collider signature of light A

- We have a light A (mass < 60 GeV) decaying to two tau which further decays hadronically.
- If minimum p_T for the tau tagged jets is close to $M_A/2$ then the neutrinos can not take large amount of tau momentum.
- In that case invariant mass of tau-jets will peak at parent mass(!!)

Collider signature of light A

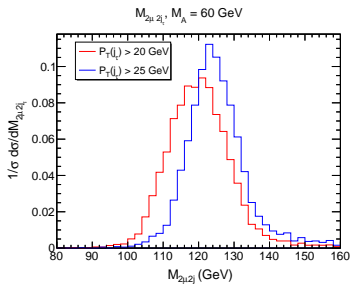
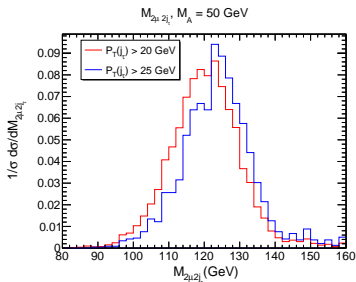
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Chun, Dwivedi, TM, Mukhopadhyaya PLB 774 (2017)

Collider signature of light A

The same argument holds if we construct invariant mass using 2μ and 2τ -tagged jet.

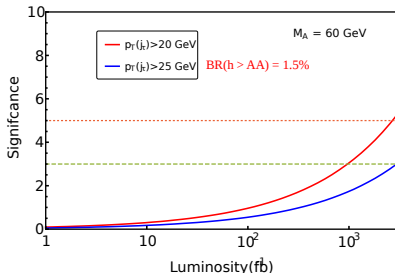
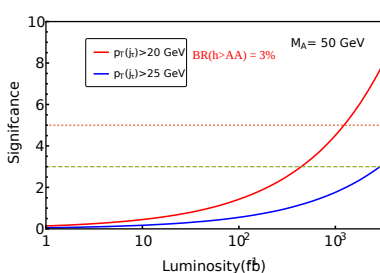


Chun, Dwivedi, TM, Mukhopadhyaya PLB 774 (2017)

Simulation cuts

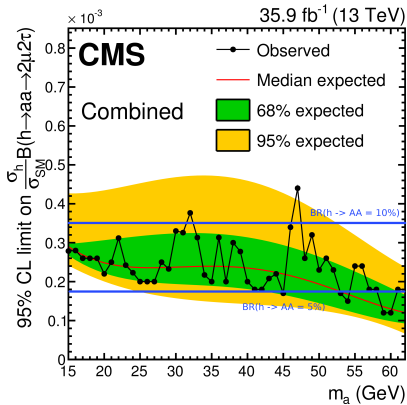
- Signal contains 2 isolated muons and 2 tau-tagged jets.
- Preselection:
 - ▶ $p_T(\mu) > 10$ GeV and $|\eta| < 2.5$.
 - ▶ $p_T(j_\tau) > 20/25$ GeV $|\eta(j_\tau)| < 2.5$.
- The invariant mass of the di-muon system ($M_{\mu\mu}$) satisfies the window: $|M_{\mu\mu} - M_A| < 7.5$ GeV.
- The invariant mass of the two tau-tagged jets ($M_{j_\tau j_\tau}$) satisfies:
 - ▶ for $p_T(j_\tau) > 20$ GeV : $(M_A - 20) < M_{j_\tau j_\tau} < (M_A + 10)$ GeV
 - ▶ for $p_T(j_\tau) > 25$ GeV : $|M_{j_\tau j_\tau} - M_A| < 15$ GeV.
- The invariant mass of two muons and two taujets ($M_{2\mu 2j_\tau}$) lies within the range :
 - ▶ for $p_T(j_\tau) > 20$ GeV : $(M_h - 20) < M_{2\mu 2j_\tau} < (M_h + 10)$ GeV.
 - ▶ for $p_T(j_\tau) > 25$ GeV : $|M_{2\mu 2j_\tau} - M_h| < 15$ GeV.
- Asymmetric cuts for low p_T since the distribution peaks at lower value.

$$\text{Significance} = S = \sqrt{2 \left[(S + B) \ln \left(1 + \frac{S}{B} \right) - S \right]}$$



- Large $p_T(j)$ results in better invariant mass peaks but provides fewer number of events which decreases the discovery prospect
- At 3 ab^{-1} it is possible to rule out $\text{BR}(h \rightarrow aa) < 1\%$.

Chun, Dwivedi, TM, Mukhopadhyaya PLB 774 (2017)



JHEP 11 (2018) 018

Collider searches for H and H^\pm

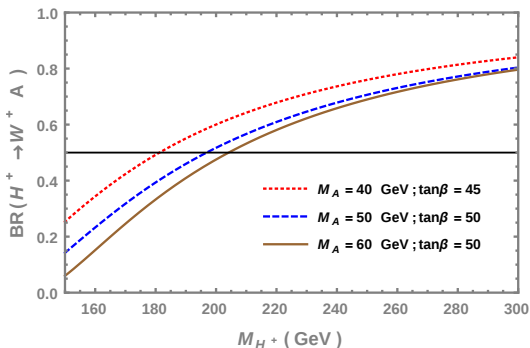
Branching fraction of H^\pm

There are two possible decay modes for the charged Higgs

$$\Gamma(H^\pm \rightarrow W^\pm A) \sim \frac{m_{H^\pm}}{16\pi} \left(\frac{m_{H^\pm}}{v} \right)^2$$

$$\Gamma(H^\pm \rightarrow \tau^+ \nu_\tau) \sim \frac{m_{H^\pm}}{16\pi} \left(\frac{\sqrt{2} m_\tau \tan \beta}{v} \right)^2$$

WA channel dominates when $m_{H^\pm} > \sqrt{2} m_\tau \tan \beta$



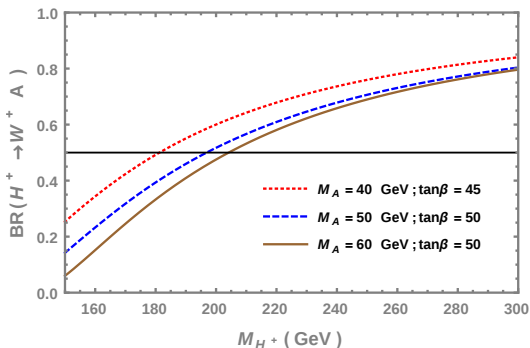
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Same is true for neutral heavy Higgs and $BR(H \rightarrow ZA)$ is substantial.

Collider searches for H and H^\pm

- EWPD forces the heavy scalars to be almost degenerate.
- Signal at LHC

$$p p \rightarrow (H^\pm)A \rightarrow (W^\pm A) \quad A \rightarrow (j j 2\mu) \quad 2\tau$$

- Added contribution from heavy Higgs H

$$p p \rightarrow (H)A \rightarrow (ZA) \quad A \rightarrow (j j 2\mu) \quad 2\tau$$

- Signal : 2 light jets, 2 muon and at least one τ tagged jet
- Benchmark the signal for $m_A = 40, 50$ and 60 GeV. For each, m_{H^\pm} and m_H lies in $150 - 300$ GeV.
- Invariant mass distribution of $j j 2\mu$ system will peak at the parent particle mass.

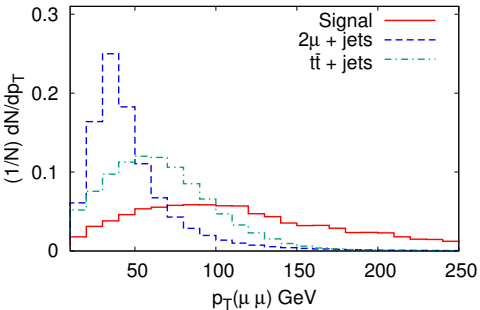
Collider searches for H and H^\pm

- Signal : $2 j + 2 \mu + \geq 1 j_\tau$
- Dominant Backgrounds :
 - ▶ $pp \rightarrow \mu^+ \mu^- + jets$
 - ▶ $pp \rightarrow t\bar{t} + jets$
- Preselection Cuts (a) : Two oppositely charged muons with $p_T > 10$ GeV accompanied with two light jets and at least one tau-tagged jet of $p_T > 20$ GeV.
- Preselection Cuts (b) : b -veto on the final state to suppress the $t\bar{t} + jets$ and $tW + jets$ background.
- The invariant mass of the di-muon system ($M_{\mu\mu}$) satisfies $|M_{\mu\mu} - M_A| < 2.5$ GeV.
- Other cuts from kinematic distributions.

Collider searches for H and H^\pm

Kinematic distributions - I

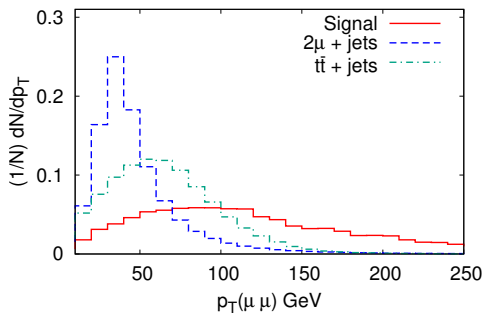
The 2μ system is originates from a light A which in turn comes from heavy H/H^\pm decay. Expected to be boosted.



Collider searches for H and H^\pm

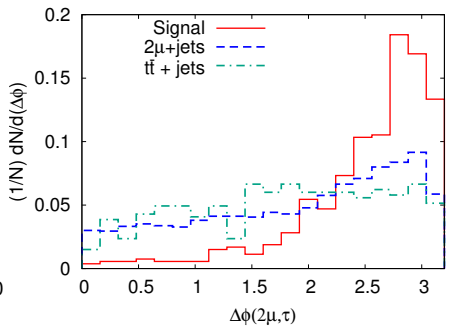
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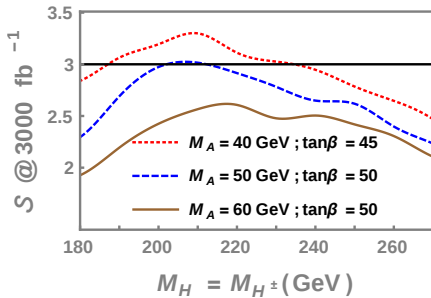
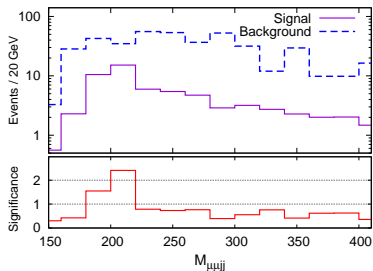
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Kinematic distributions - II

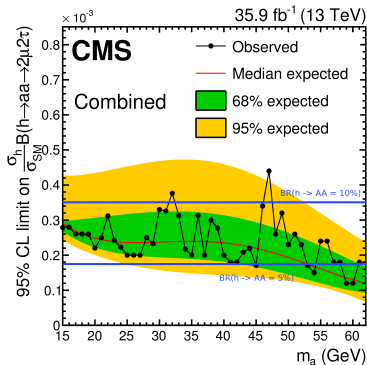
Azimuthal separation between the $\mu\mu$ & the τ -jet.
 The H^\pm and A are expected to be almost back-to-back.





- Low M_{H^\pm} : Significance decreases as not enough branching to $W^\pm A$.
- Also low boost for the $\mu\mu$ system.
- High M_{H^\pm} : Low production cross-section.

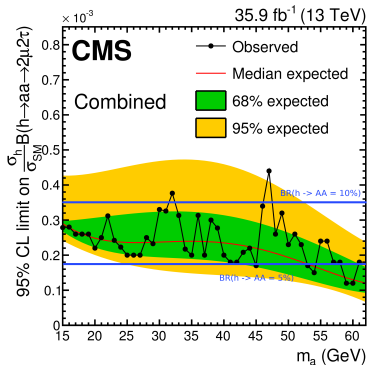
Chun,Dwivedi,TM,Mukhopadhyaya,Rai PRD 98 (2018) 7



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- $\lambda_{hAA} = \frac{-1}{v} \left[2m_A^2 + \xi_h^\ell m_h^2 - (s_{\beta-\alpha}^2 + \xi_h^\ell s_{\beta-\alpha}) m_H^2 \right]$.
- λ_{hAA} can be very small in Wrong Sign limit due to cancellation when $m_H \gg m_h/m_A$.
- Can not restrict the light A – large $\tan \beta$ scenario.
- Q. Can we explore light pseudoscalar without any additional information ?

CMS reported $2\mu 2\tau$ search in 2018

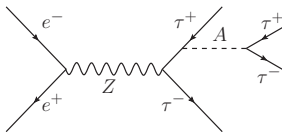


JHEP 11 (2018) 018

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- A. **ILC**

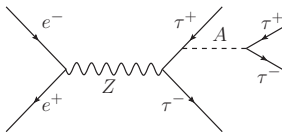
Searches for light A in 2HDMX at ILC250

- The channel $Z \rightarrow h_{125}A$ is not possible since the relevant coupling is proportional to $\cos(\beta - \alpha)$.
- At ILC250 $Z \rightarrow HA$ may not be feasible when H is heavier than 200 GeV.
- Possible search option : $Z \rightarrow \tau\tau \rightarrow \tau\tau A \rightarrow 4\tau$. So called Yukawa production.

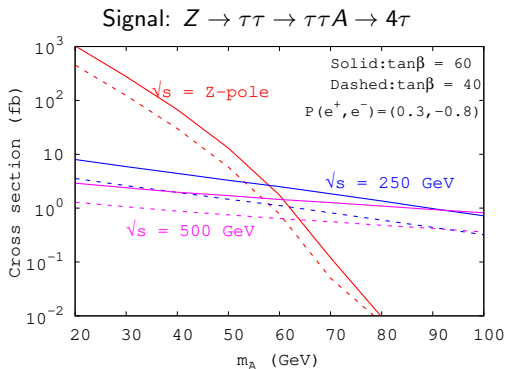


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- This is the equivalent to $t\bar{t}H$ searches at LHC. Independent probe of Yukawa structure.
- At the ILC all the 4τ s can be reconstructed using collinear approximation.
- This enables to measure mass of the light particle.



- Dominant Backgrounds : $e^+e^- \rightarrow Z(\gamma^*) \rightarrow 4\tau$
- Also $e^+e^- \rightarrow Z(\gamma^*) \rightarrow 2\tau 2j$ with mis-identified jets
- Other background : $e^+e^- \rightarrow Zh \rightarrow 4\tau$
- Parton level total 4τ BG cross-section $\simeq 6.6 \text{ fb}$. $2\tau 2j \simeq 100 \text{ fb}$.

- MadGraph_aMC@NLO → PYTHIA8 → Delphes3 + ILD card
- Signal : 3 τ -tagged jets + X (= τ -jet/untagged jet/lepton) so that total number of object = 4.
- Jets and leptons should have minimum energy of 20 GeV and should be in the central region with $|\eta| < 2.3$ i.e. $\cos\theta < 0.98$.
- τ -tagging efficiency : 60%(From LHC) or 90%(Hopefully at ILC).
- Mis-identification of jets: 0.5%

Collinear approximation : Reconstruction of the taus

- The collinear approximation : Assume that the missing energy in the decay of a tau lepton is collinear to the visible part of the decay.
- Energy momentum equations are,

$$\begin{aligned}\vec{p}(\tau_1) + \vec{p}(\tau_2) + \vec{p}(\tau_3) + \vec{p}(\tau_4) &= \vec{0}, \\ E(\tau_1) + E(\tau_2) + E(\tau_3) + E(\tau_4) &= \sqrt{s}.\end{aligned}$$

- Visible part of the tau decay take z_i fraction of the tau momentum :
 $p^\mu(j_i) = z_i p^\mu(\tau_i)$
- Solve for z_i where we should have $0 < z_i < 1$. However to account for the detector resolution etc we assume 10% relaxation in the upper limit of z_i .

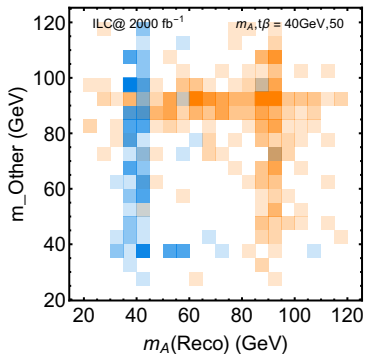
Reconstruction of the pseudoscalar

- We have 4 tau jets. However, the highest energy τ out of the four is unlikely to come from the pseudoscalar since the maximum available energy for A is $125 \text{ GeV}(\sqrt{s}/2)$, whereas energy of highest τ can also be 125 GeV.
- It is reasonable to assume that the highest energy tau is coming from the decay of Z and did not radiate an A .
- From the remaining 3 taus there are two possible OS combinations.
- Choose the combination which gives highest transverse momentum(p_T) since they are likely to come from the decay of A . The invariant mass calculated from this combination is denoted as $m_A(\text{Reco})$.
- The invariant mass from the other opposite sign tau pair is denoted as m_{Other} .

Reconstruction of the pseudoscalar

$m_A = 40$ GeV and $\tan \beta = 50$

For different m_A

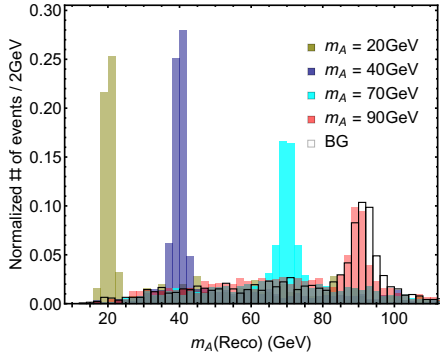
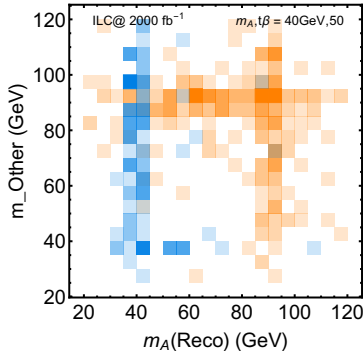


Searches for light A in 2HDMX at ILC250

Reconstruction of the pseudoscalar

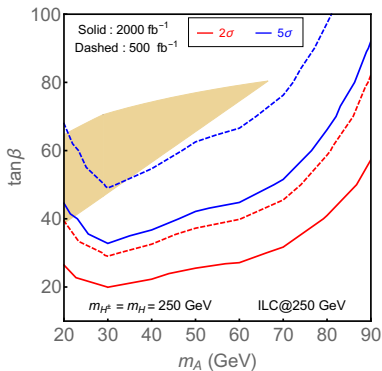
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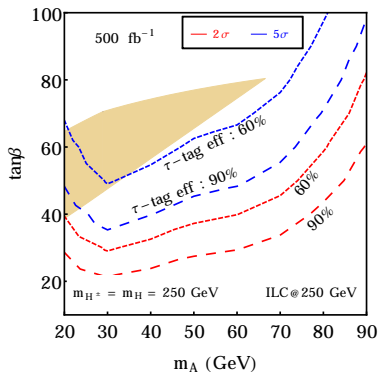
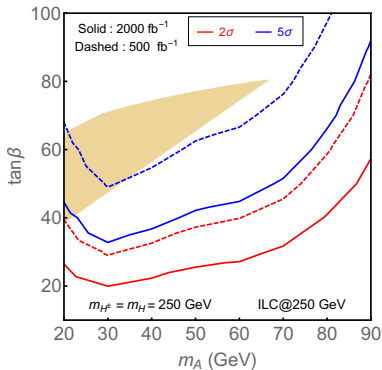
Chun, TM PLB 802 (2020) 135190

Reach of ILC250. $\epsilon_\tau = 60\%$



Searches for light A in 2HDMX at ILC250 : Result

Reach of ILC250. $\epsilon_\tau = 60\%$



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Explaining electron and muon anomalous magnetic moment in 2HDM-X

Electron and muon $g - 2$ anomalies

Electron anomalous magnetic moment:

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$$\delta a_e = a_e^{\text{EXP}} - a_e^{\text{SM}} = - (8.8 \pm 3.6) \times 10^{-13}$$

Muon anomalous magnetic moment:

$$\delta a_\mu = a_\mu^{\text{EXP}} - a_\mu^{\text{SM}} = (2.706 \pm 0.726) \times 10^{-9}$$

- Deviations are in opposite directions
- Also $\frac{\delta a_\mu}{\delta a_e} \neq \frac{m_\mu^2}{m_e^2}$
- Possibly of different origin \Rightarrow light A in 2HDM-X can not explain both.
- Q. What minimal modification in 2HDM-X can explain both $\delta a_{e/\mu}$?

Electron and muon $g - 2$ anomalies

2HDM + Vector-like leptons ($L_{L,R}$ and $E_{L,R}$)

$$\begin{aligned}
 -\mathcal{L} \supset & y_e \bar{\ell}_L e_R \Phi_1 + \lambda_L \bar{L}_L e_R \Phi_1 + \lambda_E \bar{\ell}_L E_R \Phi_1 \\
 & + \lambda \bar{L}_L E_R \Phi_1 + \bar{\lambda} \Phi_1^\dagger \bar{E}_L L_R + M_L \bar{L}_L L_R + M_E \bar{E}_L E_R + \text{h.c.}
 \end{aligned}$$

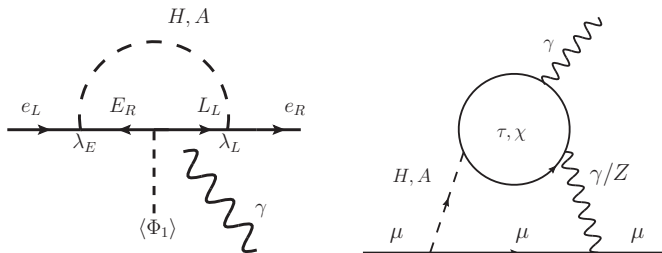
Mass matrix for charged leptons:

$$\mathcal{L}_{mass} = (\bar{\ell}_{L_i}, \bar{L}_L^-, \bar{E}_L) \mathcal{M}_E \begin{pmatrix} \ell_{R_j} \\ L_R^- \\ E_R \end{pmatrix} + \text{h.c.}$$

$$\mathcal{M}_E = \begin{pmatrix} \frac{1}{\sqrt{2}} y_{e,ij} v_1 & 0 & \frac{1}{\sqrt{2}} \lambda_{E_i} v_1 \\ \frac{1}{\sqrt{2}} \lambda_{L_j} v_1 & M_L & \frac{1}{\sqrt{2}} \lambda v_1 \\ 0 & \frac{1}{\sqrt{2}} \bar{\lambda} v_1 & M_E \end{pmatrix},$$

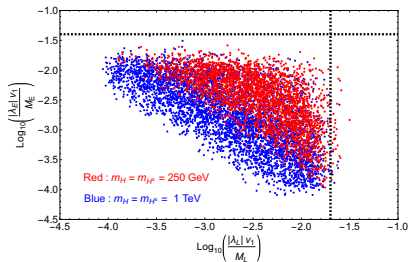
- Mass diagonalization : $\tilde{U}_L^\dagger \mathcal{M}_E \tilde{U}_R = \text{diag}(m_e, m_\mu, m_\tau, m_1, m_2)$
- We assume $\lambda_{E_2}, \lambda_{E_3}, \lambda_{L_2}, \lambda_{L_3} = 0$

Electron and muon $g - 2$ anomalies

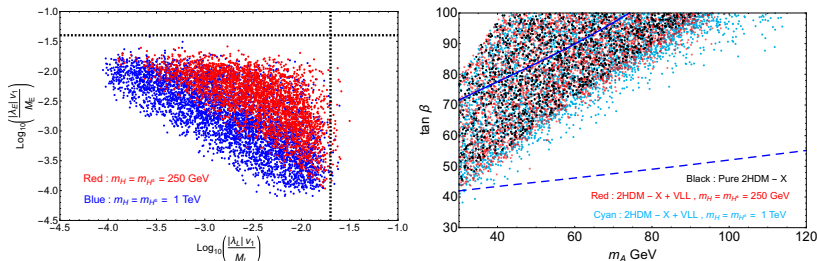


- Electron $g - 2$ diagrams mediated by W and Z bosons is small.
- When VLL is heavier than H/A , then H and A contribution will cancel partially.

$v_1 \frac{ \lambda_{L/E} }{M_{L/E}}$	$\lambda, \bar{\lambda}$	$M_L(\text{GeV})$	$\Delta M = \frac{M_E - M_L}{M_E + M_L}$	$M_A(\text{GeV})$	$\tan \beta$
$(10^{-1}, 10^{-5})$	$(-\sqrt{4\pi}, \sqrt{4\pi})$	(500, 1000)	(0.01, 0.10)	(30, 150)	(30, 100)

Electron and muon $g - 2$ anomalies

Electron and muon $g - 2$ anomalies



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- The dashed lines in left plot are constraints coming from Z pole observables:

$$\frac{v_1 |\lambda_E|}{M_E} \leq 0.04 \quad \text{and} \quad \frac{v_1 |\lambda_L|}{M_L} \leq 0.02.$$

- Right plot : Solid(dashed) lines are upper limit on $\tan \beta$ from $Z \rightarrow \ell\ell$ for $M_H = 250(1000)\text{GeV}$.
- The VLL loop contribution for $(g - 2)_\mu$ is small due to chiral mass insertion in the fermion loop in BZ diagram. Contribution $\propto \left(\frac{\lambda/\bar{\lambda} v_1}{M_{L/E}}\right)$.

Electron and muon $g - 2$ anomalies

The model has interesting signature at the LHC

- VLL couples dominantly to new scalars ($A/H/H^\pm$) as gauge boson couplings are proportional to small vev v_1
- Hence the doublet VLL ($\equiv (L^0, L^-)^T$) signature at the LHC:

$$p p \rightarrow W^{*+} \rightarrow L^0 L^+ \rightarrow (H^+ e^-)(H/A e^+) \rightarrow e^+ e^- H^+ H/A.$$

- Depending on M_A and $\tan \beta$, $H(H^\pm)$ decays to $\tau\tau(\tau\nu)$ or $ZA(WA)$
- Since $M_L \gg M_A \Rightarrow L^+ \rightarrow e^+ A$ will produce a highly boosted A :

$$p_T(A) \sim \frac{m_{L^+}^2 - m_A^2}{2 m_{L^+}}$$

- The tau pair from the A will be collimated and appear as merged jet
- 'di- τ ' tagger by ATLAS can be used to look for such light boosted pseudoscalar
- Another signature will be a lepton in the close proximity of a tau-jet.

- 2HDM : one of the simplest BSM scalar structure.
- Type-X 2HDM : Can explain muon $g - 2$ anomaly. Constrained by lepton universality.
- The allowed parameter space can be explored at the LHC.
- Conventional signature at LHC : multi τ -tagged jets.
- Can't reconstruct the mass of mediator. Hard to trigger for low mass pseudoscalar.
- One needs to look for $\mu\mu\tau\tau$ final state.
- Due to light A , the tau-tagged jets takes almost all the momentum from the taus.
- This enables us to reconstruct $M_{j_\tau j_\tau}$ and $M_{2\mu 2j_\tau}$. We can restrict $h \rightarrow AA$ branching ratio.
- Using the associated production the heavy scalar/charged higgs can be reconstructed.
- Sweet spot : $M_{H^\pm} \sim [200 - 240]$ GeV with $M_A \sim [40 - 50]$ GeV.

- Due to hadrophobic nature it is hard to probe light A at the LHC.
- Lepton collider can be ideal to test the model.
- We can utilize ILC *Higgs Factory* for testing the light A scenario independent of the mass scale of the other scalars (H/H^\pm).
- It is possible to reconstruct the mass of the resonance using collinear approximation.
- 500 fb^{-1} is enough to explore the relevant parameter space.
- Recent measurement of electron $g - 2$ can not be explained the pure Type-X 2HDM.
- A family of vector-like lepton doublet and singlet can explain both the anomalies.
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Thank You