

CP-violating light dark sector

Wen Yin (Tohoku University) 殷文 (東北大学)

Based on [2111.03653](#) with Kodai Sakurai and

[Phys.Rev.D 104 \(2021\) 9, 095010](#) with

Dongok Kim, Younggeun Kim, Yannis K. Semertzidis, Yun Chang Shin, @ Osaka University, Nov 30th 2021

Contents

- 1. Introduction - light axion/ALP DM and CP
- 2. A CP-even ALP from generic CPV
- 3. Phenomenology of CP even ALP
- 4. Cosmic axion force from ultra-light ALP
- 5. Conclusions

2. Introduction

-light axion/ALP DM and CP-

Light dark matter

- What is dark matter?

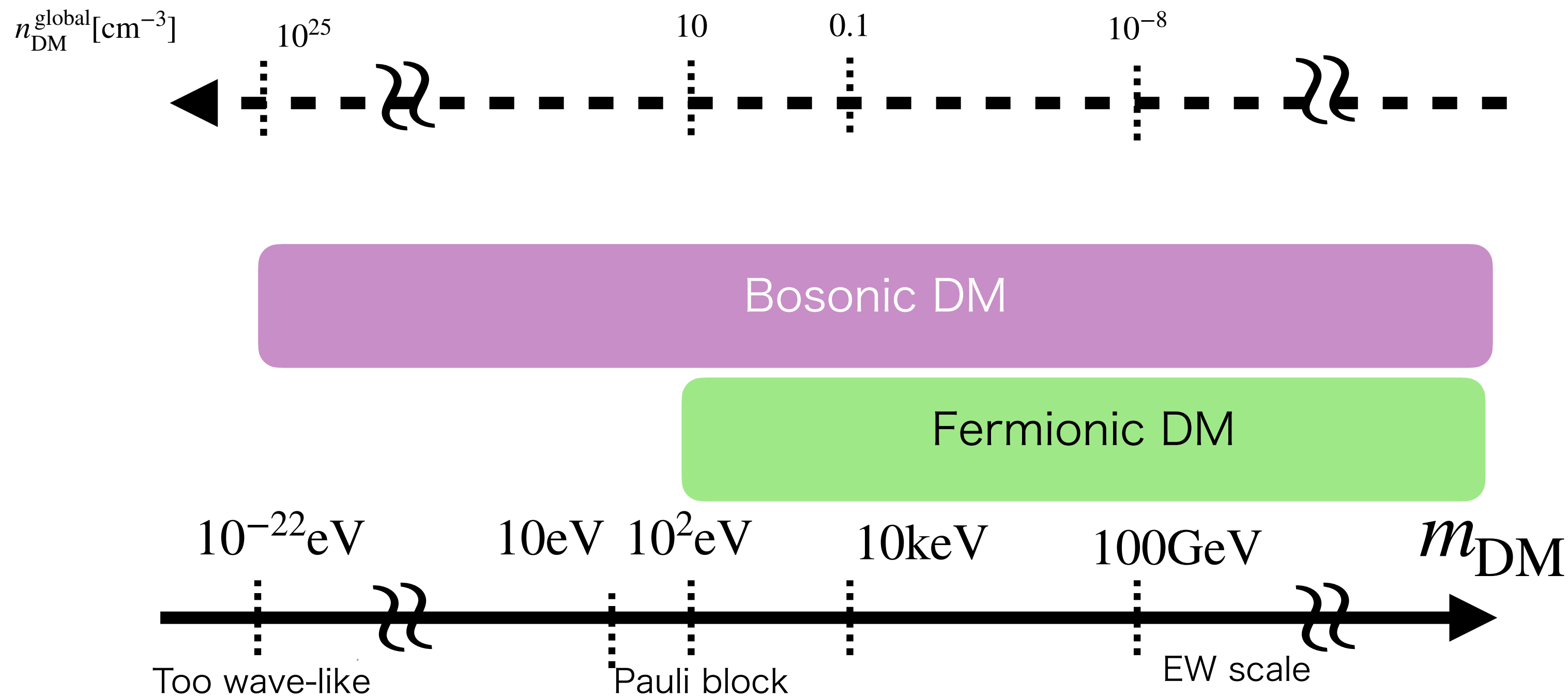
Very stable

Neutral

Cold

$$\rho_{\text{DM}} \quad (= n_{\text{DM}} m_{\text{DM}})$$

- Generic mass range (for a single dominant component DM)



- Questions for very light DM

Why is it light? (what is the origin?)

How to produce it? dense and cold.

How to detect it?

- Light DM candidates

Boson: axion/ALP, hidden photon etc.

Fermion: chiral fermion
(sterile neutrino) etc

Light dark matter

• What is dark matter?

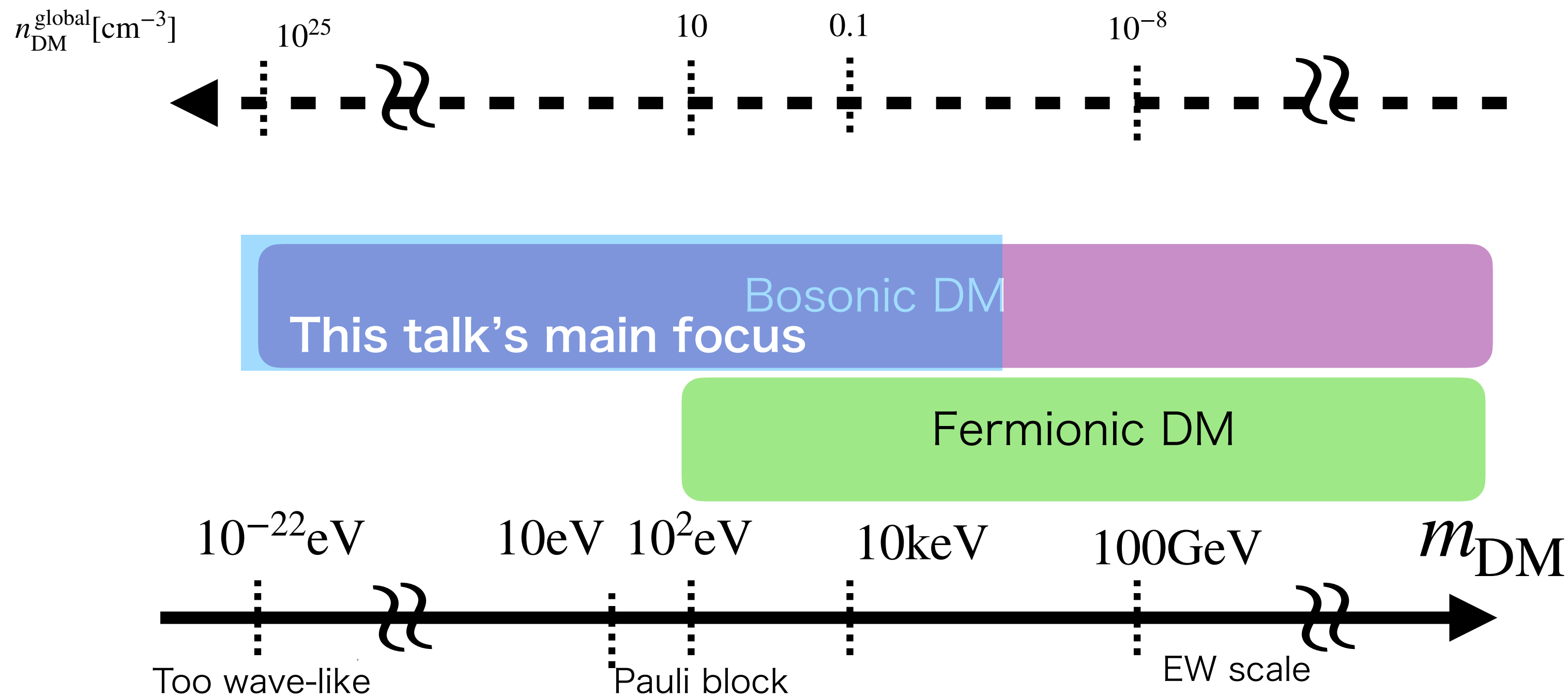
Very stable $\Gamma_{decay} \propto m_{DM}^{positive} \rightarrow$ Light DM?

Neutral

Cold

$$\rho_{DM} \quad (= n_{DM} m_{DM})$$

• Generic mass range (for a single dominant component DM)



• Questions for very light DM

Why is it light? (what is the origin?)

How to produce it? dense and cold.

How to detect it?

• Light DM candidates

Boson: axion/ALP, hidden photon etc.

Fermion: chiral fermion
(sterile neutrino) etc

Light dark matter

• What is dark matter?

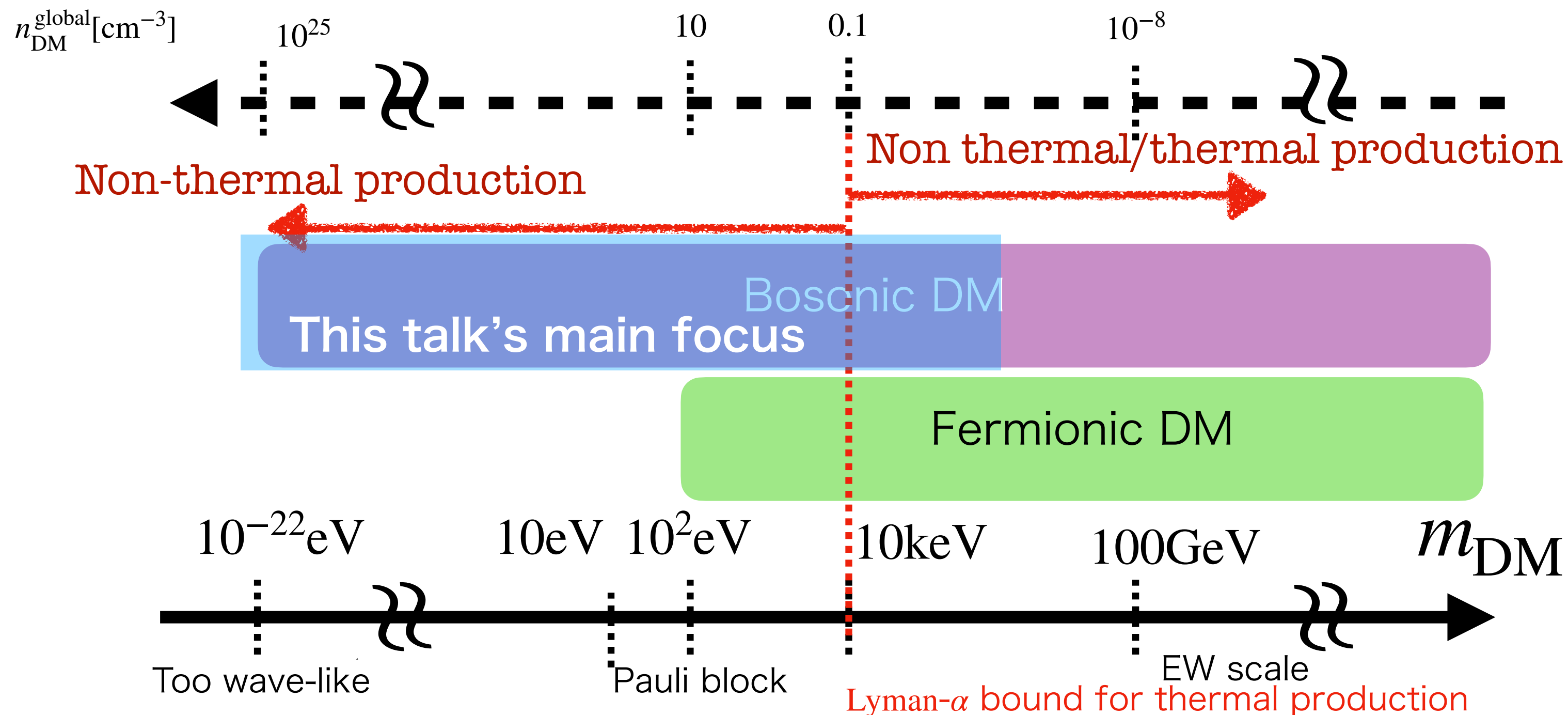
Very stable $\Gamma_{decay} \propto m_{DM}^{positive} \rightarrow$ Light DM?

Neutral

Cold

$$\rho_{DM} \quad (= n_{DM} m_{DM})$$

• Generic mass range (for a single dominant component DM)



• Questions for very light DM

Why is it light? (what is the origin?)

How to produce it? dense and cold.

How to detect it?

• Light DM candidates

Boson: axion/ALP, hidden photon etc.

Fermion: chiral fermion (sterile neutrino) etc

Light dark matter

• What is dark matter?

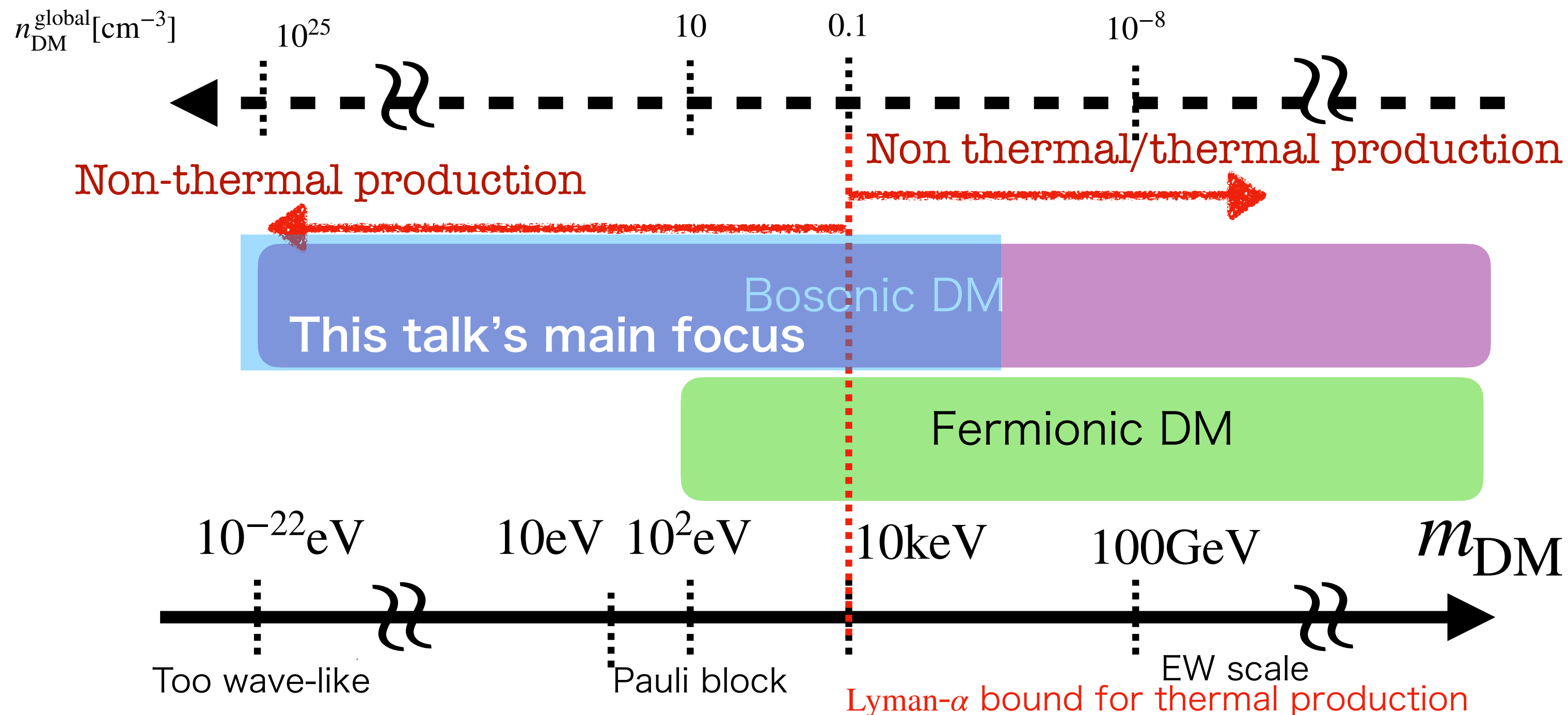
Very stable $\Gamma_{decay} \propto m_{DM}^{positive} \rightarrow$ Light DM?

Neutral

Cold

$$\rho_{DM} \quad (= n_{DM} m_{DM})$$

• Generic mass range (for a single dominant component DM)



• Questions for very light DM

Why is it light? (what is the origin?)

How to produce it? dense and cold.

How to detect it?

• Light DM candidates

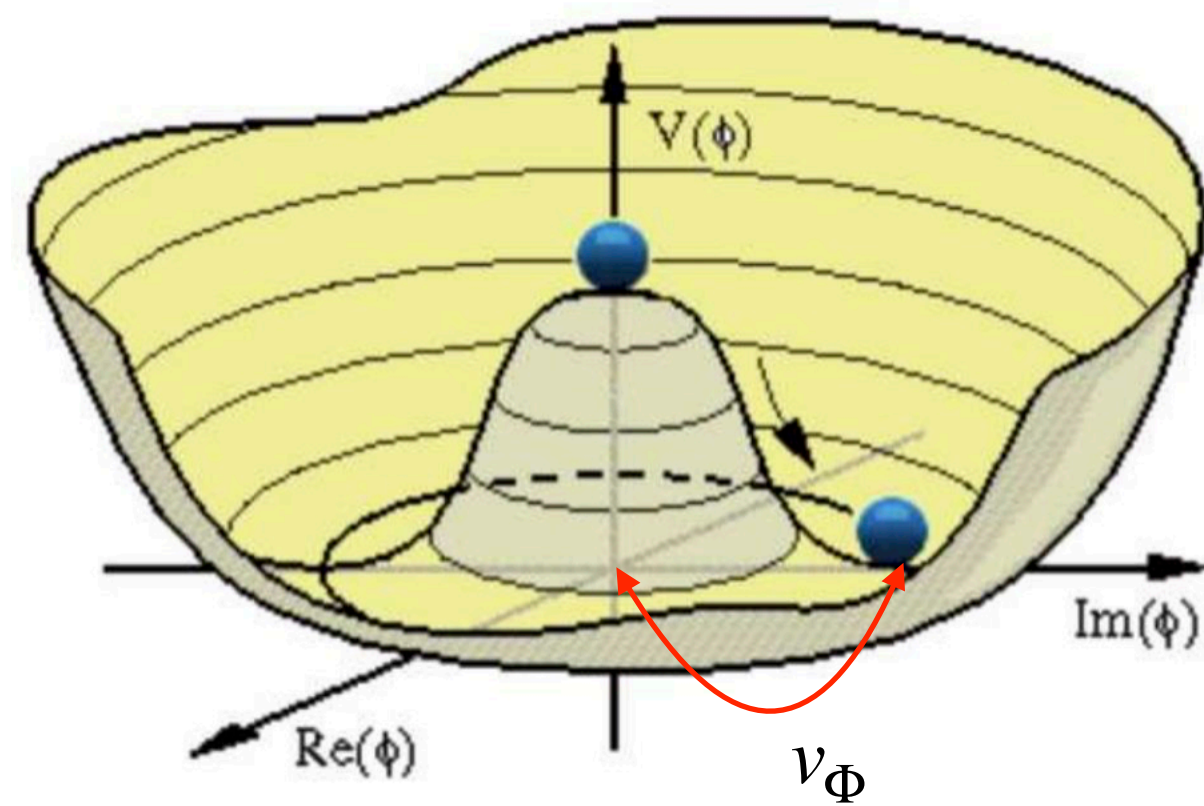
Boson: axion/ALP, hidden photon etc.

Fermion: chiral fermion (sterile neutrino) etc

Review: model of ALP/axion

If a continuous global U(1) symmetry is *spontaneously* broken, there is a Nambu Goldstone Boson (NGB), a , which is massless.

$$V = -m_{\Phi}^2 |\Phi|^2 + \lambda |\Phi|^4 + \lambda_P |H|^2 |\Phi|^2 + \lambda_H |H|^4 - \mu_H^2 |H|^2.$$



U(1) Higgs field: $\Phi \sim (v + s) \exp\left(i \frac{a}{\sqrt{2}v}\right)$

$$U(1) \quad a \rightarrow a + \alpha$$

$$\tilde{V}(a) = \tilde{V}(a + \alpha)$$

The mass of the NGB is 0.

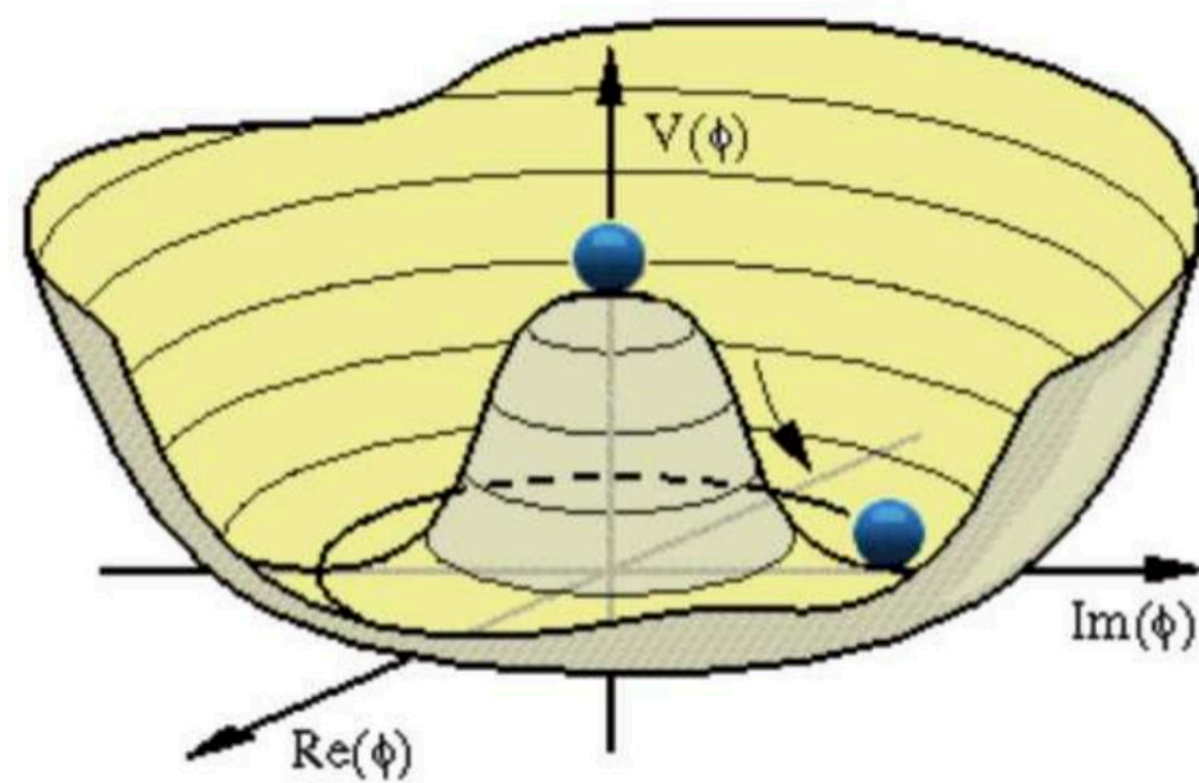
Review: model of ALP/axion

Axion obtains a small mass via **explicit** breaking of U(1)

$$V = -m_{\Phi}^2 |\Phi|^2 + \lambda |\Phi|^4 + \lambda_P |H|^2 |\Phi|^2 + \lambda_H |H|^4 - \mu_H^2 |H|^2.$$

$$+ \kappa m_{\Phi}^3 \Phi + \text{h.c.}$$

(or $\frac{g_s^2 a}{16\pi^2 f_a} G\tilde{G}$) QCD axion



$$\Phi \sim (v_{\Phi} + s) \exp\left(i \frac{a}{\sqrt{2}v}\right)$$

$$\tilde{V} \sim \kappa v_{\Phi}^4 \cos\left[\frac{a}{f_a}\right]$$

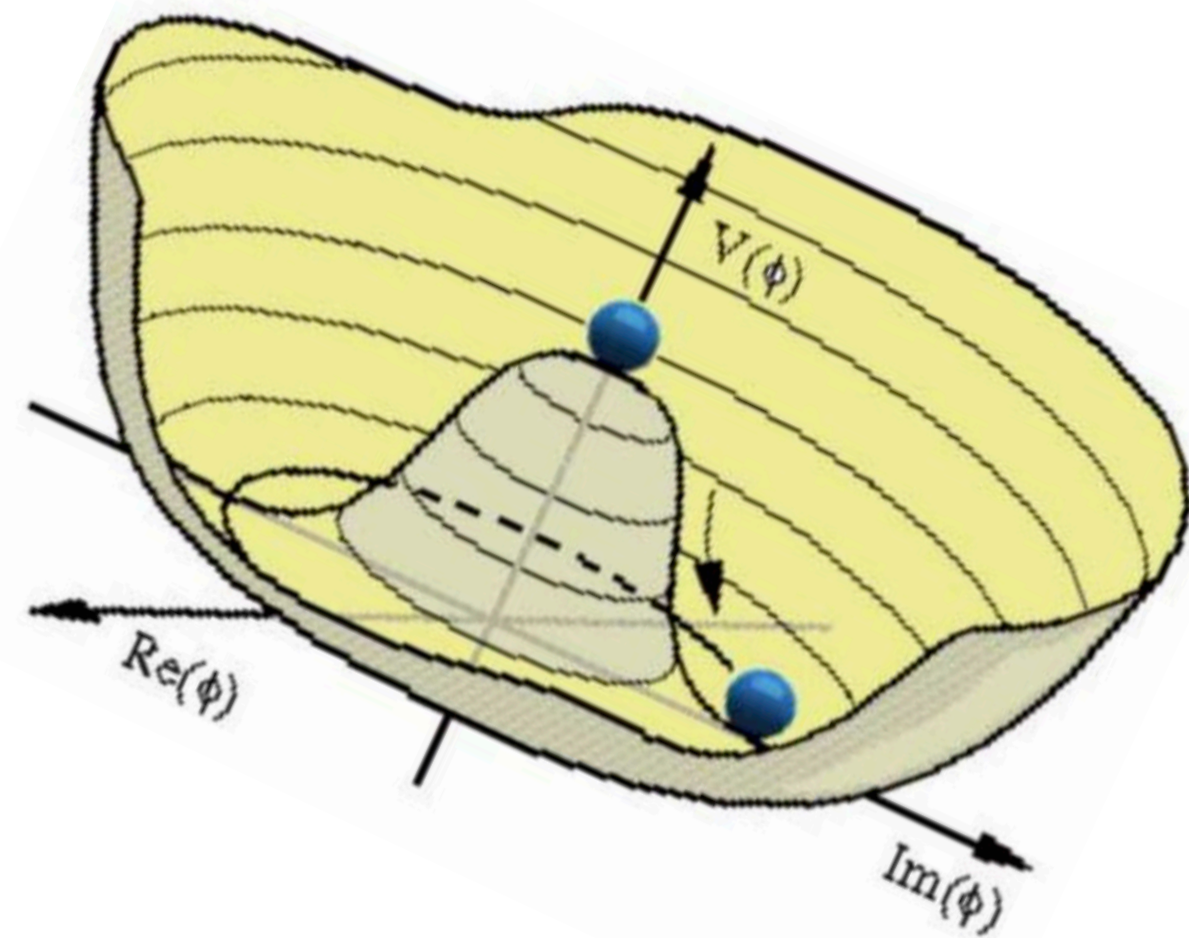
Review: model of ALP/axion

Axion obtains a small mass via **explicit** breaking of U(1)

$$V = -m_{\Phi}^2 |\Phi|^2 + \lambda |\Phi|^4 + \lambda_P |H|^2 |\Phi|^2 + \lambda_H |H|^4 - \mu_H^2 |H|^2.$$

$$+ \kappa m_{\Phi}^3 \Phi + \text{h.c.}$$

(or $\frac{g_s^2 a}{16\pi^2 f_a} G\tilde{G}$) QCD axion



$$\Phi \sim (v_{\Phi} + s) \exp\left(i \frac{a}{\sqrt{2} v}\right)$$

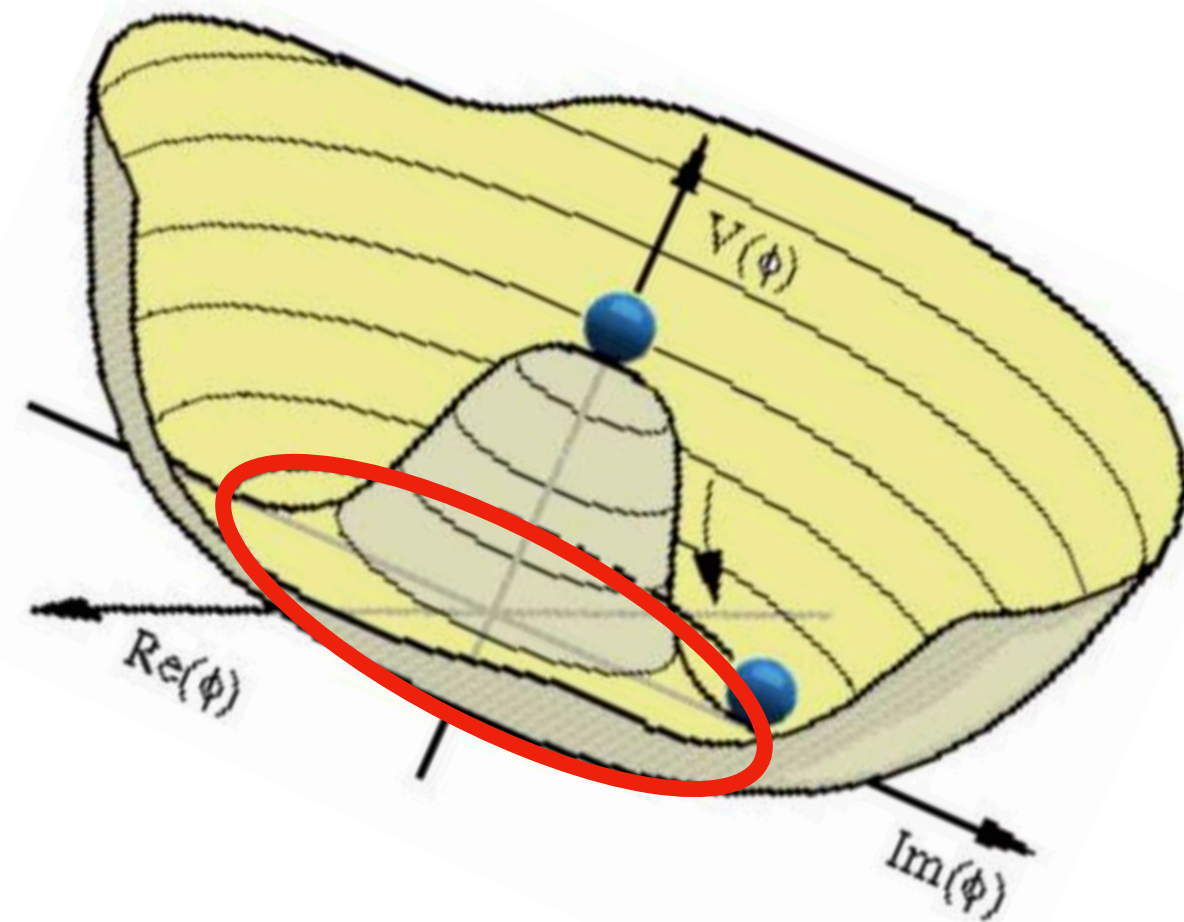
$$\tilde{V} \sim \kappa v_{\Phi}^4 \cos\left[\frac{a}{f_a}\right]$$

Review: model of ALP/axion

Axion obtains a small mass via **explicit** breaking of U(1)

$$V = -m_{\Phi}^2 |\Phi|^2 + \lambda |\Phi|^4 + \lambda_P |H|^2 |\Phi|^2 + \lambda_H |H|^4 - \mu_H^2 |H|^2.$$

$$+ \kappa m_{\Phi}^3 \Phi + \text{h.c.} \quad \left(\text{or } \frac{g_s^2 a}{16\pi^2 f_a} G\tilde{G} \right) \quad \text{QCD axion}$$



$$\Phi \sim (v_{\Phi} + s) \exp\left(i \frac{a}{\sqrt{2}v}\right)$$

$$\tilde{V} \sim \kappa v_{\Phi}^4 \cos\left[\frac{a}{f_a}\right]$$

*QCD axion explains the vanishingly small neutron EDM.

Review: model of ALP/axion

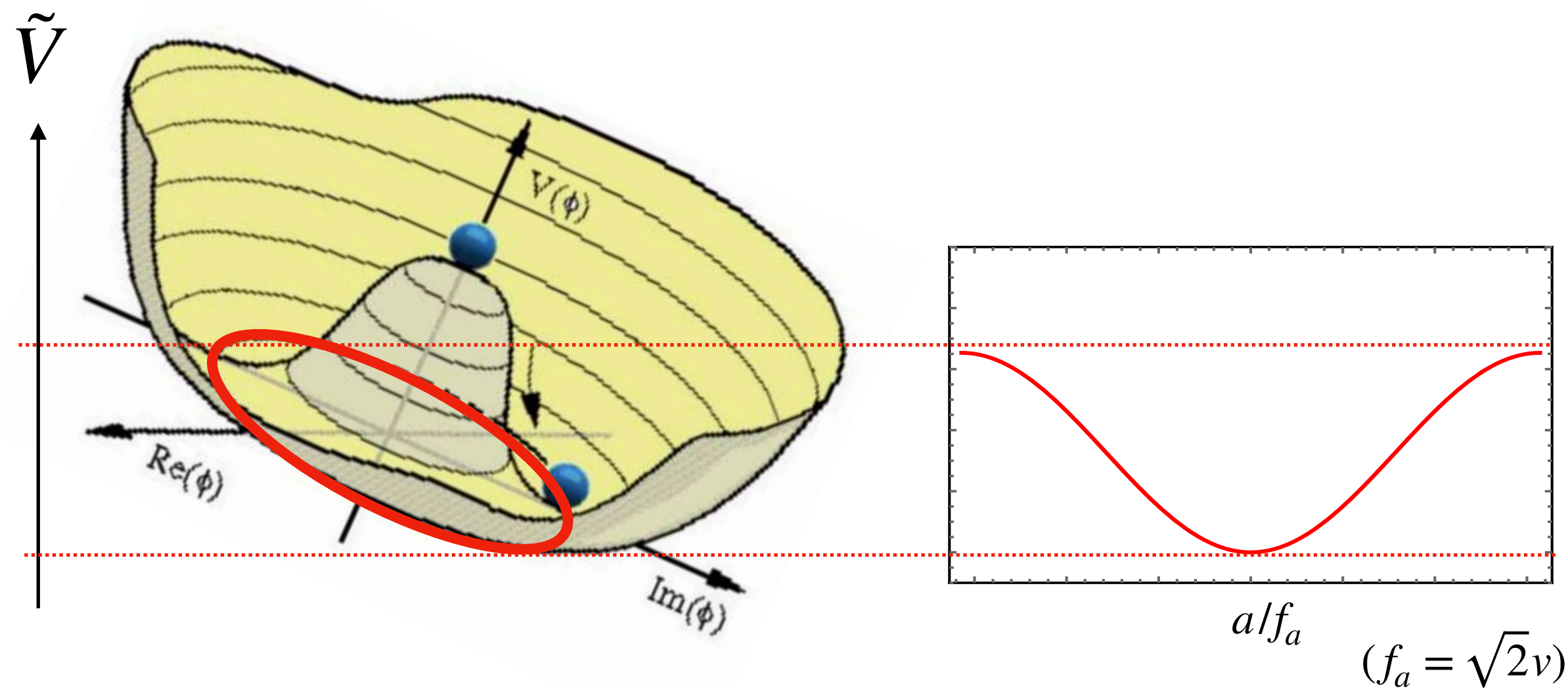
Axion obtains a small mass via **explicit** breaking of U(1)

$$V = -m_{\Phi}^2 |\Phi|^2 + \lambda |\Phi|^4 + \lambda_P |H|^2 |\Phi|^2 + \lambda_H |H|^4 - \mu_H^2 |H|^2.$$

$$+ \kappa m_{\Phi}^3 \Phi + \text{h.c.} \quad \left(\text{or } \frac{g_s^2 a}{16\pi^2 f_a} G\tilde{G} \right) \quad \text{QCD axion}$$

$$\Phi \sim (v_{\Phi} + s) \exp\left(i \frac{a}{\sqrt{2}v}\right)$$

$$\tilde{V} \sim \kappa v_{\Phi}^4 \cos\left[\frac{a}{f_a}\right]$$



*QCD axion explains the vanishingly small neutron EDM.

Review: model of ALP/axion

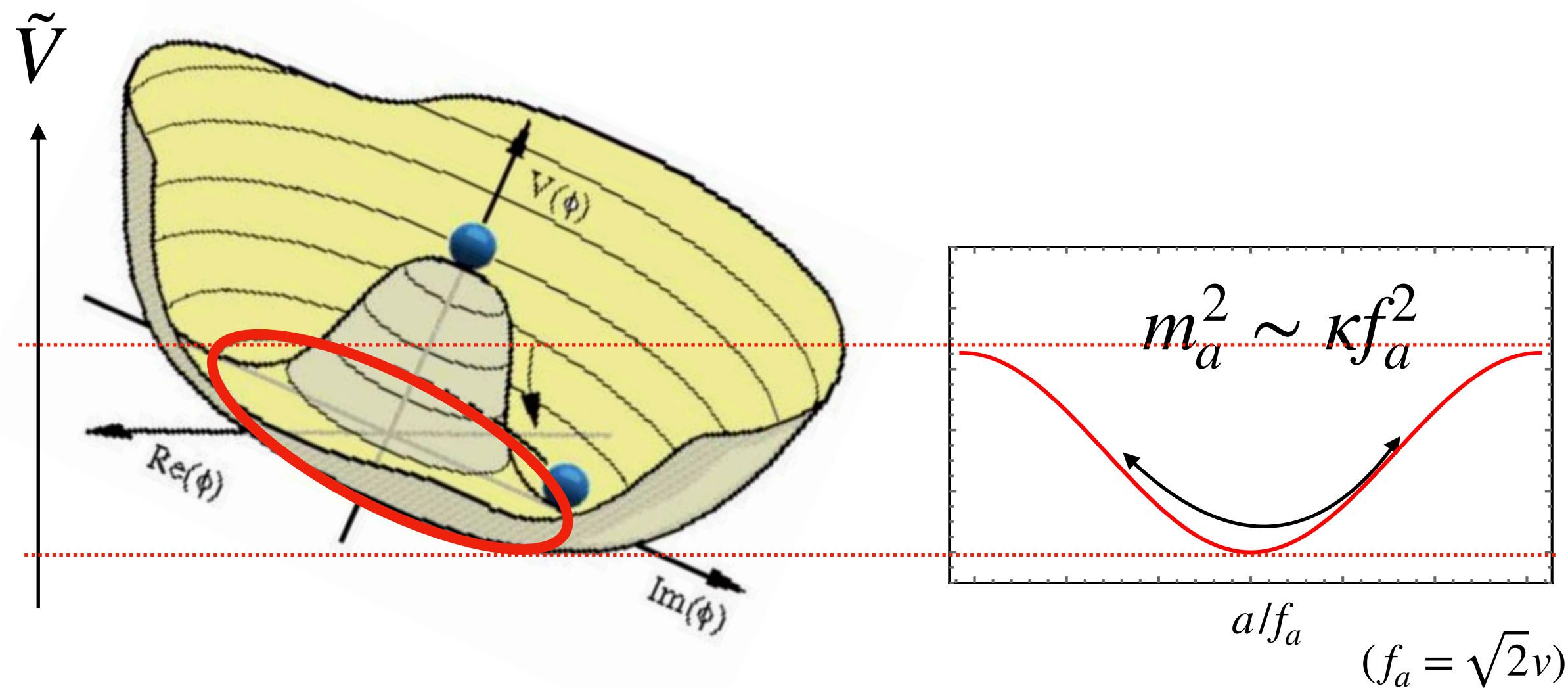
Axion obtains a small mass via **explicit** breaking of U(1)

$$V = -m_{\Phi}^2 |\Phi|^2 + \lambda |\Phi|^4 + \lambda_P |H|^2 |\Phi|^2 + \lambda_H |H|^4 - \mu_H^2 |H|^2.$$

$$+ \kappa m_{\Phi}^3 \Phi + \text{h.c.} \quad \left(\text{or } \frac{g_s^2 a}{16\pi^2 f_a} G\tilde{G} \right) \quad \text{QCD axion}$$

$$\Phi \sim (v_{\Phi} + s) \exp\left(i \frac{a}{\sqrt{2}v}\right)$$

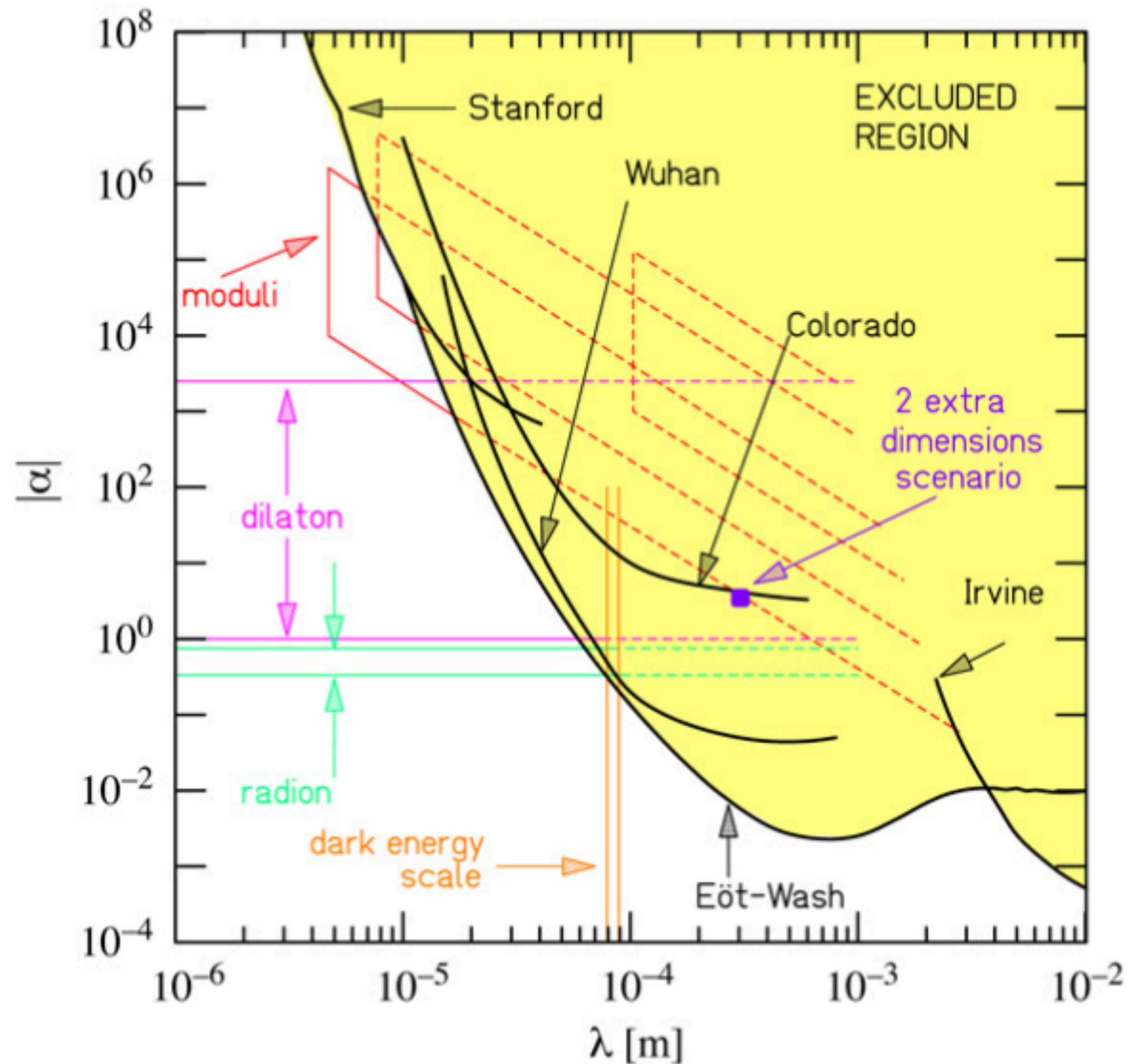
$$\tilde{V} \sim \kappa v_{\Phi}^4 \cos\left[\frac{a}{f_a}\right]$$



*QCD axion explains the vanishingly small neutron EDM.

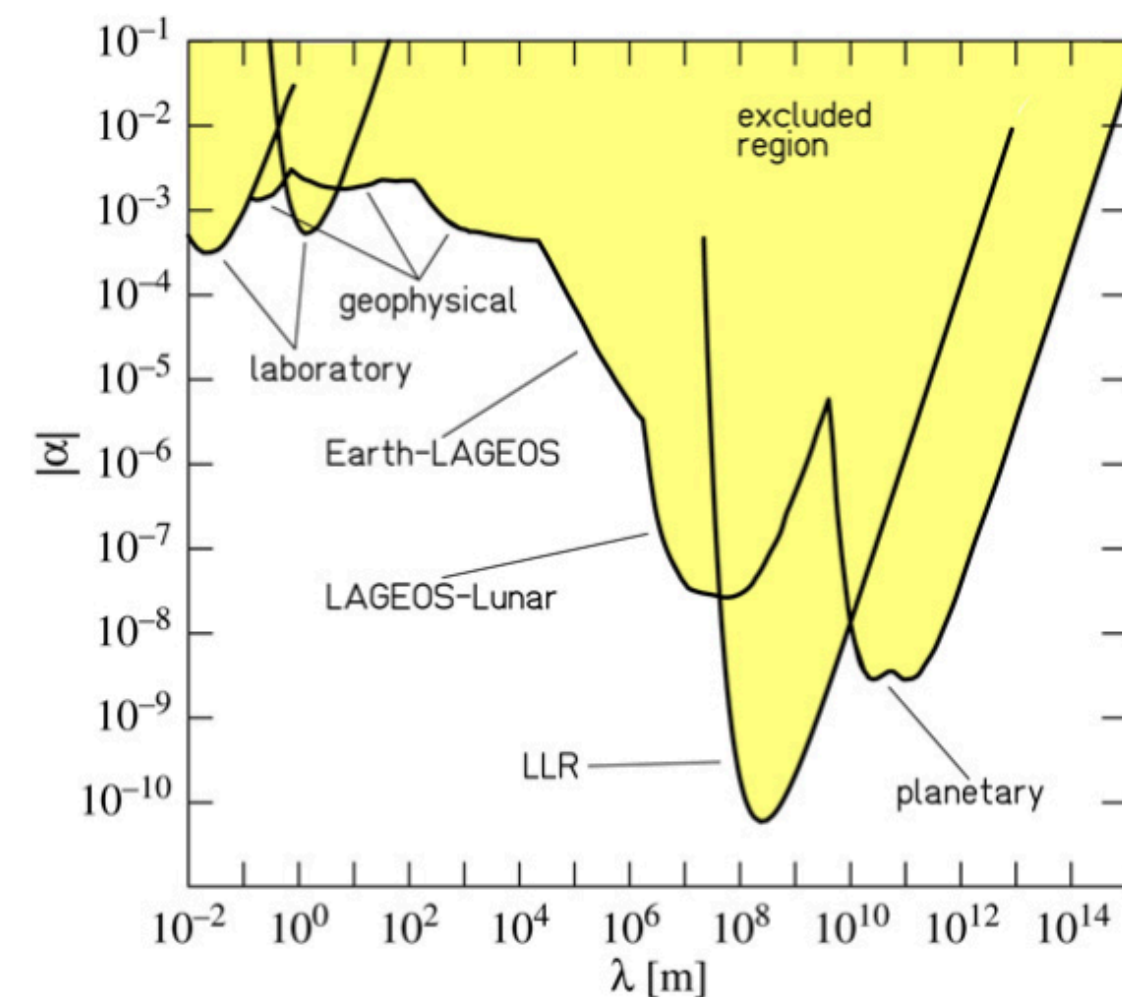
Why not a CP even scalar DM, e.g. modulus?

Fifth force search kills most models with CP even scalar mass $m_\phi < 10^{-3} eV$.



$$V = -G_N \frac{m_1 m_2}{r} (1 + \alpha e^{-r/\lambda})$$

$$\lambda \sim 2 \times 10^{-4} \text{m} \frac{10^{-3} eV}{m_\phi}$$



Why aren't axion/ALP ruled out by the fifth force?

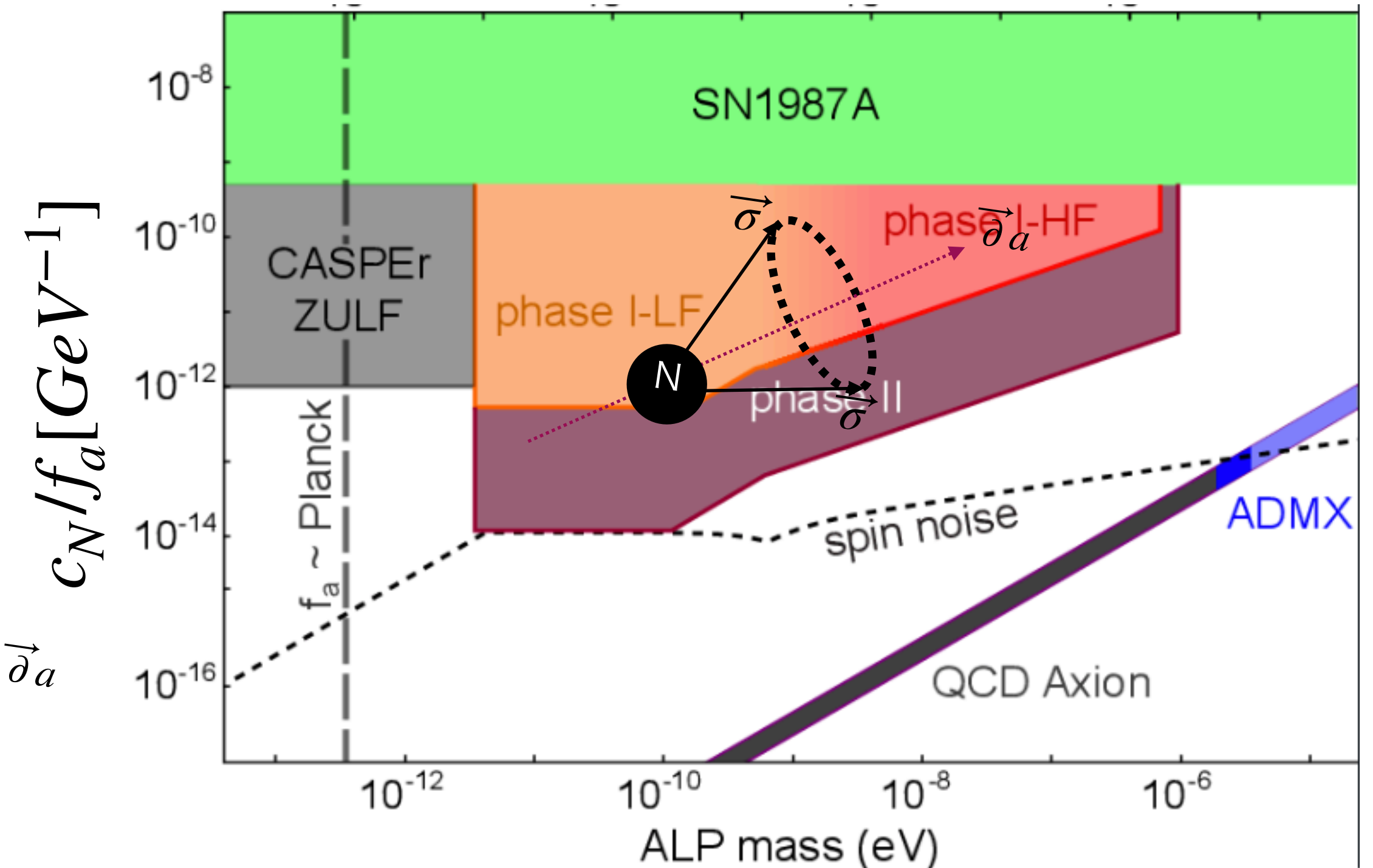
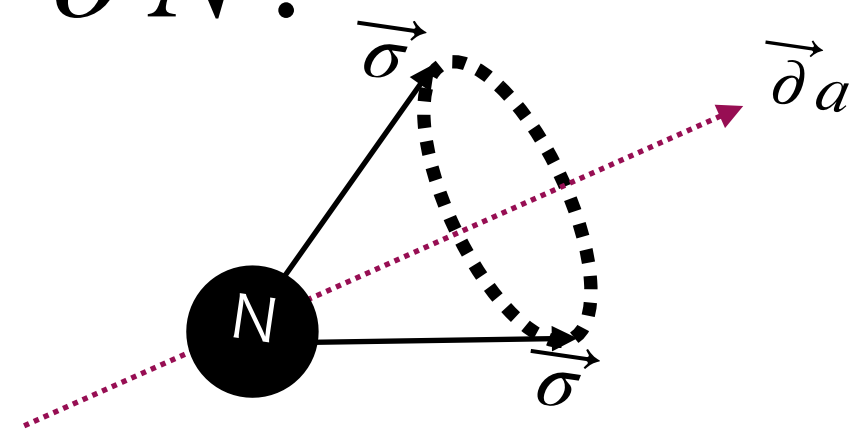
-> They are CP odd particles. Thus the mediated force is short range (dipole-dipole or spin-spin type force).

$$i \frac{c_N M_N}{f_a} a \bar{N} \gamma_5 N$$

It couples nucleon spin.

$$H_{\text{EFT}}^{\text{nonrela}} \simeq - \frac{c_N}{2f_a} \vec{\partial} a \cdot \bar{N} \vec{\sigma} N.$$

$$\vec{\partial} a \sim \vec{v}_{\text{DM}} \sqrt{\rho_{\text{DM}}} \sim 10^{-3} \sqrt{\rho_{\text{DM}}}$$



*It may or may not be a QCD axion depending on whether there is gluon anomaly.

Why aren't axion/ALP ruled out by the fifth force?

-> They are CP odd particles. Thus the mediated force is short range (dipole-dipole or spin-spin type force).

CP symmetry is based on miracle and accident

Strong CP problem $\frac{\alpha_s}{4\pi} \theta_{\text{CP}} G\tilde{G}$ $\theta_{\text{CP}} \lesssim 10^{-10}$

Given the tuning, accidental CP symmetry

$$\mathcal{L} \supset g_{aNN}^{\text{CPV}} a \bar{N} N \quad g_{aNN}^{\text{CPV}} \sim \frac{c_g \theta_{\text{CP}}}{f_a} \frac{2m_u m_d}{(m_u + m_d)^2} \langle N | \sigma | N \rangle$$

Moody and Wilczek, 1984

$$V(r) \sim \frac{\theta_{\text{CP}}^2 M_N^2}{4\pi f_a^2 r} \exp(-m_a r)$$

It is strong CP problem that allows us to have a light CP odd DM.

This problem is naturally solved if there is a QCD axion. But I will not discuss about it.

$$\theta_{\text{eff}} \sim J G_F^2 \Lambda_{\text{QCD}}^4$$

$$J \equiv \text{Im} V_{tb} V_{td}^* V_{cd} V_{cb}^* \sim 10^{-5}$$

$$V(r) \sim \frac{\theta_{\text{eff}}^2 M_N^2}{4\pi f_a^2 r} \exp(-m_a r)$$

EW induced contribution is small by an accident.

Axion/ALP can be light DM without running afoul with 5th force bounds because of the fine-tuning + accidental CP symmetry. This is observational consequence which we have to admit, but

do we really need to impose CP symmetry in dark sector?

3. CP-even ALP from generic CPV

Kodai Sakurai, WY 2111.03653

In the following I take for simplicity $\theta_{CP} = \theta_{CKM} = 0$, which does not change our conclusions.

If we do not impose CP symmetry in the dark sector,

$$V = -m_{\Phi}^2 |\Phi|^2 + \lambda |\Phi|^4 + \lambda_P |H|^2 |\Phi|^2 + \lambda_H |H|^4 - \mu_H^2 |H|^2.$$

Accidental discrete symmetry in dark global U(1) symmetric limit:

C_{dark} symmetry: SM fields do not transform, $\Phi(t, \vec{x}) \rightarrow \Phi^*(t, \vec{x})$

CP symmetry: SM fields transform as in the SM, $\Phi(t, \vec{x}) \rightarrow \Phi^*(t, -\vec{x})$.

If we do not impose CP symmetry in the dark sector,

Explicit breaking of dark $U(1)$ controlled by κ is

$$\delta V = \kappa \left(\sum_{j=1}^4 c_j m_{\Phi}^{4-j} \Phi^j + \sum_{j=1}^2 (\tilde{c}_j^H m_{\Phi}^{2-j} \Phi^j |H|^2 + \tilde{c}_j^{\Phi} m_{\Phi}^{2-j} \Phi^j |\Phi|^2) \right) + \text{h.c.}$$

$\arg c, \tilde{c} \neq 0$

~~C_{dark} symmetry: SM fields do not transform, $\Phi(t, \vec{x}) \rightarrow \Phi^*(t, \vec{x})$~~

~~CP symmetry: SM fields transform as in the SM, $\Phi(t, \vec{x}) \rightarrow \Phi^*(t, -\vec{x})$.~~

If we do not impose CP symmetry in the dark sector,

Explicit breaking of dark $U(1)$ controlled by κ is

$$\delta V = \kappa \left(\sum_{j=1}^4 c_j m_{\Phi}^{4-j} \Phi^j + \sum_{j=1}^2 (\tilde{c}_j^H m_{\Phi}^{2-j} \Phi^j |H|^2 + \tilde{c}_j^{\Phi} m_{\Phi}^{2-j} \Phi^j |\Phi|^2) \right) + \text{h.c.}$$

$$\arg c, \tilde{c} \neq 0$$

But $C_{\text{dark}} \cdot CP$ remains: $SM \rightarrow CP SM$,

$$\Phi(t, \vec{x}) \rightarrow \Phi(t, -\vec{x}) \quad (\text{a parity for dark Higgs}).$$

If we do not impose CP symmetry in the dark sector,

Explicit breaking of dark $U(1)$ controlled by κ is

$$\delta V = \kappa \left(\sum_{j=1}^4 c_j m_{\Phi}^{4-j} \Phi^j + \sum_{j=1}^2 (\tilde{c}_j^H m_{\Phi}^{2-j} \Phi^j |H|^2 + \tilde{c}_j^{\Phi} m_{\Phi}^{2-j} \Phi^j |\Phi|^2) \right) + \text{h.c.}$$

$$\arg c, \tilde{c} \neq 0$$

$$C_{\text{dark}} \cdot CP: \text{SM} \rightarrow \text{CP SM}$$

$$\Phi(t, \vec{x}) \rightarrow \Phi(t, -\vec{x}), \text{ thus } a[t, \vec{x}] (\equiv -i \arg \Phi) \rightarrow a[t, -\vec{x}]$$

If we do not impose CP symmetry in the dark sector,

Explicit breaking of dark $U(1)$ controlled by κ is

$$\delta V = \kappa \left(\sum_{j=1}^4 c_j m_{\Phi}^{4-j} \Phi^j + \sum_{j=1}^2 (\tilde{c}_j^H m_{\Phi}^{2-j} \Phi^j |H|^2 + \tilde{c}_j^{\Phi} m_{\Phi}^{2-j} \Phi^j |\Phi|^2) \right) + \text{h.c.}$$

$\arg c, \tilde{c} \neq 0$

$$CP_{\text{EFT}} \equiv C_{\text{dark}} \cdot CP: \quad \text{SM} \rightarrow \text{CP SM}, \quad a[t, \vec{x}] \rightarrow a[t, -\vec{x}]$$

A simple UV completion of axion without imposing CP symmetry has accidental CP_{EFT} with **ALP being CP-even.**

Couplings of the CP-even ALP

$$V = -m_\Phi^2 |\Phi|^2 + \lambda |\Phi|^4 + \lambda_P |H|^2 |\Phi|^2 + \lambda_H |H|^4 - \mu_H^2 |H|^2.$$

$$\mathcal{L}_{\text{eff}} \sim \frac{\mathcal{O}_{SM}}{m_\Phi^{d_{\mathcal{O}_{SM}}}} (\partial a)^2$$

- Induced from U(1) symmetric part, and thus $C_{\text{dark}} \times CP$ symmetric.
- Non-renormalizable (dim 6 or 8).
i.e. very weak at low energy.

$$\delta V = \kappa \left(\sum_{j=1}^4 c_j m_\Phi^{4-j} \Phi^j + \sum_{j=1}^2 (\tilde{c}_j^H m_\Phi^{2-j} \Phi^j |H|^2 + \tilde{c}_j^\Phi m_\Phi^{2-j} \Phi^j |\Phi|^2) \right) + \text{h.c.}$$

$$\mathcal{L}_{\text{eff}} \sim \frac{m_a^2 m_h}{m_\Phi} a h, \theta_{ah} \sim \frac{m_a^2}{m_h m_\Phi}$$

- Induced from U(1) breaking part.
- At $\kappa \rightarrow 0$, (i.e. $m_a^2 \rightarrow 0$), it vanishes, i.e.
amplitude $\propto m_a^2$
- Renormalizable, dominant at low energy.

3. Phenomenology of CP-even ALP

- Probing CP-even ALP in Higgs factory
- CP-even ALP DM

CP-even ALP can be naturally produced via Higgs boson decay

$$V = -m_{\Phi}^2 |\Phi|^2 + \lambda |\Phi|^4 + \lambda_P |\Phi|^2 |H|^2 + \lambda_H |H|^4 - \mu_H^2 |H|^2.$$

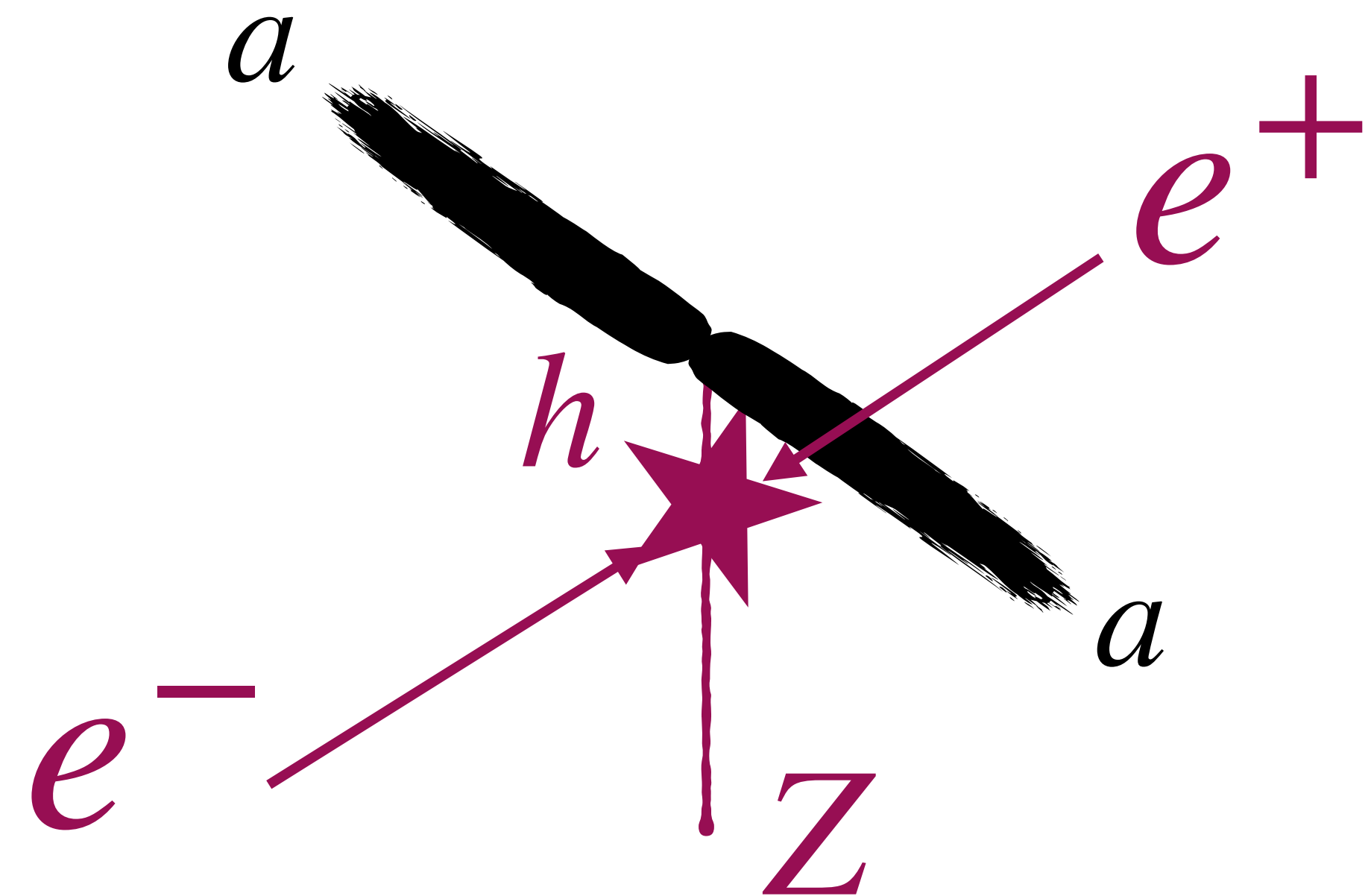
Higgs portal coupling

Φ : U(1) Higgs field
 H : SM Higgs doublet

$$\mathcal{L}_{\text{eff}} \sim \frac{\sqrt{2}v}{\Lambda_H^2} h(\partial a)^2 \quad \frac{1}{\Lambda_H^2} \equiv -\frac{\lambda_P}{m_s^2 - m_h^2}.$$

$$\Gamma_{h \rightarrow aa} \simeq \frac{1}{16\pi} \frac{v^2 m_h^3}{\Lambda_H^4}.$$

$$\text{Br}_{h \rightarrow aa} = 2\% \left(\frac{2\text{TeV}}{\Lambda_H} \right)^4$$



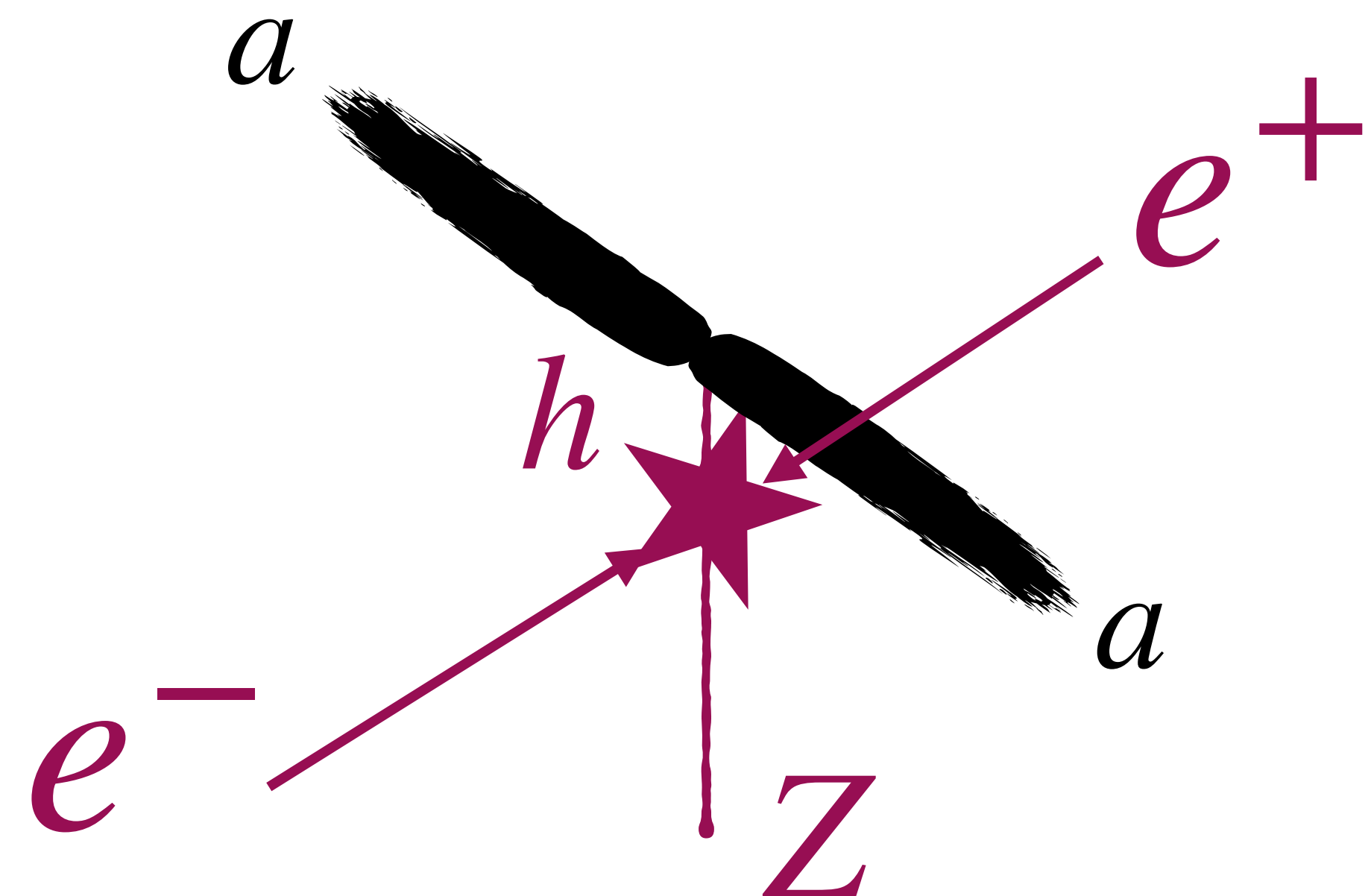
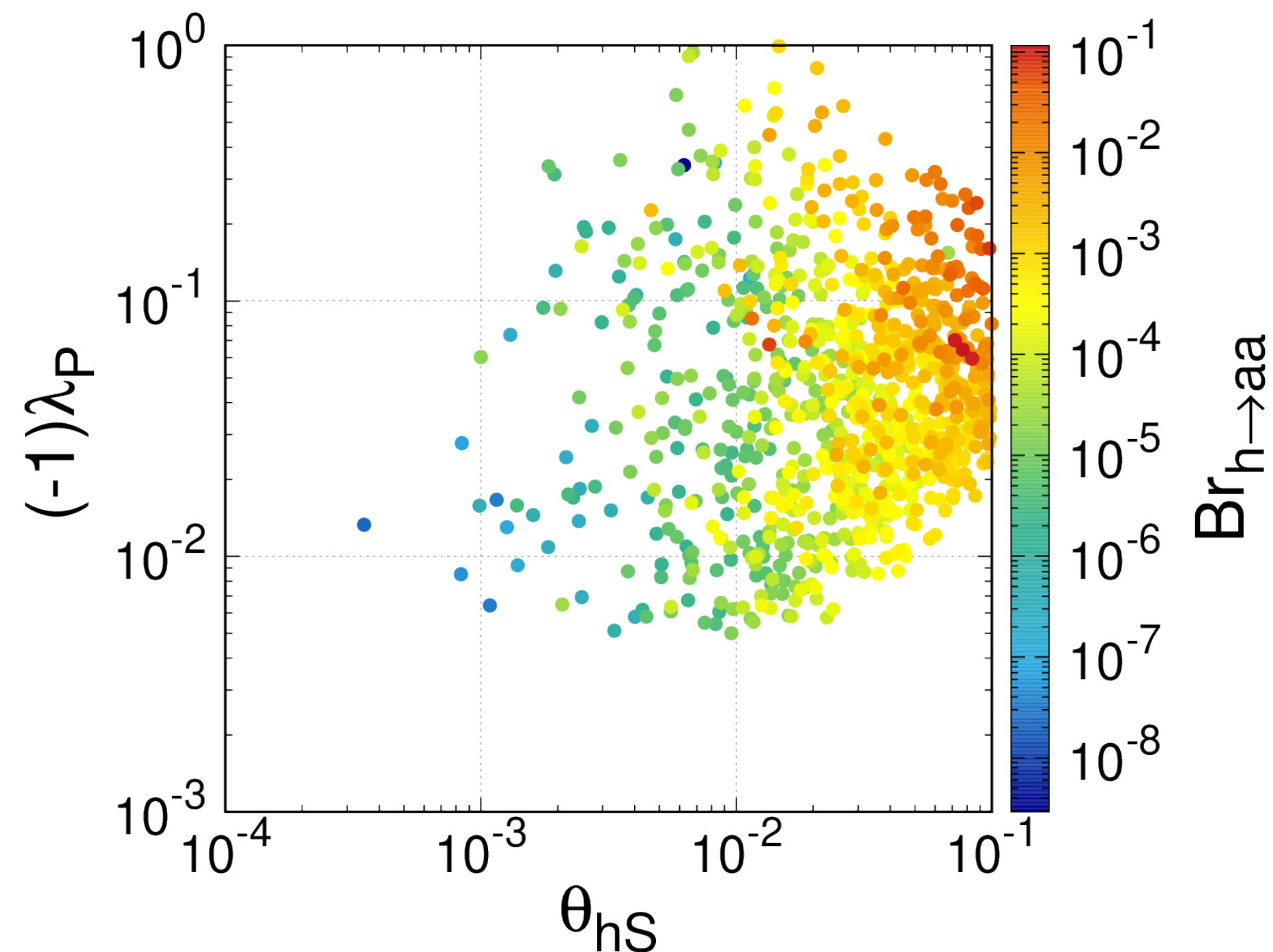
CP-even ALP can be naturally produced via Higgs boson decay

$$V = -m_{\Phi}^2 |\Phi|^2 + \lambda |\Phi|^4 + \lambda_P |\Phi|^2 |H|^2 + \lambda_H |H|^4 - \mu_H^2 |H|^2.$$

Higgs portal coupling

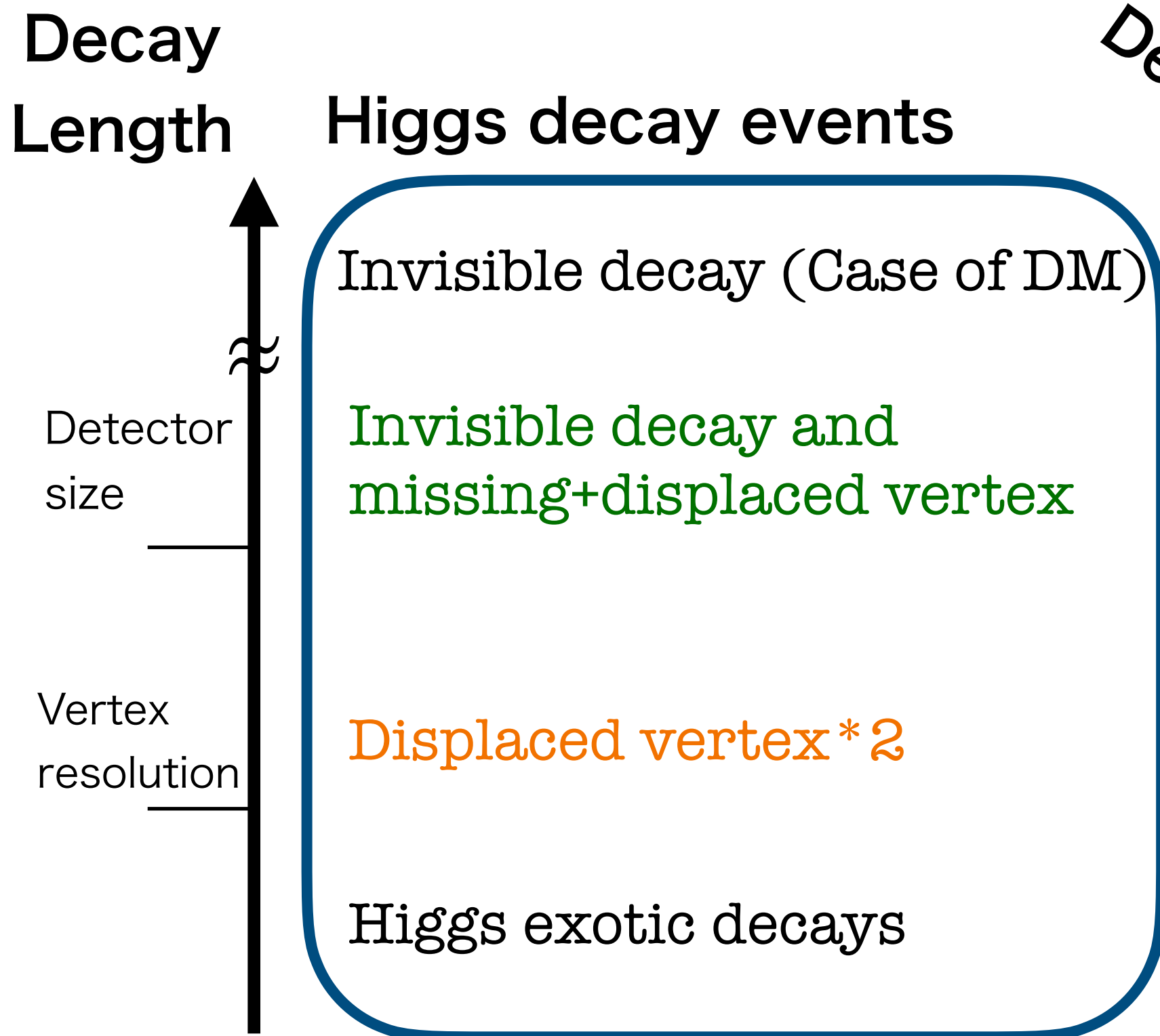
Φ : U(1) Higgs field
 H : SM Higgs doublet

Production from Higgs decay



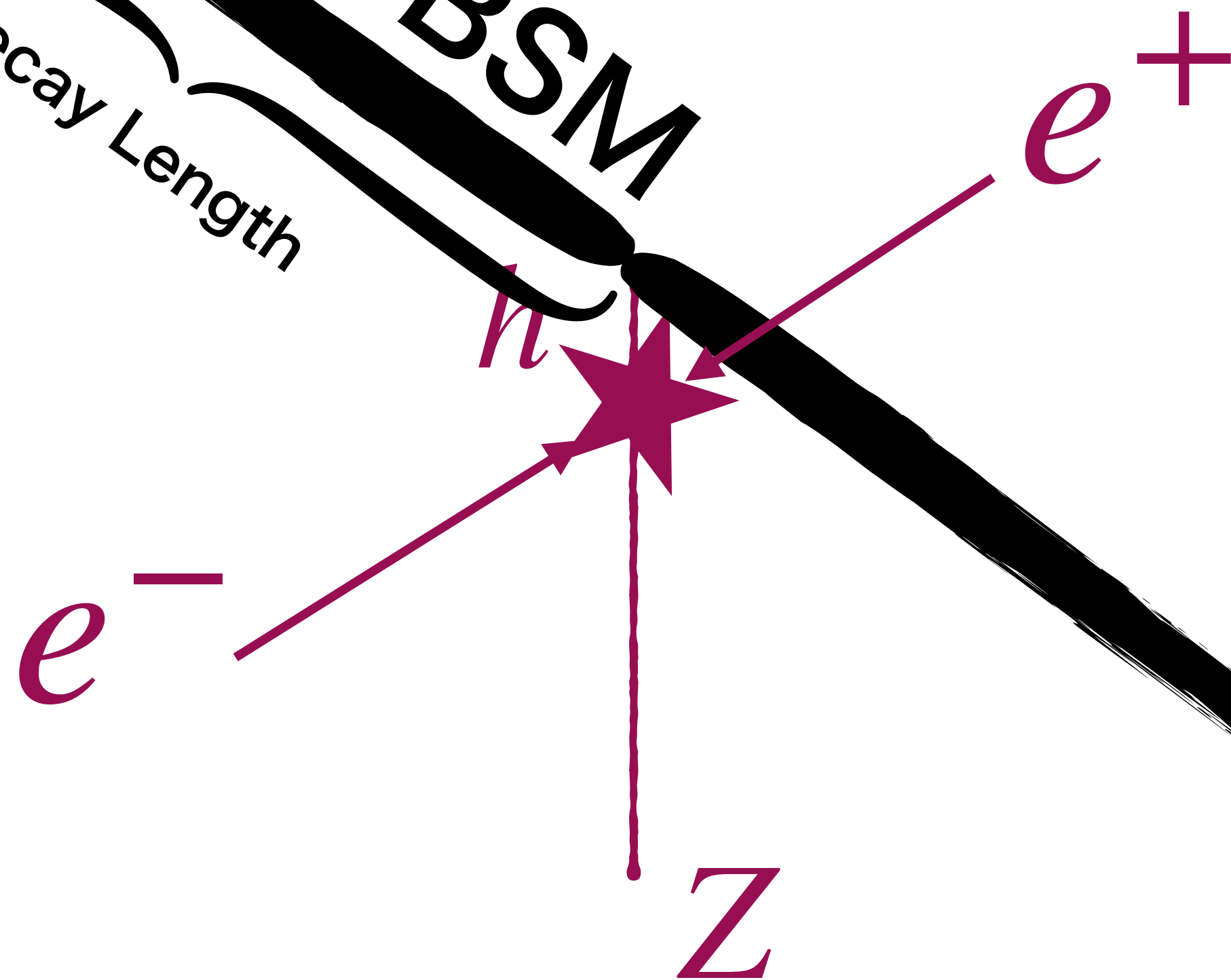
After the production, it is long-lived if light.

$$\delta V = \kappa \left[\sum_{j=1}^4 c_j m_\Phi^{4-j} \Phi^j + \sum_{j=1}^2 (\tilde{c}_j^H m_\Phi^{2-j} \Phi^j |H|^2 + \dots) \right]$$



Light BSM

Decay Length



$$\mathcal{L}_{\text{eff}} \sim \frac{m_a^2 m_h}{m_\Phi} ah, \theta_{ah} \sim \frac{m_a^2}{m_h m_\Phi}$$

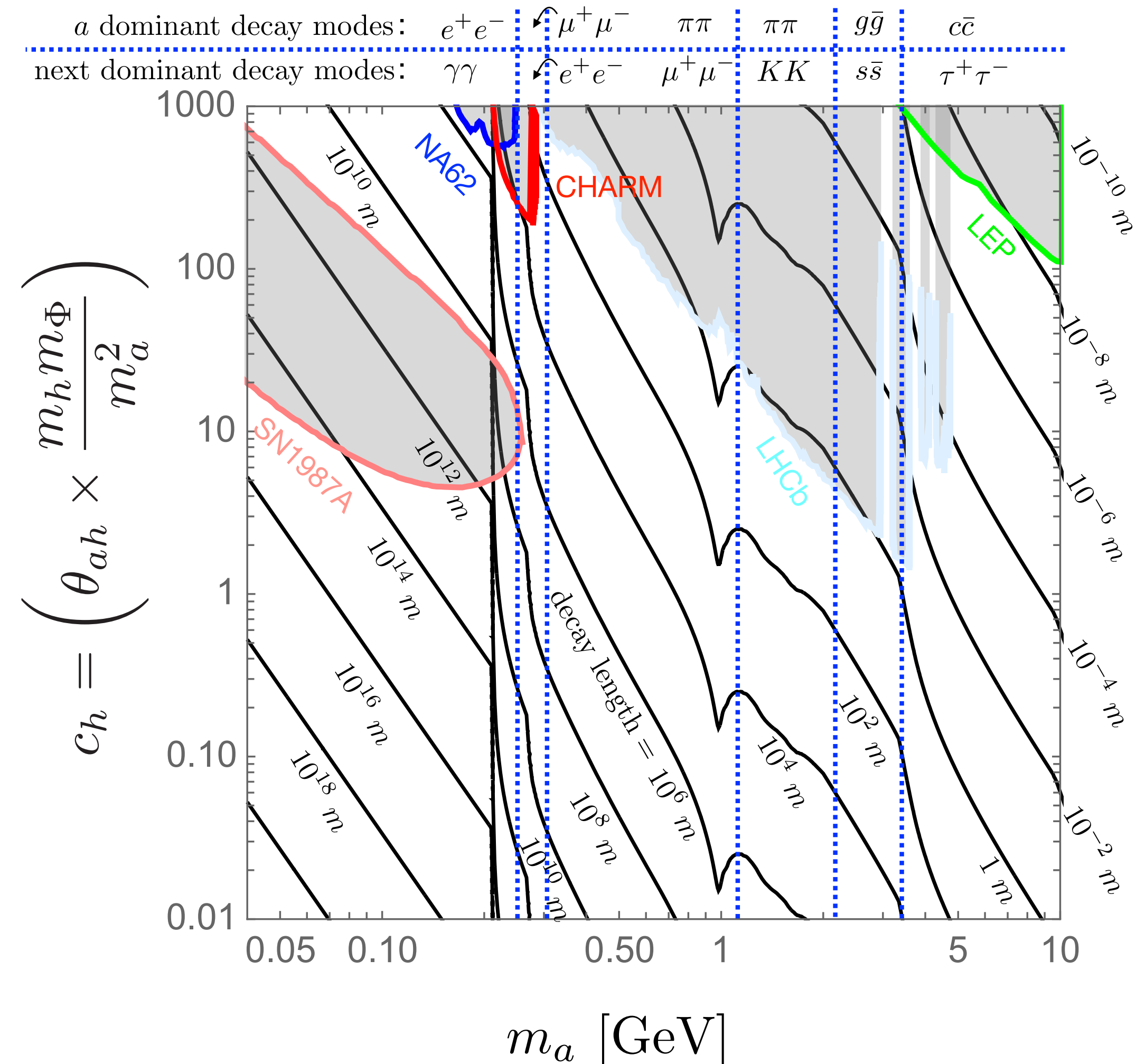
Visible particles

Probing CP-even ALP at e.g. ILC 250GeV

Kodai Sakurai, WY 2111.03653

Decay length and product of a from Higgs decay and signature at ILC

$$\mathcal{L}_{\text{eff}} \sim \frac{m_a^2 m_h}{m_\Phi} ah, \theta_{ah} \sim \frac{m_a^2}{m_h m_\Phi}$$



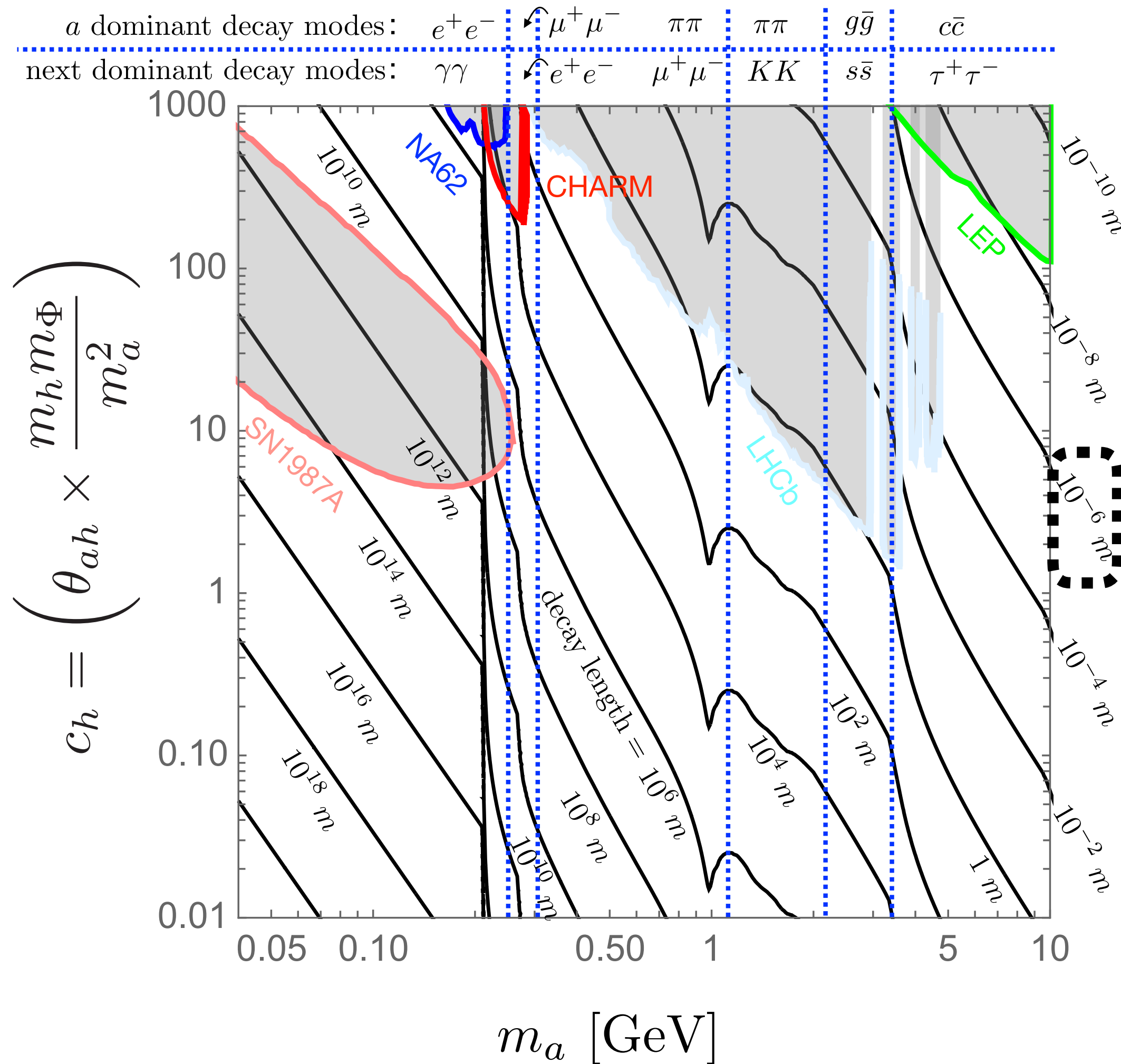
See also Bhattacharjee et al
2111.02437
for hadron collider reach
of CP-even light mediator

Probing CP-even ALP at e.g. ILC 250GeV

Kodai Sakurai, WY 2111.03653

Decay length and product of a from Higgs decay and signature at ILC

$$\mathcal{L}_{\text{eff}} \sim \frac{m_a^2 m_h}{m_\Phi} ah, \theta_{ah} \sim \frac{m_a^2}{m_h m_\Phi}$$



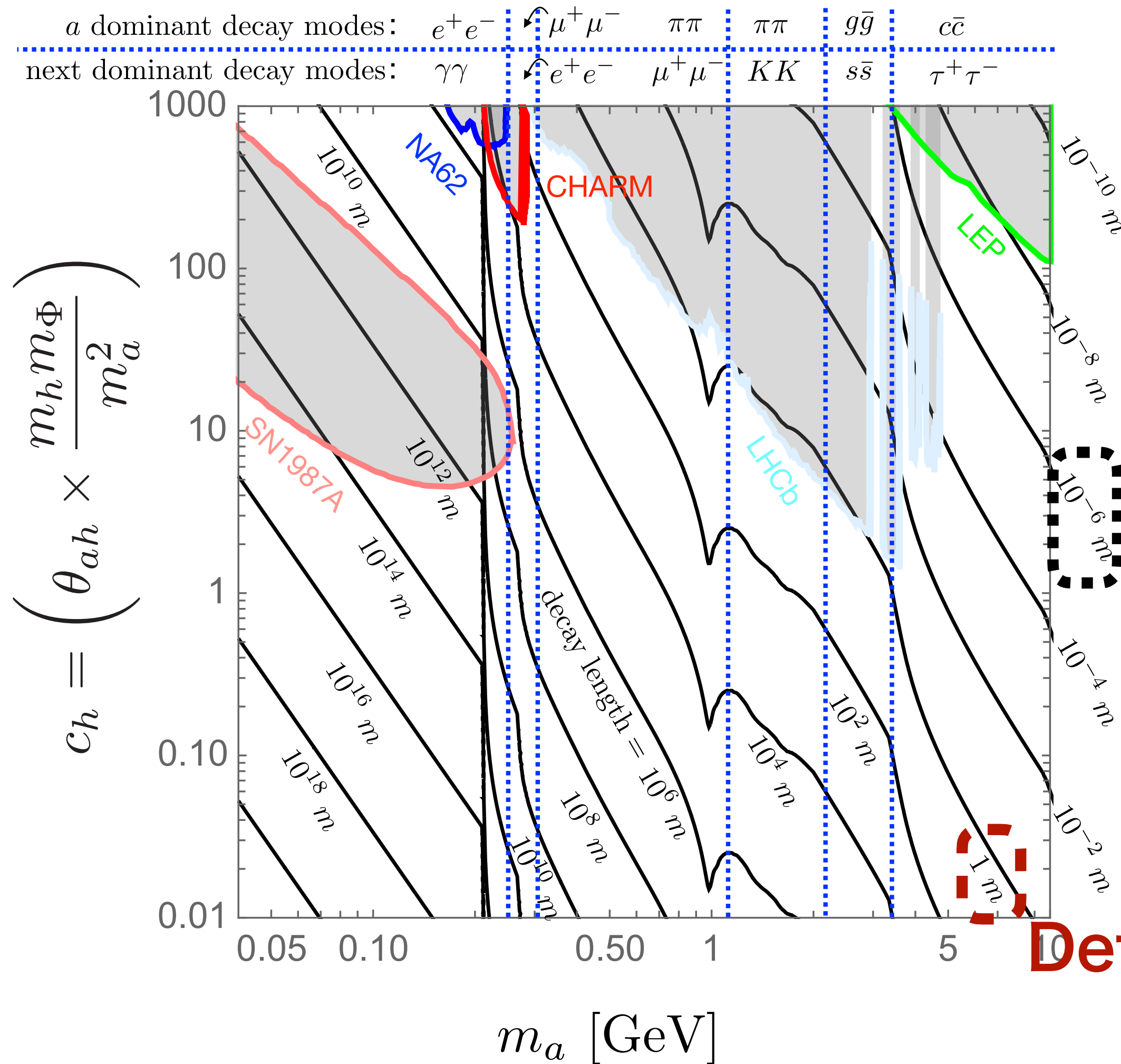
See also Bhattacharjee et al
2111.02437
for hadron collider reach
of CP-even light mediator

Probing CP-even ALP at e.g. ILC 250GeV

Kodai Sakurai, WY 2111.03653

Decay length and product of a from Higgs decay
and signature at ILC

$$\mathcal{L}_{\text{eff}} \sim \frac{m_a^2 m_h}{m_\Phi} ah, \theta_{ah} \sim \frac{m_a^2}{m_h m_\Phi}$$



Vertex resolution

Detector size (TPC)

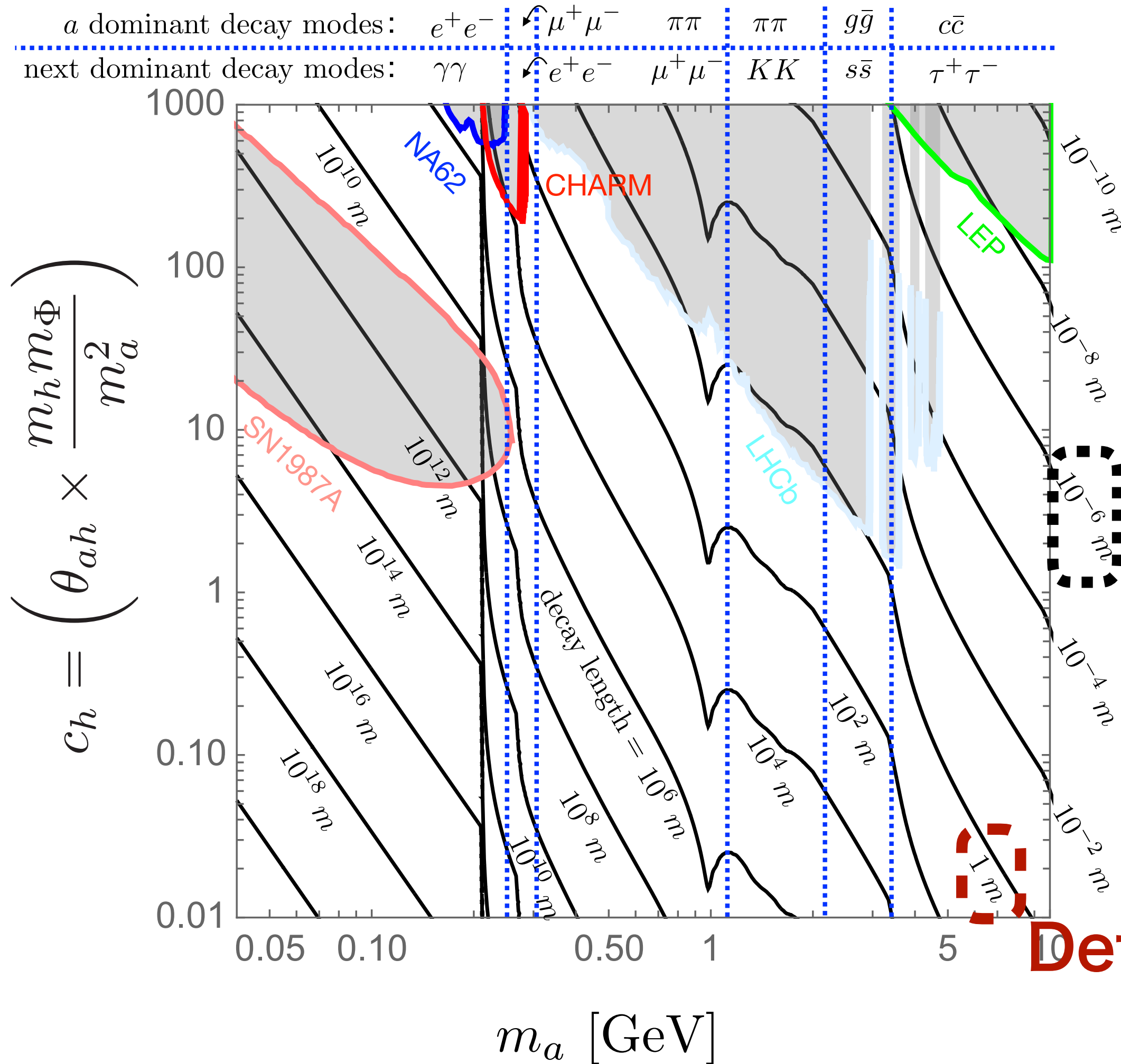
See also Bhattacharjee et al
2111.02437
for hadron collider reach
of CP-even light mediator

Probing CP-even ALP at e.g. ILC 250GeV

Kodai Sakurai, WY 2111.03653

Decay length and product of a from Higgs decay and signature at ILC

$$\mathcal{L}_{\text{eff}} \sim \frac{m_a^2 m_h}{m_\Phi} ah, \theta_{ah} \sim \frac{m_a^2}{m_h m_\Phi}$$



Higgs exotic decay

$$Br_{h \rightarrow aa(\rightarrow c\bar{c}c\bar{c})} \gtrsim 10^{-3} \text{ (} 2\sigma\text{CL, } 2 \text{ ab}^{-1}\text{)}$$

Liu et al, 1612.09284

Vertex resolution

Detector size (TPC)

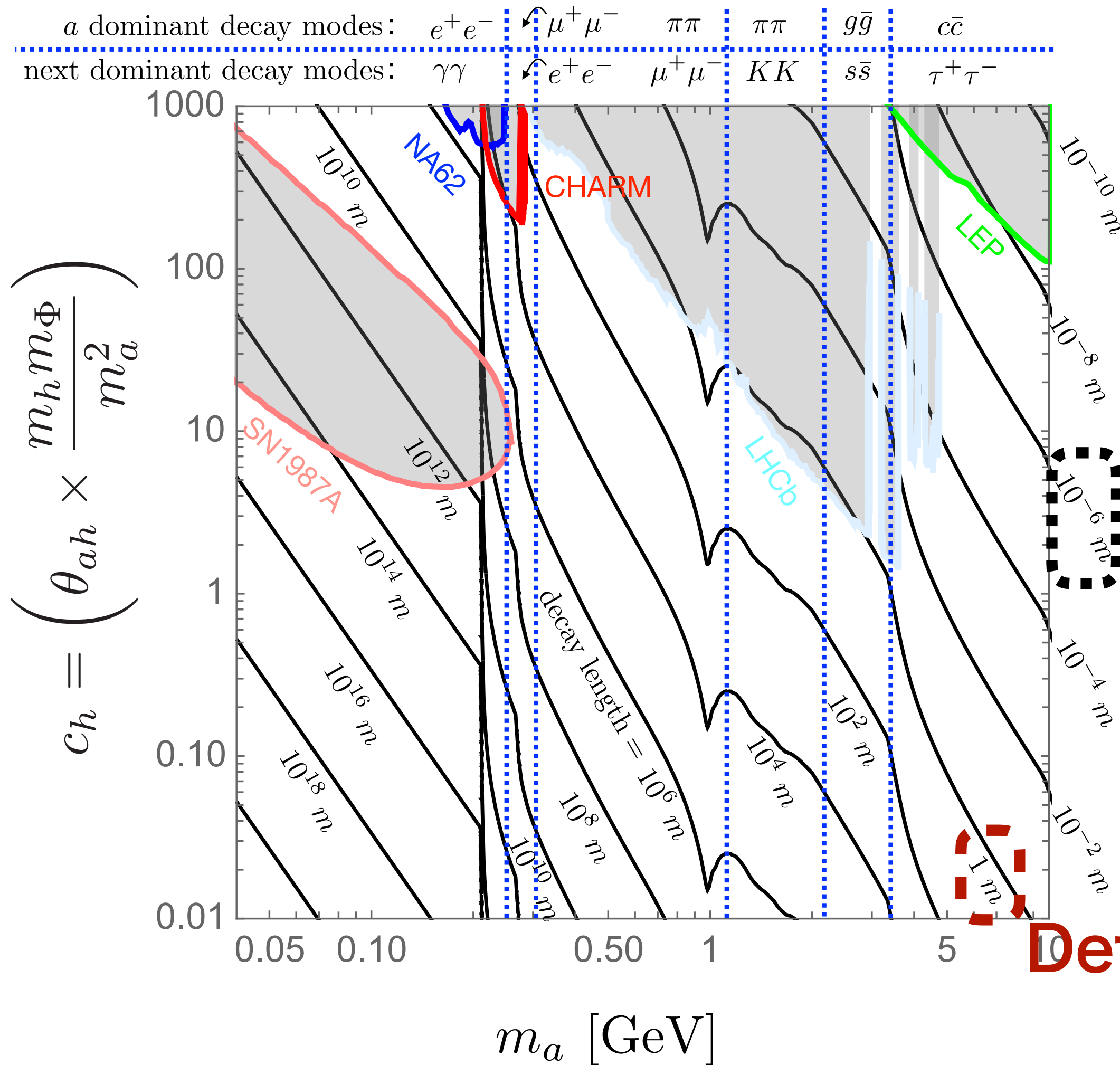
See also Bhattacharjee et al 2111.02437 for hadron collider reach of CP-even light mediator

Probing CP-even ALP at e.g. ILC 250GeV

Kodai Sakurai, WY 2111.03653

Decay length and product of a from Higgs decay and signature at ILC

$$\mathcal{L}_{\text{eff}} \sim \frac{m_a^2 m_h}{m_\Phi} ah, \theta_{ah} \sim \frac{m_a^2}{m_h m_\Phi}$$



Higgs exotic decay

$$Br_{h \rightarrow aa(\rightarrow c\bar{c}c\bar{c})} \gtrsim 10^{-3} \quad (2\sigma\text{CL}, 2 \text{ ab}^{-1})$$

Liu et al, 1612.09284

Vertex resolution

Displaced vertex $\times 2$

$$Br_{h \rightarrow aa} > 10^{-6}, \quad (2\sigma\text{CL}, 3 \text{ ab}^{-1})$$

Detector size (TPC)

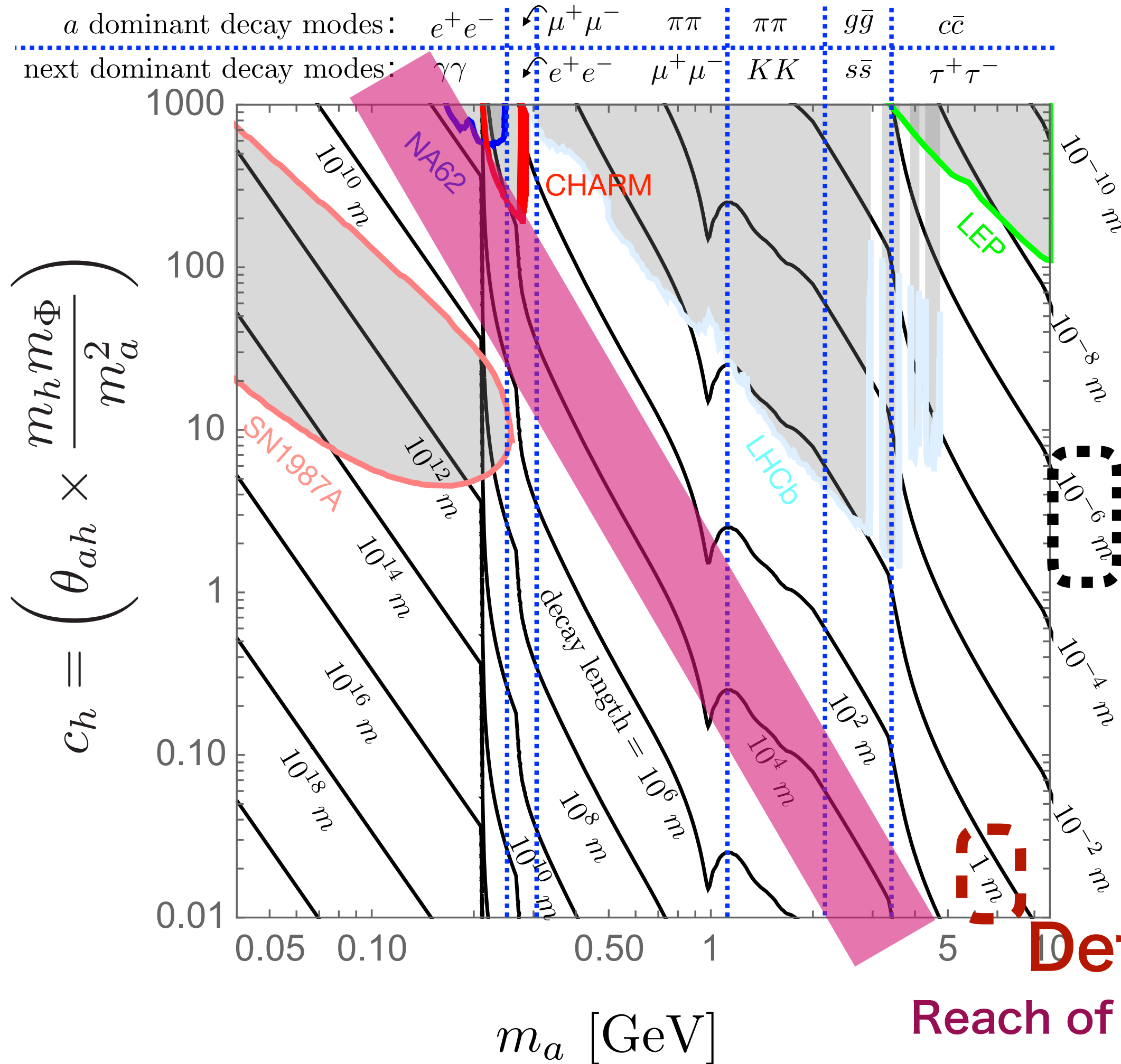
See also Bhattacharjee et al 2111.02437 for hadron collider reach of CP-even light mediator

Probing CP-even ALP at e.g. ILC 250GeV

Kodai Sakurai, WY 2111.03653

Decay length and product of a from Higgs decay and signature at ILC

$$\mathcal{L}_{\text{eff}} \sim \frac{m_a^2 m_h}{m_\Phi} ah, \theta_{ah} \sim \frac{m_a^2}{m_h m_\Phi}$$



Higgs exotic decay

$$Br_{h \rightarrow aa(\rightarrow c\bar{c}c\bar{c})} \gtrsim 10^{-3} \quad (2\sigma\text{CL}, 2 \text{ ab}^{-1})$$

Liu et al, 1612.09284

Vertex resolution

Displaced vertex $\times 2$

$$Br_{h \rightarrow aa} > 10^{-6}, \quad (2\sigma\text{CL}, 3 \text{ ab}^{-1})$$

Detector size (TPC)

Reach of rare displaced vertex
($Br_{h \rightarrow aa} \sim 1\%, 3 \text{ ab}^{-1}$)

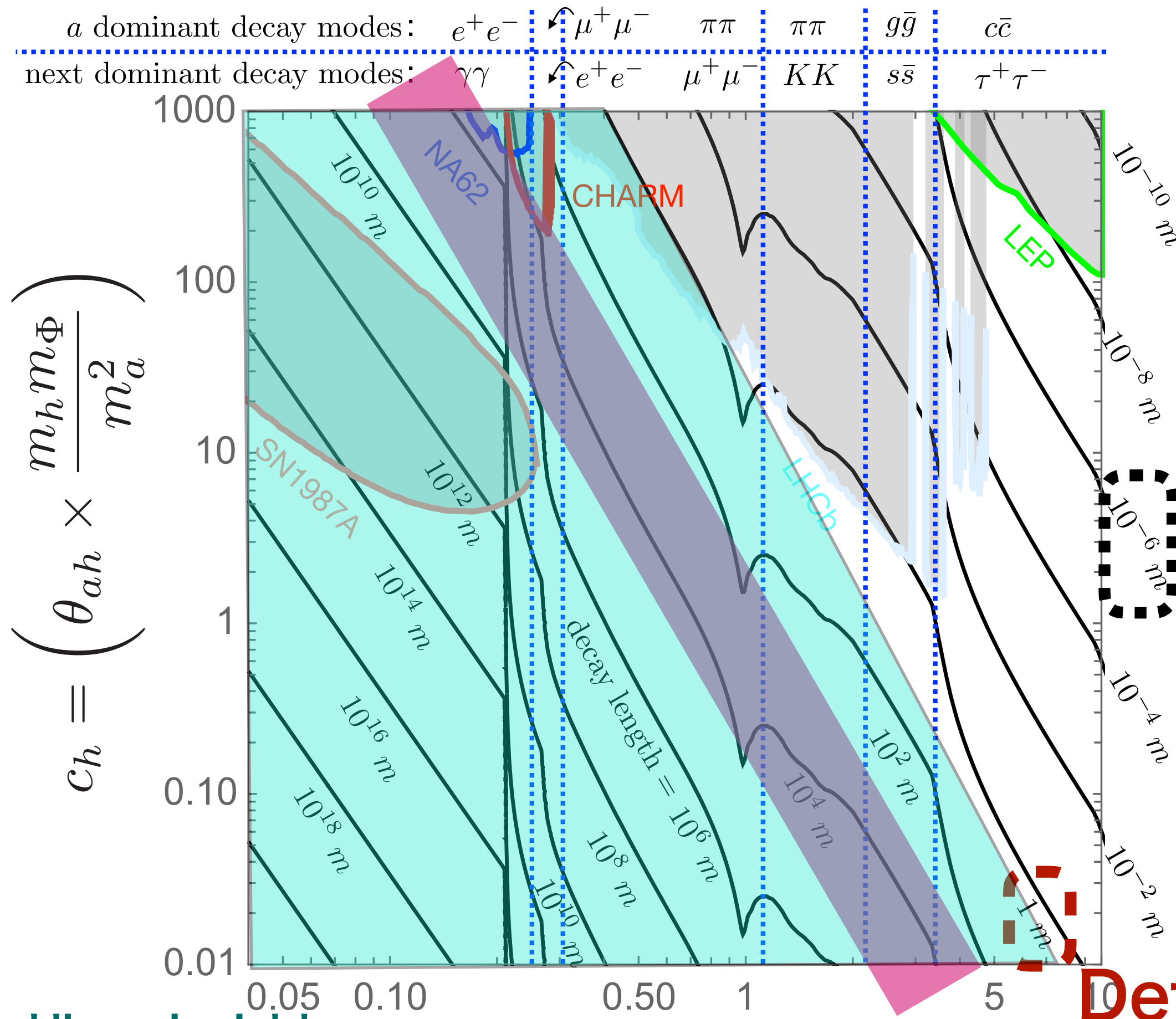
See also Bhattacharjee et al 2111.02437 for hadron collider reach of CP-even light mediator

Probing CP-even ALP at e.g. ILC 250GeV

Kodai Sakurai, WY 2111.03653

Decay length and product of a from Higgs decay and signature at ILC

$$\mathcal{L}_{\text{eff}} \sim \frac{m_a^2 m_h}{m_\Phi} ah, \theta_{ah} \sim \frac{m_a^2}{m_h m_\Phi}$$



Higgs exotic decay

$$Br_{h \rightarrow aa(\rightarrow c\bar{c}c\bar{c})} \gtrsim 10^{-3} \quad (2\sigma\text{CL}, 2 \text{ ab}^{-1})$$

Liu et al, 1612.09284

Vertex resolution

Displaced vertex $\times 2$

$$Br_{h \rightarrow aa} > 10^{-6}, \quad (2\sigma\text{CL}, 3 \text{ ab}^{-1})$$

Detector size (TPC)

Reach of rare displaced vertex

$$(Br_{h \rightarrow aa} \sim 1\%, 3 \text{ ab}^{-1})$$

See also Bhattacharjee et al 2111.02437 for hadron collider reach of CP-even light mediator

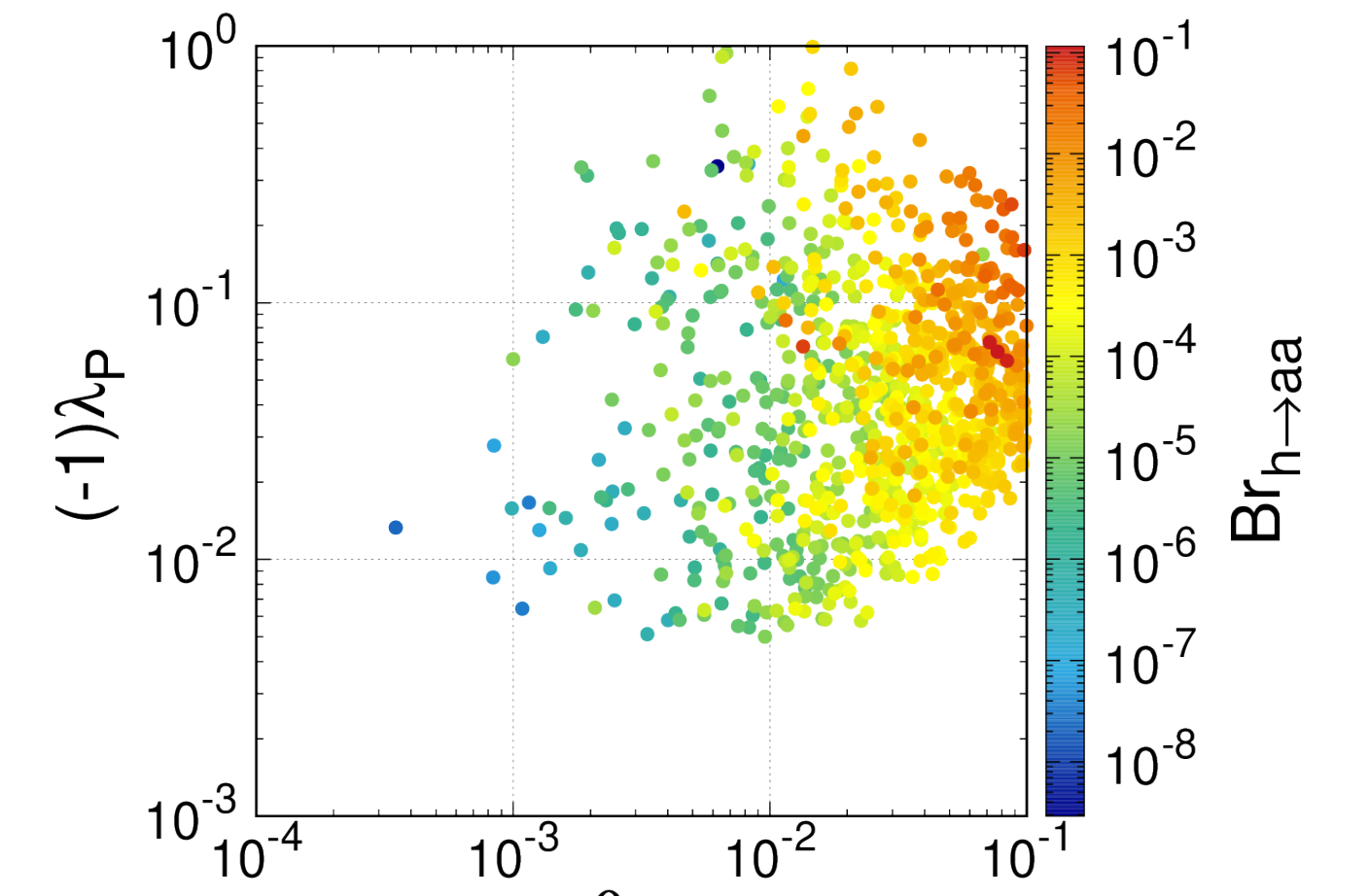
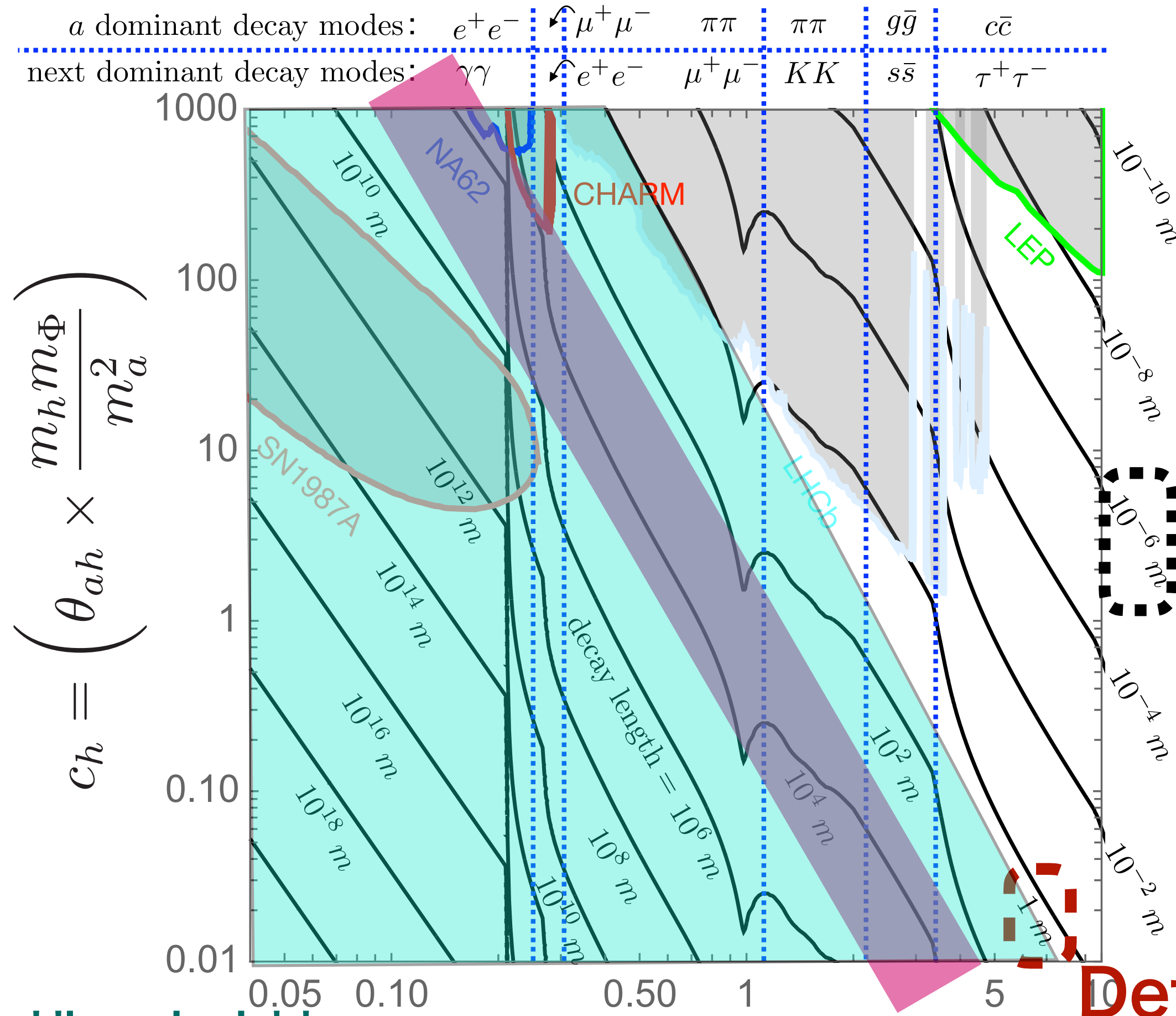
Higgs invisible

$$\text{decay } Br_{h \rightarrow aa} \gtrsim 0.1\% \quad m_a [\text{GeV}] \quad \text{ILC whitepaper}$$

Probing CP-even ALP at e.g. ILC 250GeV

Decay length and product of a from Higgs decay and signature at ILC

Kodai Sakurai, WY 2111.03653



Higgs exotic decay

$$Br_{h \rightarrow aa(\rightarrow c\bar{c}c\bar{c})} \gtrsim 10^{-3} \quad (2\sigma\text{CL}, 2 \text{ ab}^{-1})$$

Liu et al, 1612.09284

Vertex resolution

Displaced vertex $\times 2$

$$Br_{h \rightarrow aa} \gtrsim 10^{-6}, \quad (2\sigma\text{CL}, 3 \text{ ab}^{-1})$$

Detector size (TPC)

Reach of rare displaced vertex

$$(Br_{h \rightarrow aa} \sim 1\%, 3 \text{ ab}^{-1})$$

See also Bhattacharjee et al 2111.02437 for hadron collider reach of CP-even light mediator

Higgs invisible

decay $Br_{h \rightarrow aa} \gtrsim 0.1\% \quad m_a [\text{GeV}]$ ILC whitepaper

What roles does CP-even ALP play in the early Universe?

- Light mediator to DM with $\mathcal{L} \supset \Phi \bar{\Psi}_{\text{DM}}^c \Psi_{\text{DM}}$.

ALP couples SM fermion weakly but strongly with DM, which is the desired property of a light mediator.

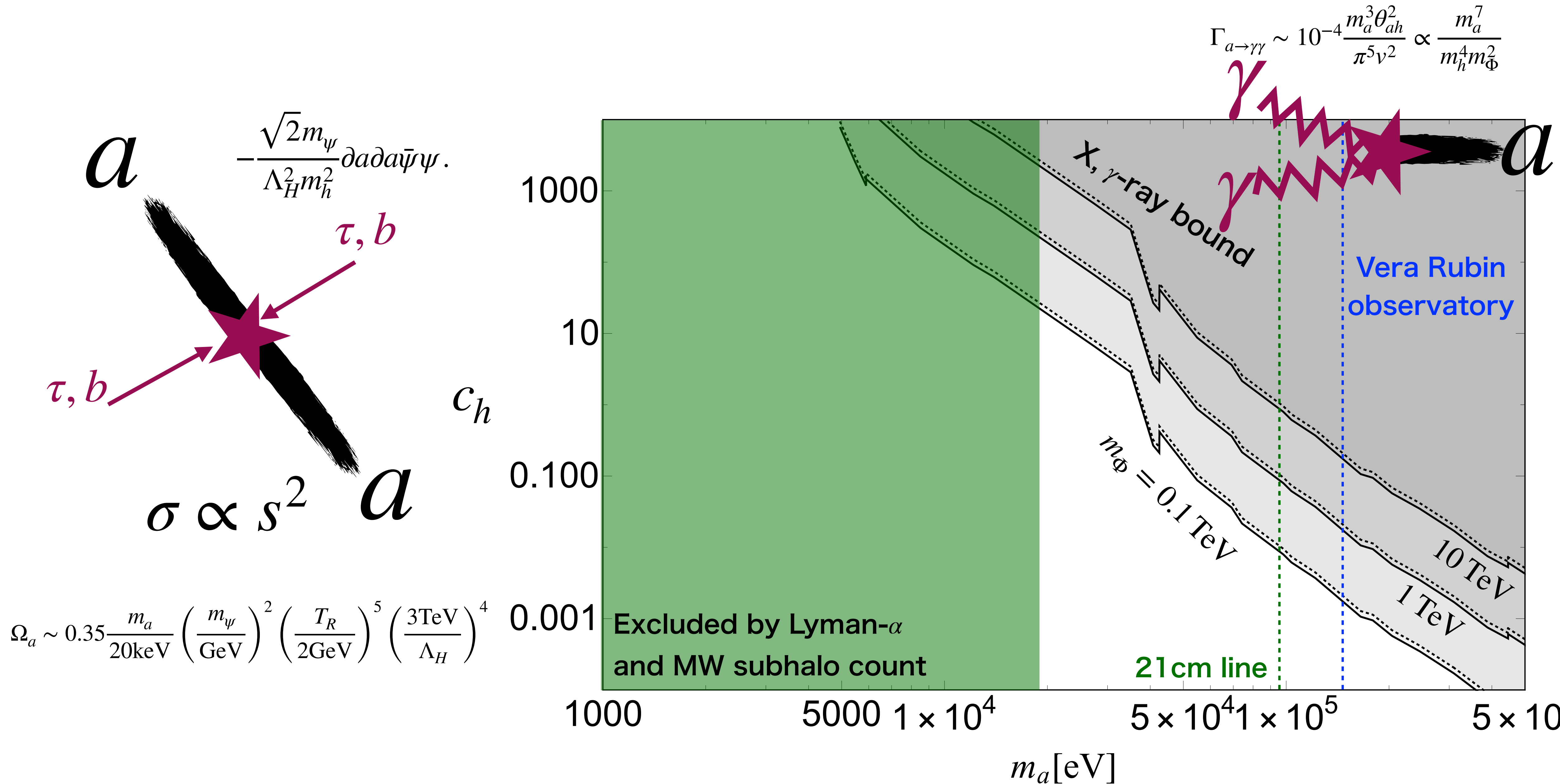
Please study it with WIMP, which should be an interesting topic!

- **CP-even ALP DM.** This talk.

CP-even ALP is a good DM candidate if it is lighter than MeV.

$$\Gamma_{a \rightarrow \gamma\gamma} \sim 10^{-4} \frac{m_a^3 \theta_{ah}^2}{\pi^5 v^2} \propto \frac{m_a^7}{m_h^4 m_\Phi^2}$$

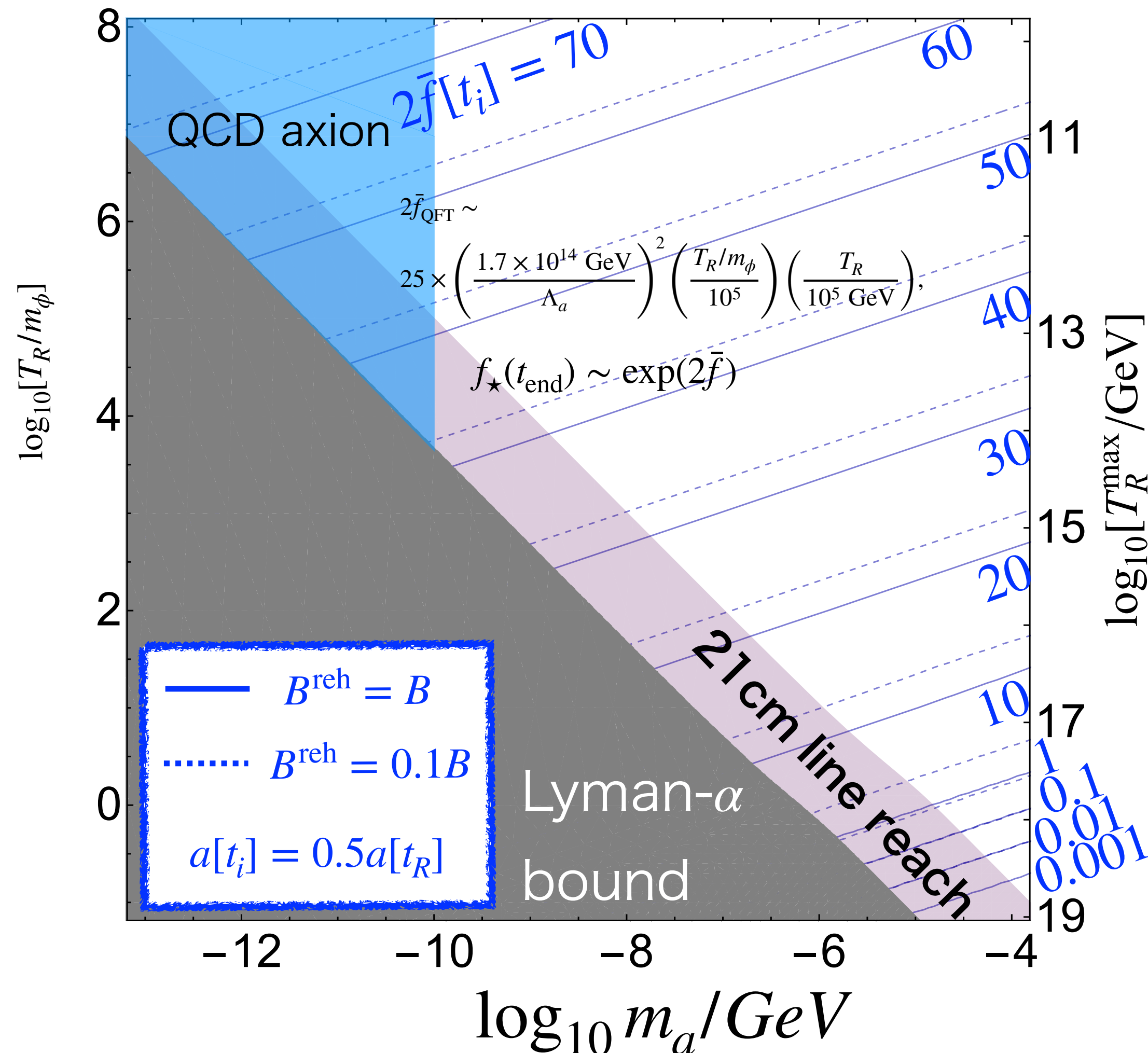
Thermally produced CP-even ALP DM



Non-thermal production scenario: lighter mass range.

Light bosonic DM can be produced during reheating if $T_R > m_{\text{inflaton}}$ as laser.

Moroi, WY, 2011.09475, 2011.12285

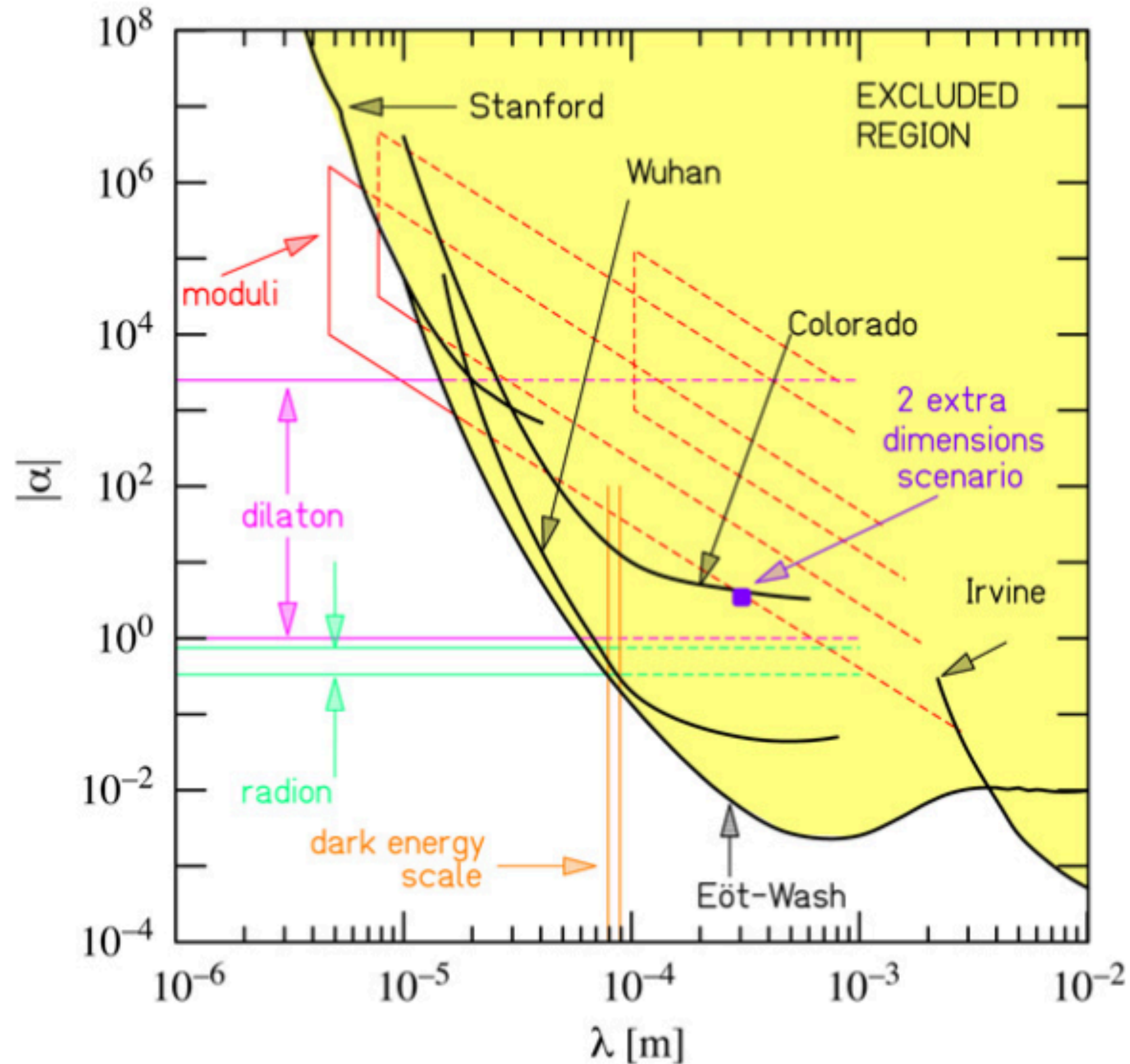


$$\mathcal{L}_{\text{int}} = \frac{\phi}{\Lambda_a} \partial_\mu a \partial^\mu a + \frac{\phi}{\Lambda_G} G_{\mu\nu}^{(a)} G^{(a)\mu\nu}$$

For CP-even ALP, we need $T_R \ll m_\Phi$ for the produced ALP not to be thermalized. Probed by inflaton search, 21 cm line.

Does fifth force search kills the CP even ALP DM with $m_a < 10^{-3} eV$?

$$\alpha \sim \theta_{ah}^2 \frac{M_{pl}^2}{v^2} \sim 10^{-27} \left(\frac{3 \text{TeV}}{m_\Phi} \right)^2 \left(\frac{m_a}{10^{-3} eV} \right)^4$$



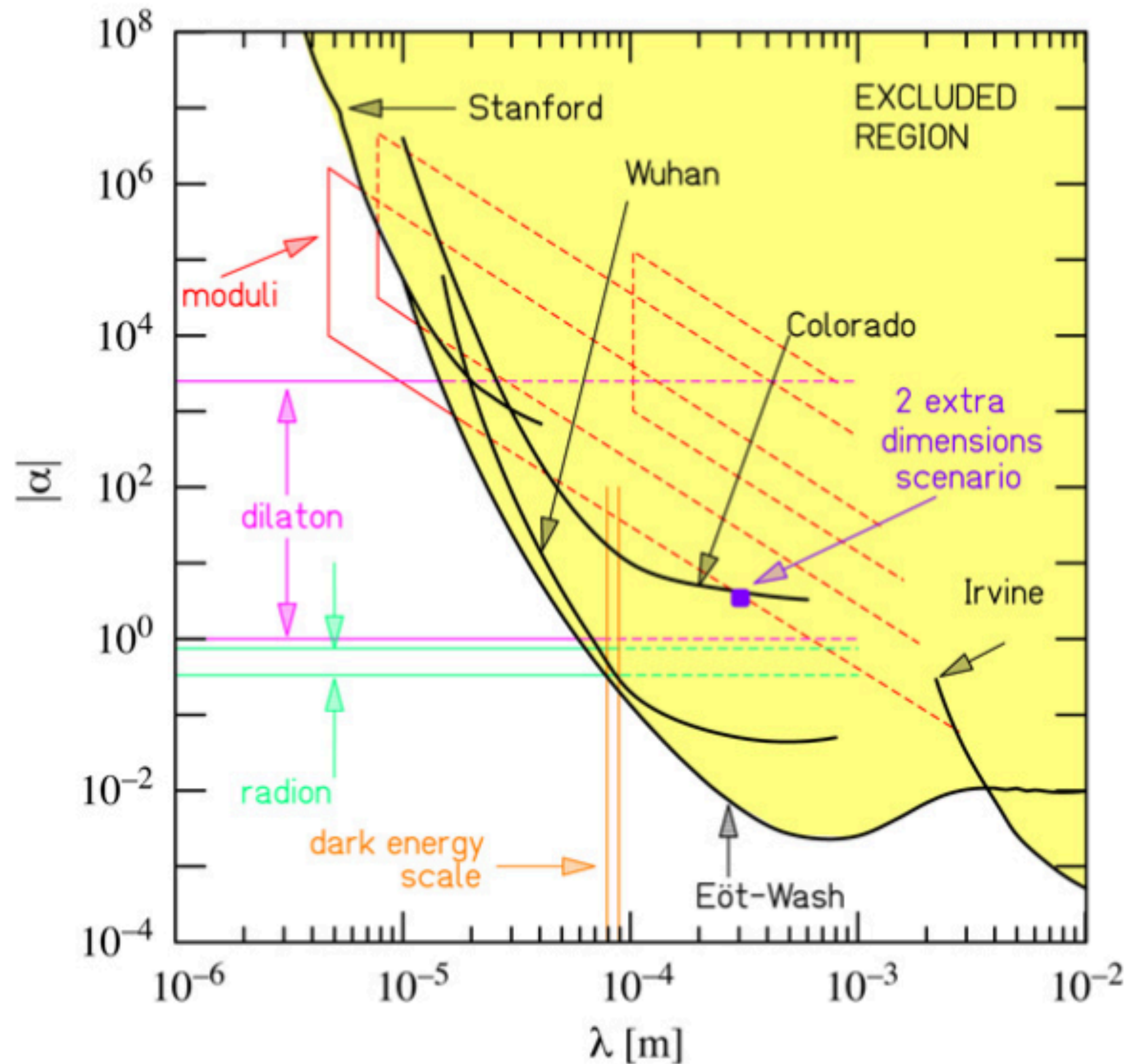
$$V = -G_N \frac{m_1 m_2}{r} (1 + \alpha e^{-r/\lambda})$$

$$\lambda \sim 2 \times 10^{-4} m \frac{10^{-3} eV}{m_\phi}$$

Does fifth force search kills the CP even ALP DM with $m_a < 10^{-3} eV$?

$$\alpha \sim \theta_{ah}^2 \frac{M_{pl}^2}{v^2} \sim 10^{-27} \left(\frac{3 \text{TeV}}{m_\Phi} \right)^2 \left(\frac{m_a}{10^{-3} eV} \right)^4$$

No, totally safe.

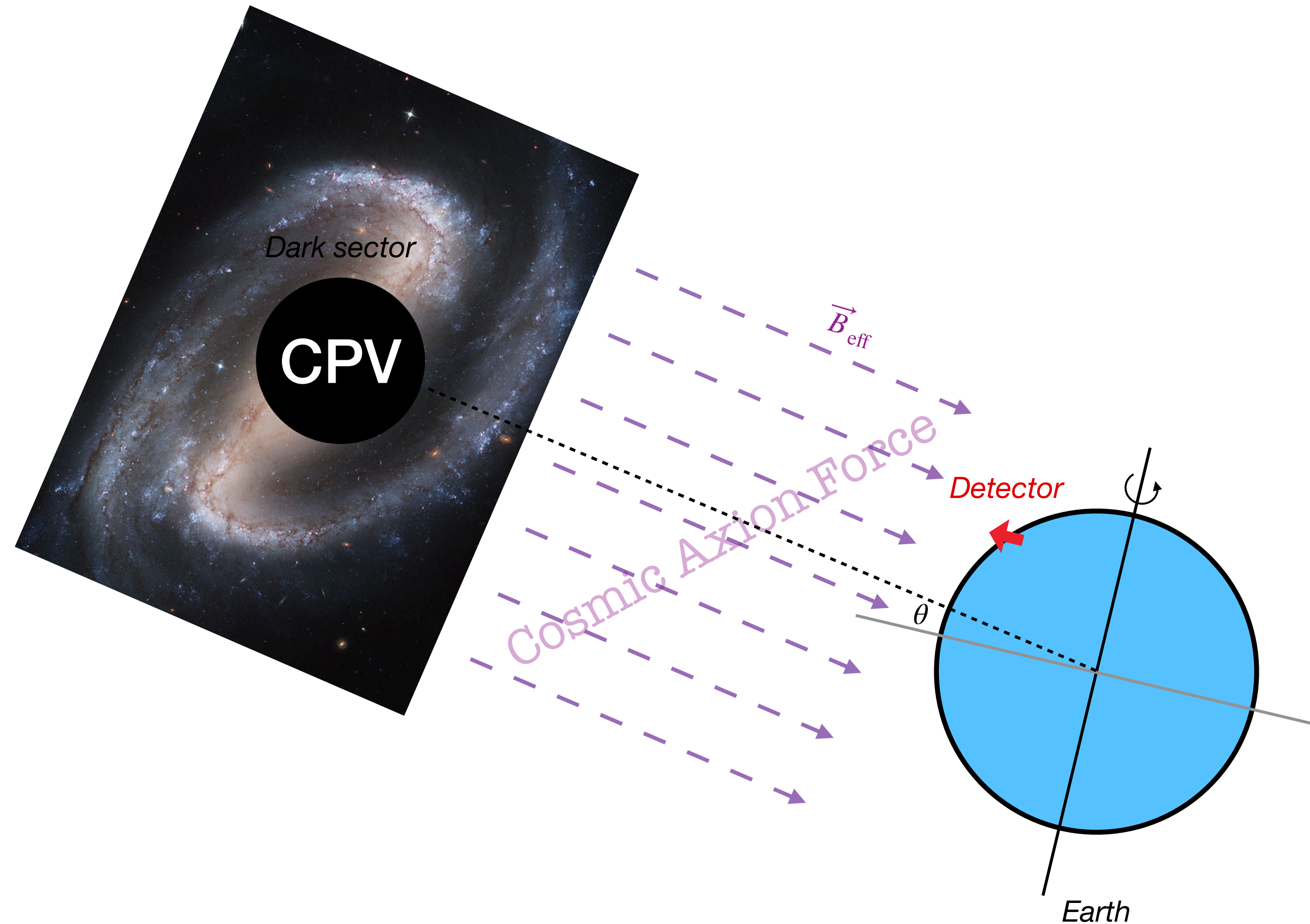


$$V = -G_N \frac{m_1 m_2}{r} (1 + \alpha e^{-r/\lambda})$$

$$\lambda \sim 2 \times 10^{-4} m \frac{10^{-3} eV}{m_\phi}$$

**Difficult to test it at low energy,
but it is probed by the Higgs invisible decay!**

4. Cosmic axion force from ultra-light ALP



Motivation for ultra-light ALP

- **Axiverse** [Witten 1984](#), [Arvanitaki et al 0905.4720](#), see also [Kitano](#), and [WY 2103.08598](#) for a simplified QCD axion model.

e.g. if SUSY scale is high, an M-theory compactification predicts

axion coupled to photons with mass [Acharya, et al 1004.5138](#), see also [Marsh WY, 1912.08188](#);

$$m_\phi^2 f_\phi^2 \sim M_{\text{pl}}^4 \exp(-2\pi/\alpha_{Y,2}) \sim e^{-O(1000)} \text{GeV}^4$$

• Axionic relaxation of cosmological constant

- Relaxing CC around today, [Abbott 1985](#); [Banks 1984](#), but predicts empty Universe.
- Possibility of reheating the Universe after a bounce [Graham et al 1902.06793](#),
- Relaxation during inflation with a peculiar inflaton potential [WY, 2108.04246](#)

In any case

$$m_\phi \lesssim H_0 \sim 10^{-42} \text{ GeV}$$

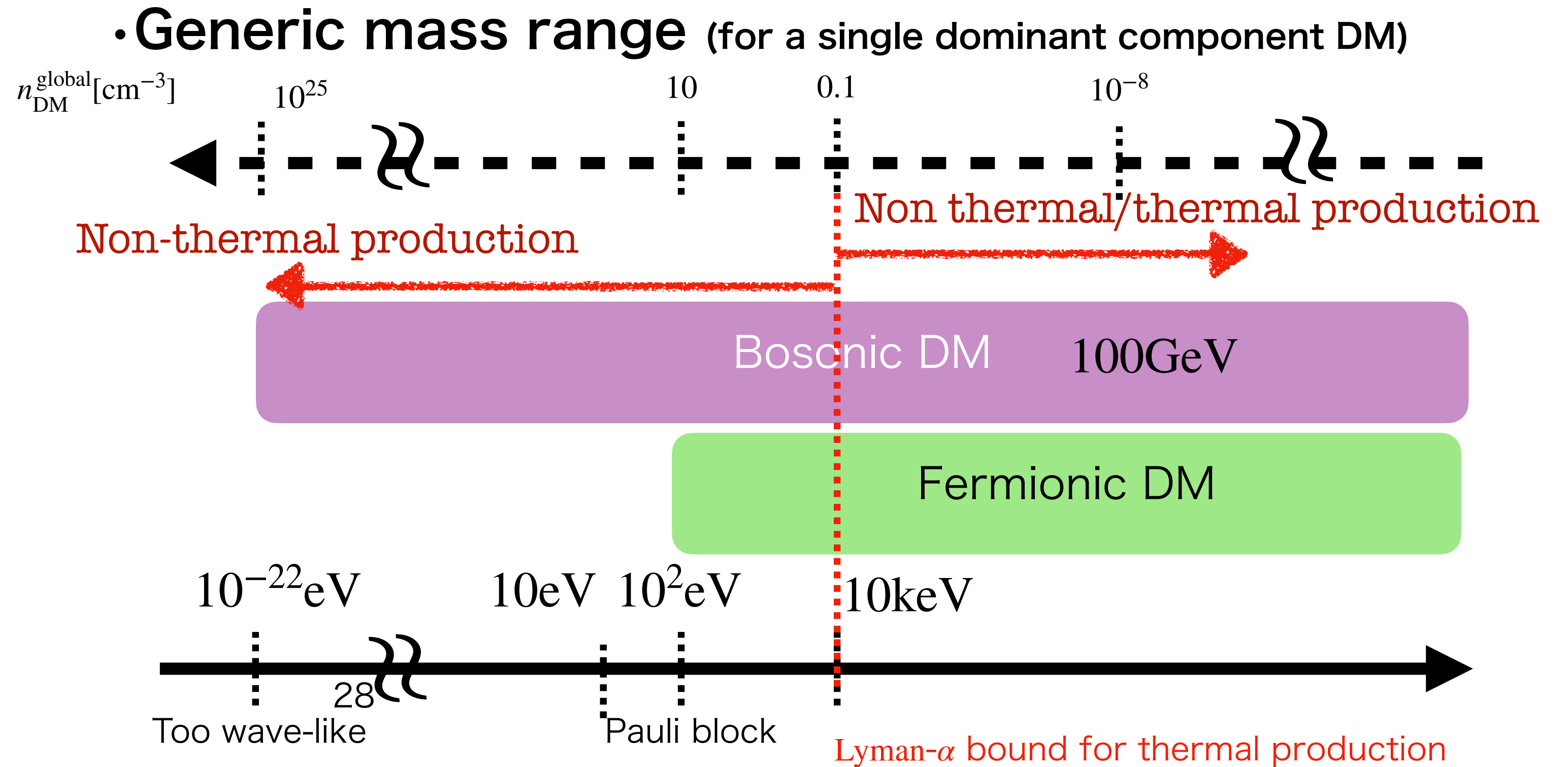
• Cosmic birefringence

- Parity violation of CMB photon propagation, [Minami and Komatsu, 2011.11254](#);
[See also Clark et al, 2105.00120](#) for discussion on dust.
- Time-varying ALP explanation [Minami and Komatsu, 2011.11254](#), [Fujita et al, 2011.11894](#), (CB and H_0 tension) etc

$$m_\phi \lesssim 10^{-27} \text{ eV}$$

- Spatially varying ALP explanation, ALP domain wall [Takahashi, WY, 2012.11576](#) $m_\phi \lesssim 10^{-17} \text{ eV}$

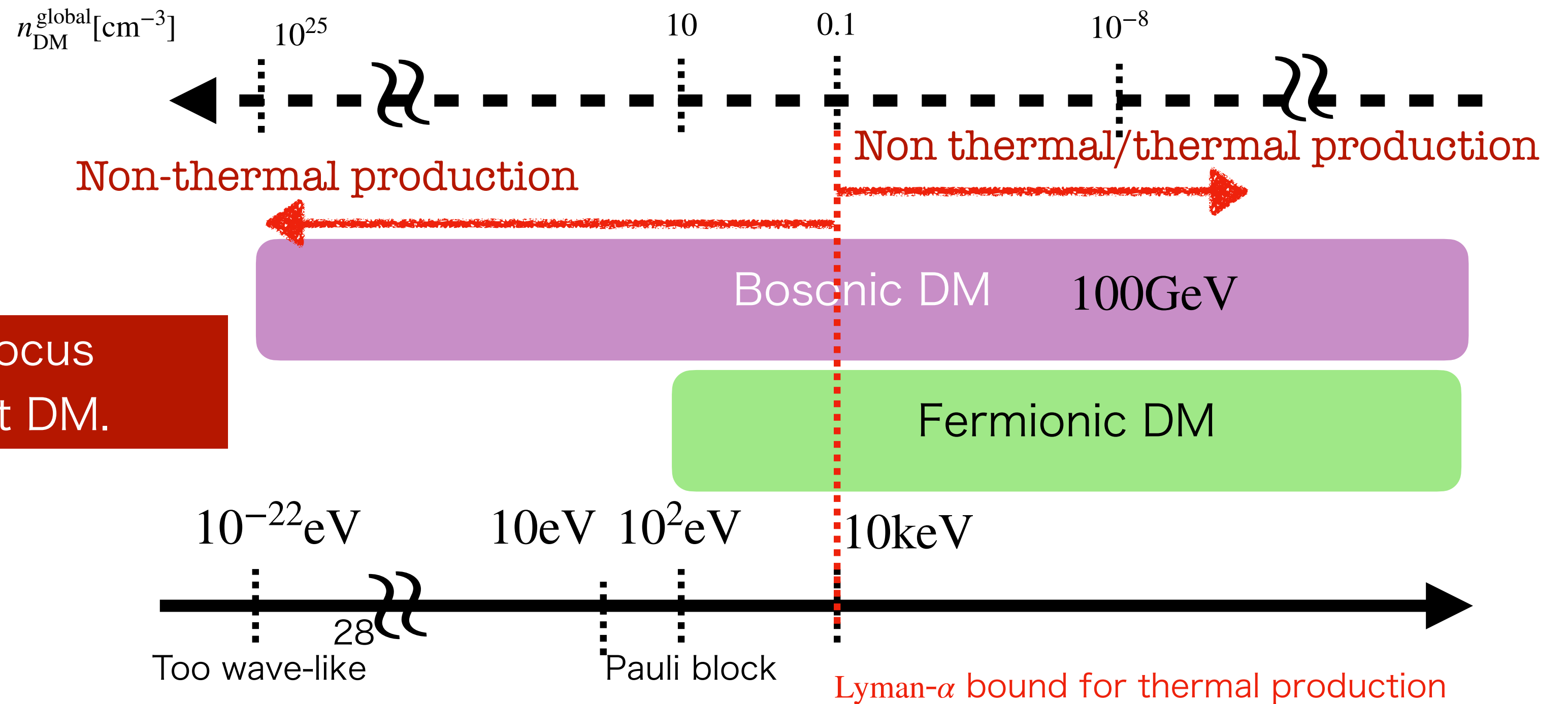
→ Ultra-light ALP+SM+DM



Ultra-light ALP may couple to DM.

→ Ultra-light ALP+SM+DM

• Generic mass range (for a single dominant component DM)



Ultra-light ALP which is our focus which cannot be the dominant DM.

Ultra-light ALP may couple to DM.

DM-ALP interaction is easily CPV.

ALP DM a + ultralight ALP ϕ

$$V = -\Lambda^4 \left(\kappa_1 \cos\left(n_a \frac{a}{f_a}\right) + \kappa_2 \cos\left(\frac{\phi}{f_\phi} + \frac{a}{f_a}\right) + \kappa_3 \cos\left(n_\phi \frac{\phi}{f_\phi}\right) \right) \quad (34)$$

with $\kappa_1 \gtrsim \kappa_2, \kappa_3, n_a > 1$ then we can integrate out a who has local minima $\langle a \rangle / f_a \approx 0, 2\pi/n_a, 4\pi/n_a \dots (n_a - 1)2\pi/n_a$. The mass of a is

$$m_a^2 \sim \kappa_1 \frac{n_a^2 \Lambda^4}{f_a^2} \quad (35)$$

$$V_{\text{eff}} \simeq -\Lambda^4 \left(\kappa_2 \cos\left(\theta + \frac{\phi}{f_\phi}\right) + \kappa_3 \cos\left(n_\phi \frac{\phi}{f_\phi}\right) \right) \quad \theta = \langle a/f_a \rangle$$

$$V \supset \frac{A_a}{2} \delta a^2 \delta \phi$$

$$A_a \simeq \theta \frac{\kappa_2 \kappa_3 n^2}{\kappa_2 + \kappa_3 n^2} \frac{\Lambda^4}{f_a^2 f_\phi} + \mathcal{O}(\theta^3) \equiv \epsilon_a \frac{m_a^2}{f_\phi}.$$

Dark nucleon DM+ ultralight ALP ϕ

$$\mathcal{L} \supset g_{\phi N' N'}^{\text{CPV}} \phi \bar{N}' N'$$

$$g_{\phi N' N'}^{\text{CPV}} \sim \frac{\theta_{\text{darkCP}}}{f_\phi} \frac{2m_{u'} m_{d'}}{(m_{u'} + m_{d'})^2} \langle N' | \sigma | N' \rangle$$

$$\equiv \epsilon_{\text{CPV}} \frac{m_{N'}}{f_\phi}$$

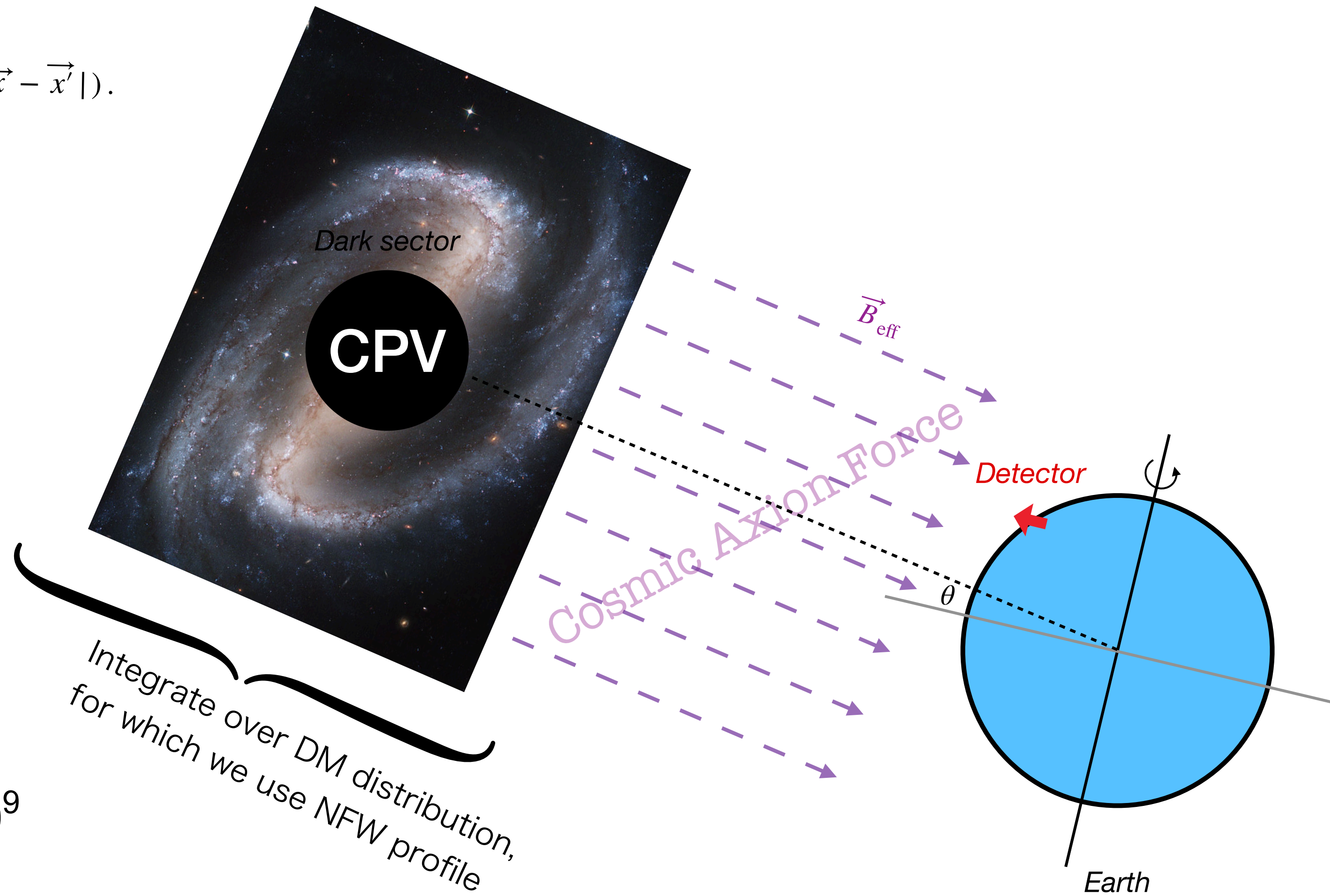
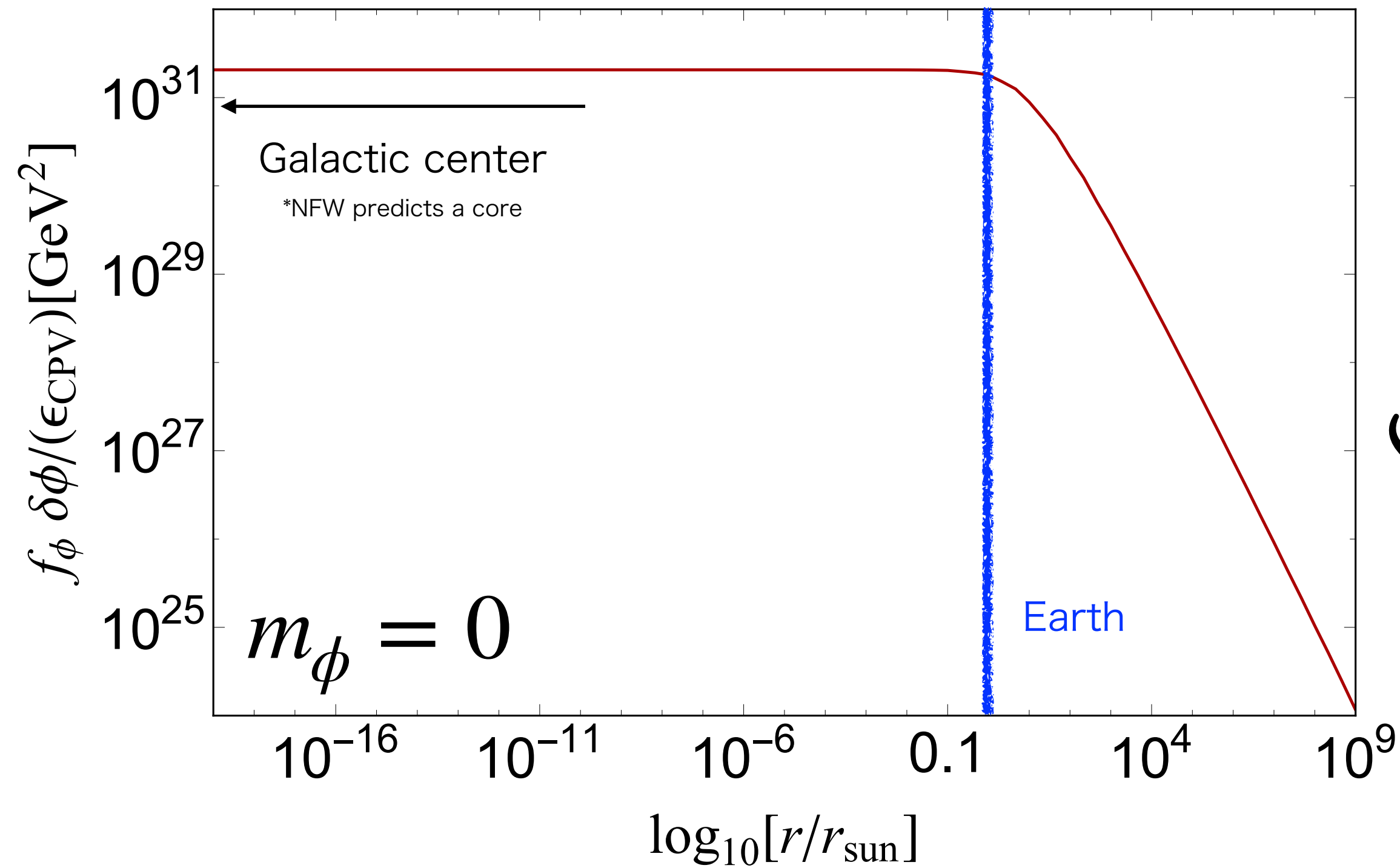
If dark QCD does not have the strong CP problem, $\theta_{\text{darkCP}} = \mathcal{O}(1)$ and $\epsilon_{\text{CPV}} = \mathcal{O}(1)$.

Ultra-light ALP mediates long range force from DM!

Cosmic axion force from DM

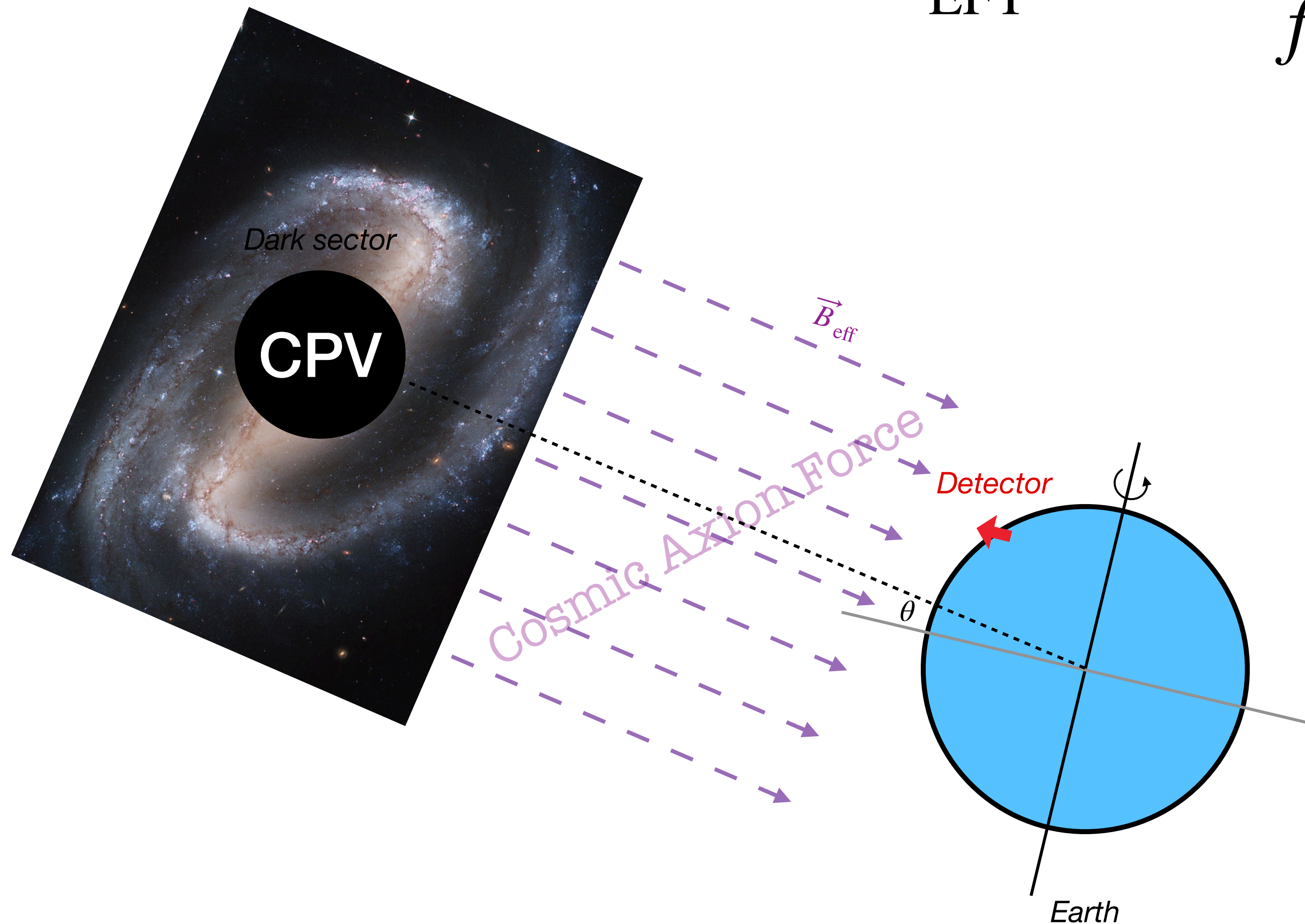
From $(\partial_t^2 - \nabla^2)\delta\phi(t, \vec{x}) = -m_\phi^2\delta\phi(t, \vec{x}) - J(t, \vec{x})$,

$$\delta\phi^{\text{ps}} \sim \epsilon_{\text{CPV}} \frac{m_{\text{DM}}}{4\pi f_\phi r} \exp(-m_\phi r) \quad \delta\phi(t, \vec{x}) \approx \int d^3\vec{x}' n_{\text{DM}}(x') \delta\phi^{\text{ps}}(t, |\vec{x} - \vec{x}'|).$$



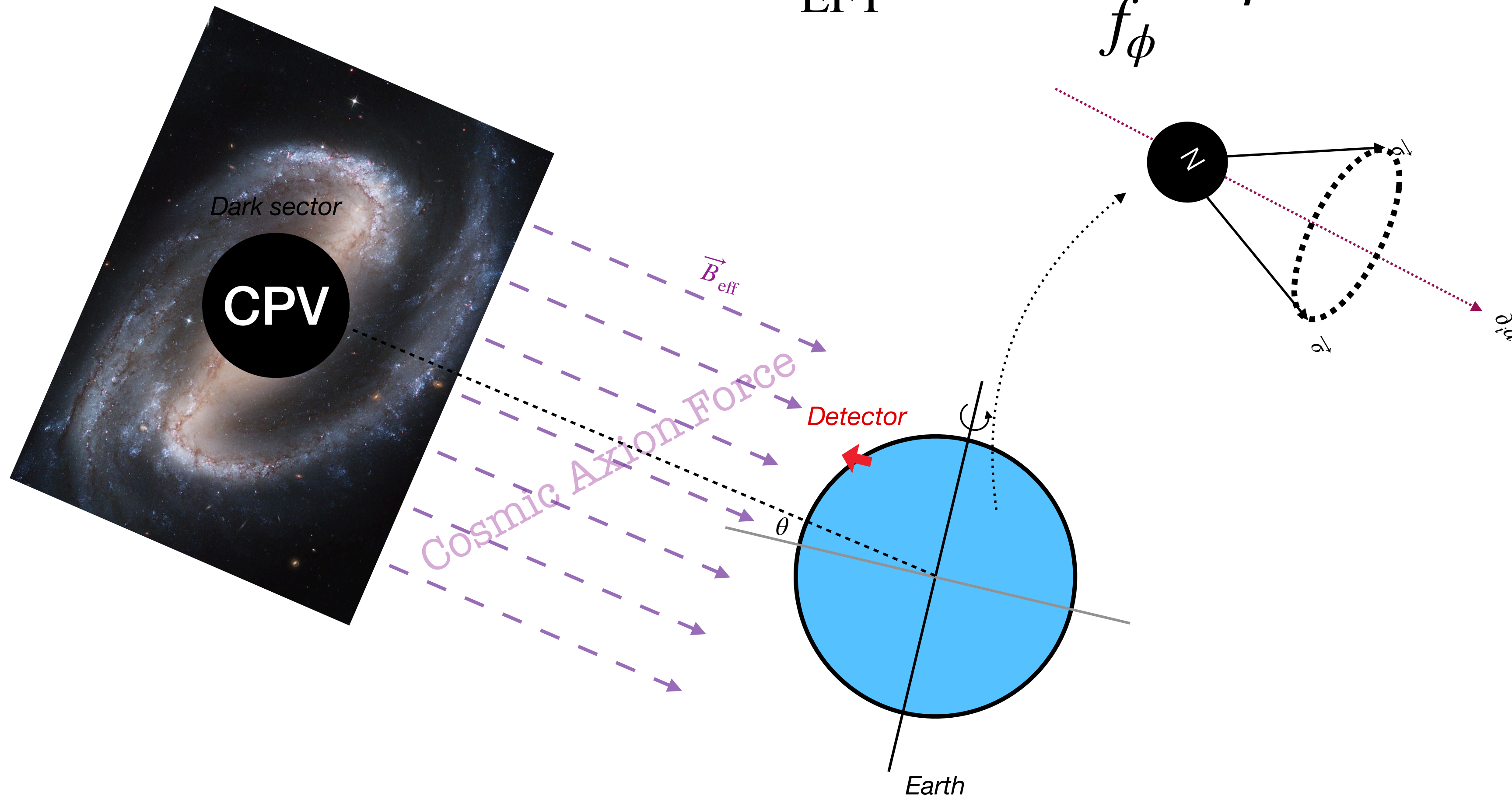
Spin precession towards galactic center everywhere on Earth!

$$H_{\text{EFT}}^{\text{nonrela}} \simeq -\frac{c_N}{f_\phi} \vec{\partial} \phi \cdot \bar{N} \vec{\sigma} N.$$



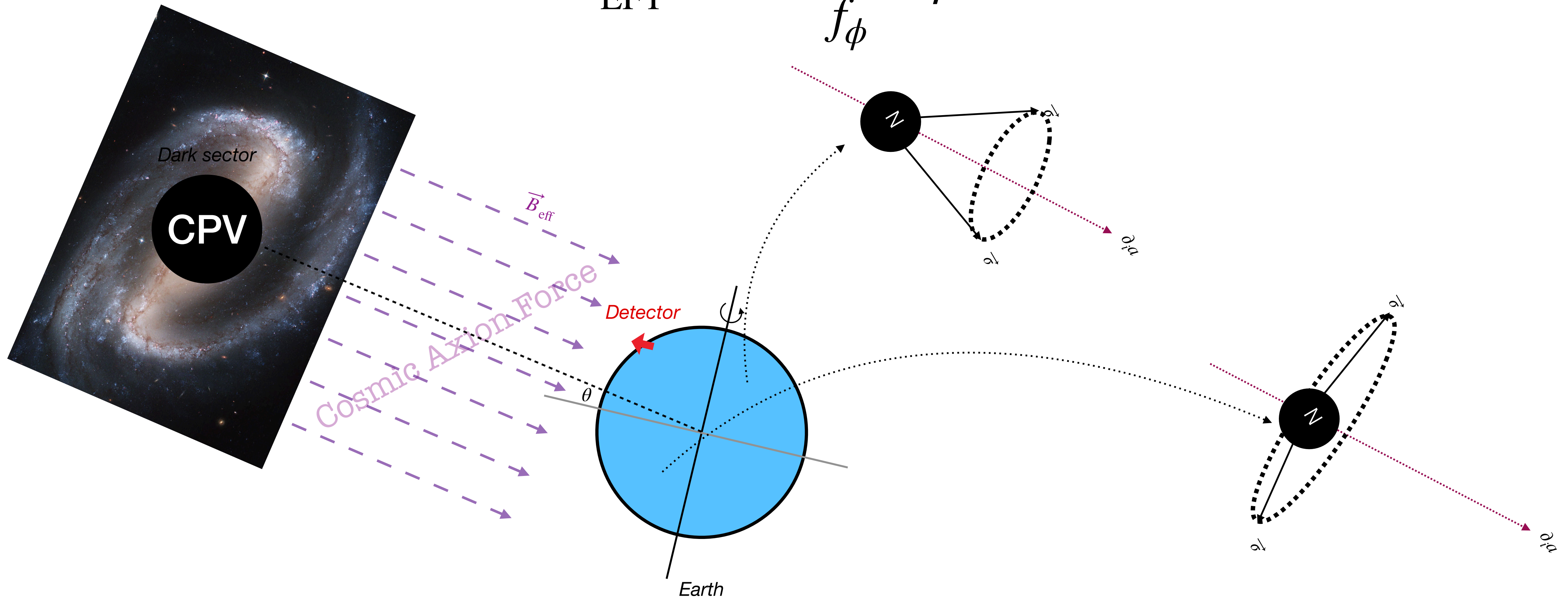
Spin precession towards galactic center everywhere on Earth!

$$H_{\text{EFT}}^{\text{nonrela}} \simeq -\frac{c_N}{f_\phi} \vec{\partial} \phi \cdot \bar{N} \vec{\sigma} N.$$



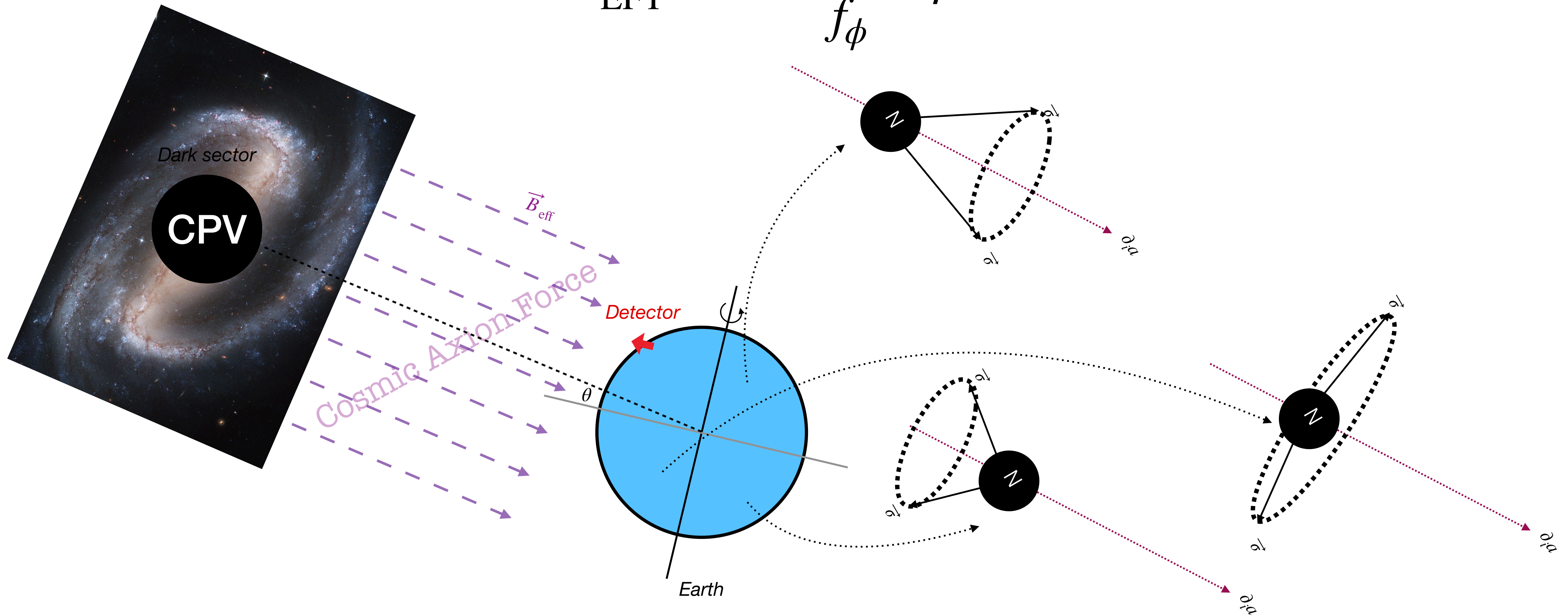
Spin precession towards galactic center everywhere on Earth!

$$H_{\text{EFT}}^{\text{nonrela}} \simeq -\frac{c_N}{f_\phi} \vec{\partial} \phi \cdot \bar{N} \vec{\sigma} N.$$



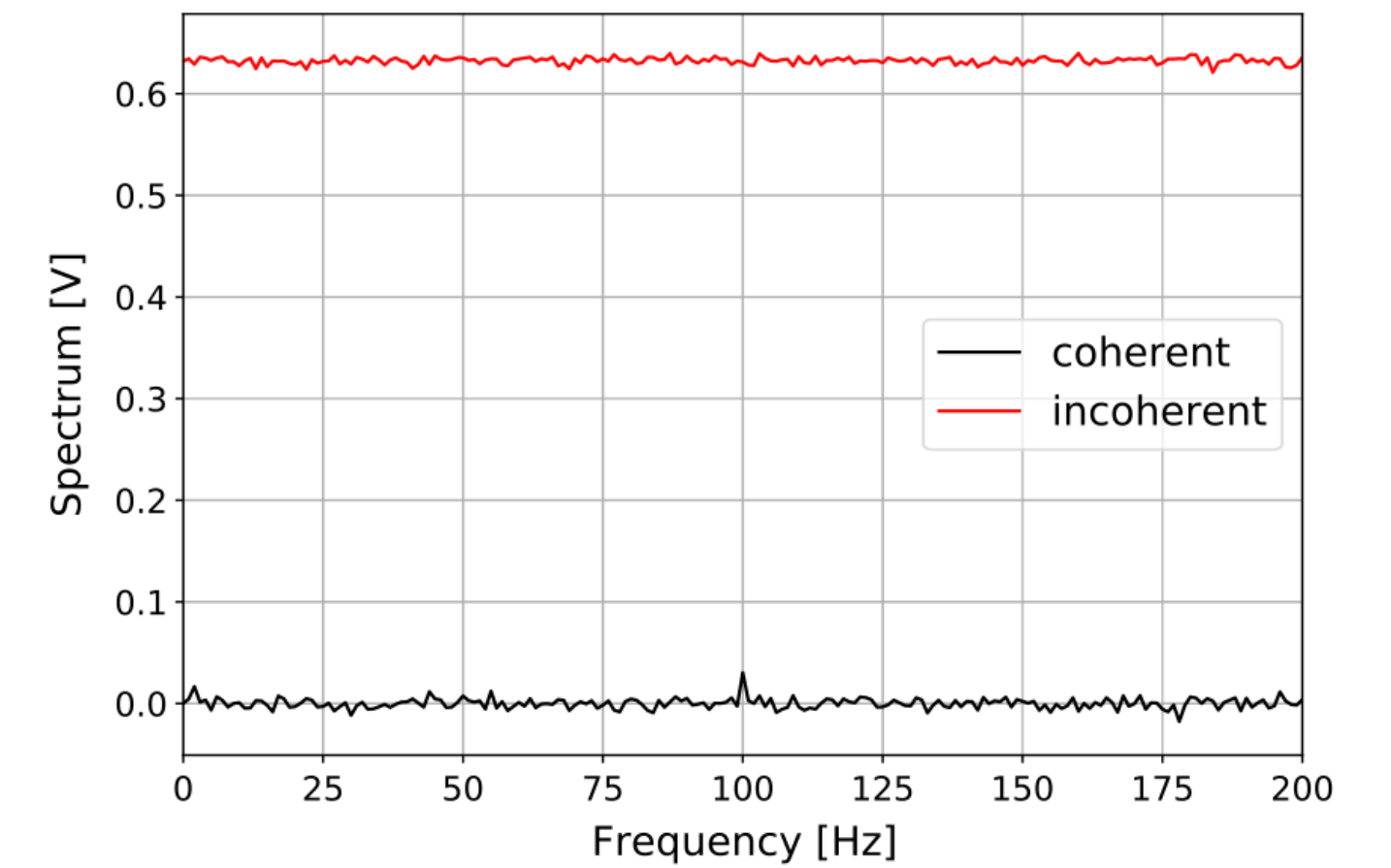
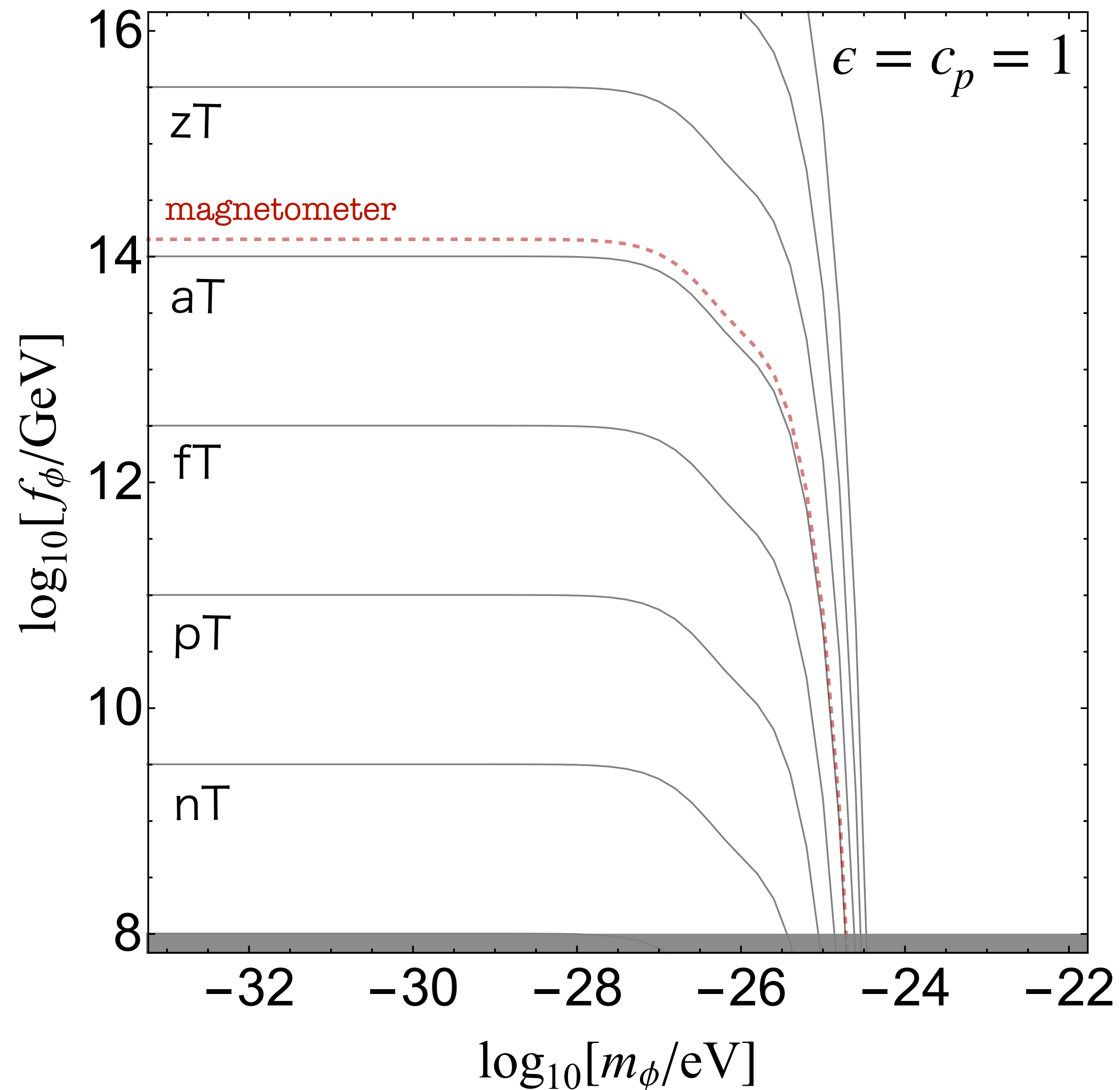
Spin precession towards galactic center everywhere on Earth!

$$H_{\text{EFT}}^{\text{nonrela}} \simeq -\frac{c_N}{f_\phi} \vec{\partial} \phi \cdot \bar{N} \vec{\sigma} N.$$



Sensitivity reach from magnetometer

- Detector has directional sensitivity
-> galactic center.
- A calibration erases a constant effective magnetic field.
-> Daily modulation
- Known periodicity
-> Coherent averaging is efficient.



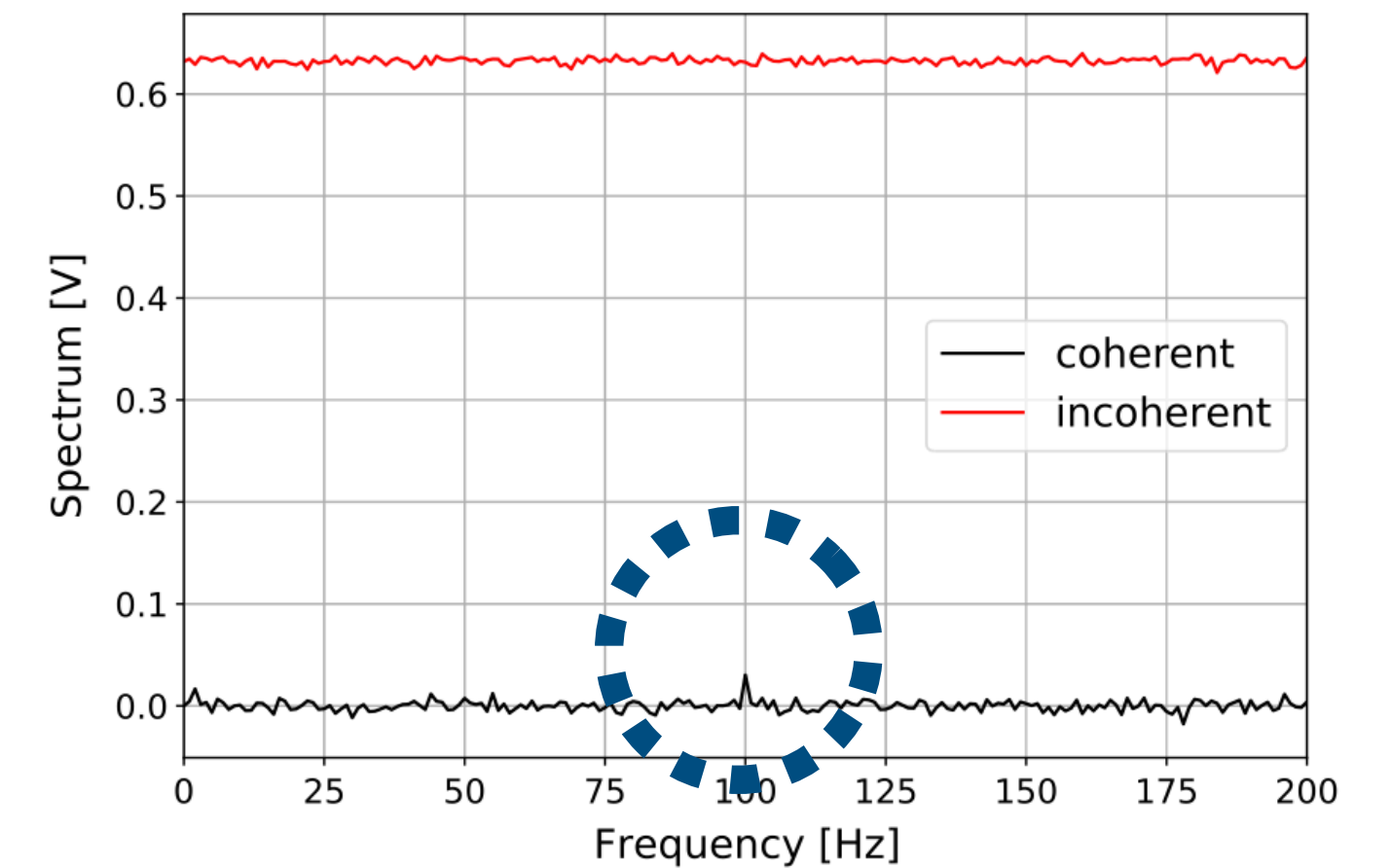
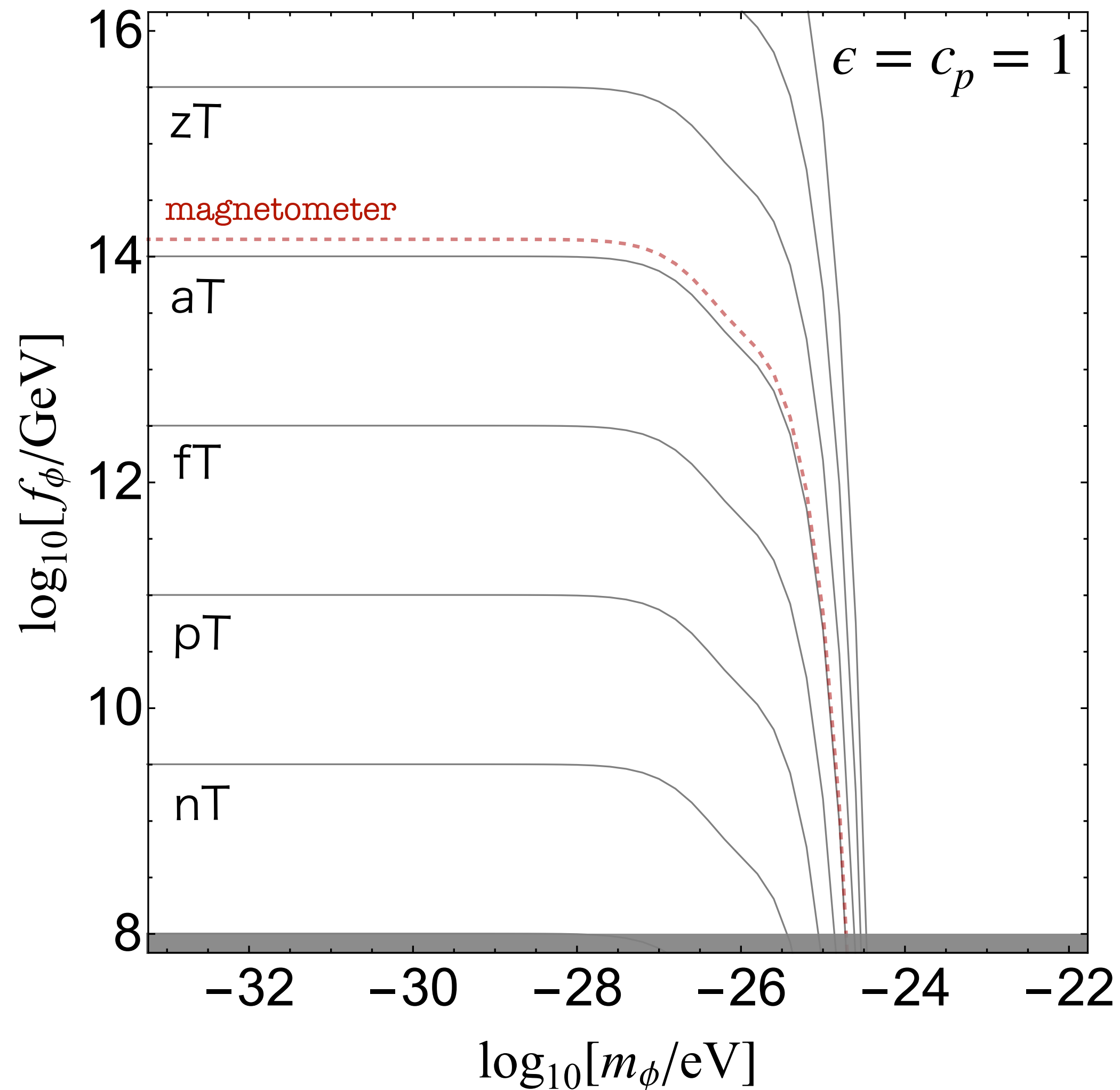
Case of nucleon-electron co-magnetometer with coherent averaging.

$$B_{\text{sig}} \approx 0.67 \text{ aT} \left[\frac{\text{SNR}}{5} \right] \left[\frac{300}{N} \right]^{0.5} \left[\frac{\delta B_n}{1 \text{ fT}/\sqrt{\text{Hz}}} \right] \left[\frac{b}{20 \mu\text{Hz}} \right]^{0.5} \frac{1}{\sqrt{2}}.$$

We can probe ultra-light axion with decay constant close to the string scale!

Sensitivity reach from magnetometer

- Detector has directional sensitivity
-> galactic center.
- A calibration erases a constant effective magnetic field.
-> Daily modulation
- Known periodicity
-> Coherent averaging is efficient.



Case of nucleon-electron co-magnetometer with coherent averaging.

$$B_{\text{sig}} \approx 0.67 \text{ aT} \left[\frac{\text{SNR}}{5} \right] \left[\frac{300}{N} \right]^{0.5} \left[\frac{\delta B_n}{1 \text{ fT}/\sqrt{\text{Hz}}} \right] \left[\frac{b}{20 \mu\text{Hz}} \right]^{0.5} \frac{1}{\sqrt{2}}.$$

We can probe ultra-light axion with decay constant close to the string scale!

Conclusions

Light ALPs are motivated and not excluded by 5th force because the miraculous and accidental CP-conserving nature in the SM. On the other hand, if we do not impose the miracle in the dark sector,

[Kodai Sakurai, WY 2111.03653](#)

- A simple, or perhaps the simplest, ALP model predicts **CP-even ALP**.
- It may be probed via displaced vertex followed by Higgs boson decay.
- It is a good DM candidate if $m_a < MeV$.

[Dongok Kim, Younggeun Kim, Yannis K. Semertzidis, Yun Chang Shin, WY, Phys.Rev.D 104 \(2021\) 9, 095010](#)

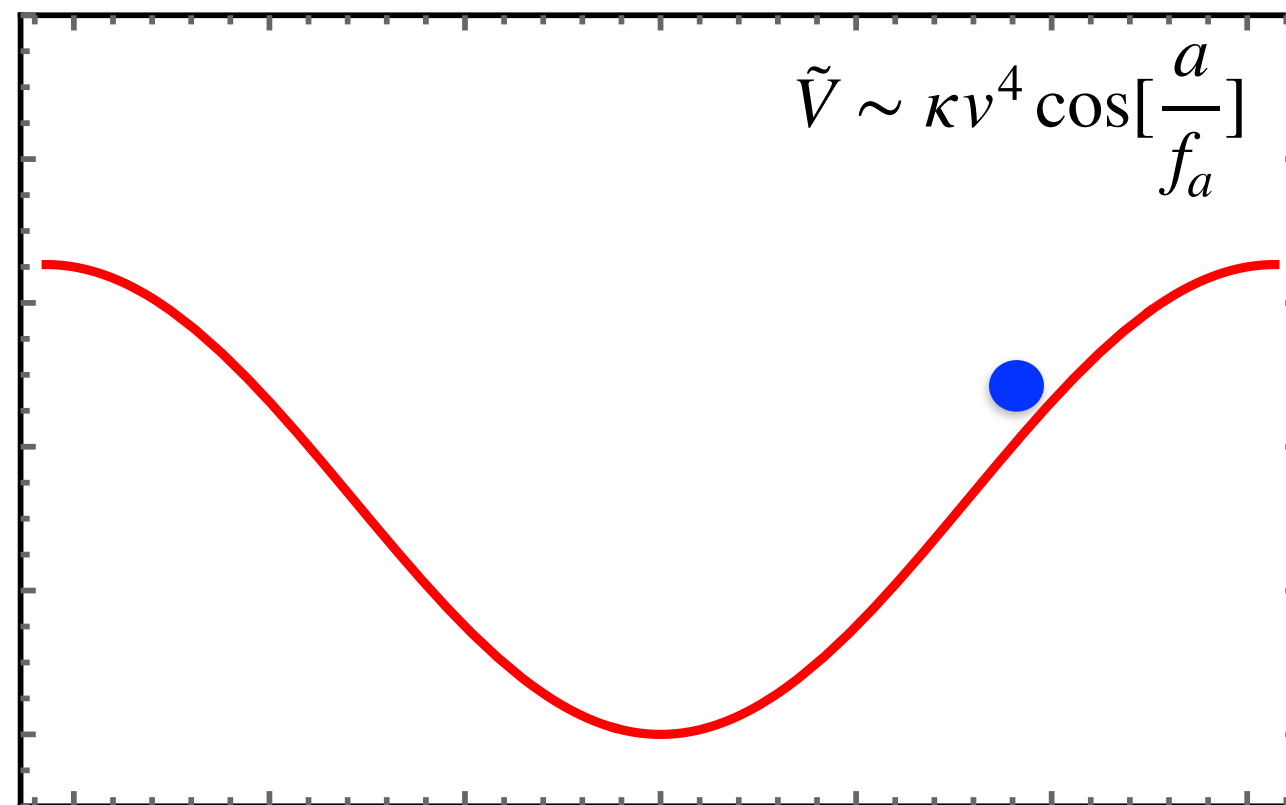
- Very light ALP coupled to DM with CPV induces a **cosmic axion force** towards galactic center.
- A decay constant around string scale can be probed via the spin precession of SM fermion.

Backup

Axion DM production in early Universe

Misalignment mechanism

Others (with interactions)



[Preskill et al, 1983;](#)
[Abbott, Sikivie, 1983;](#)
[Dine, Fishler, 1983;](#)

Energy density of
coherent oscillation
contributes to DM.

*Misalignment mechanism with
low-scale inflation

[Graham, Scherlis, 1805.07362;](#)
[Takahashi, WY, and Guth 1805.08763 etc](#)

⋮

*Inflaton decay to axion particles

[Moroi WY, 2011.09475;](#)

*Broad parametric resonance

[Mazumdar, Qutub, 1508.04136;](#)[Co et al, 1711.10486](#)

*U(1) phase transition

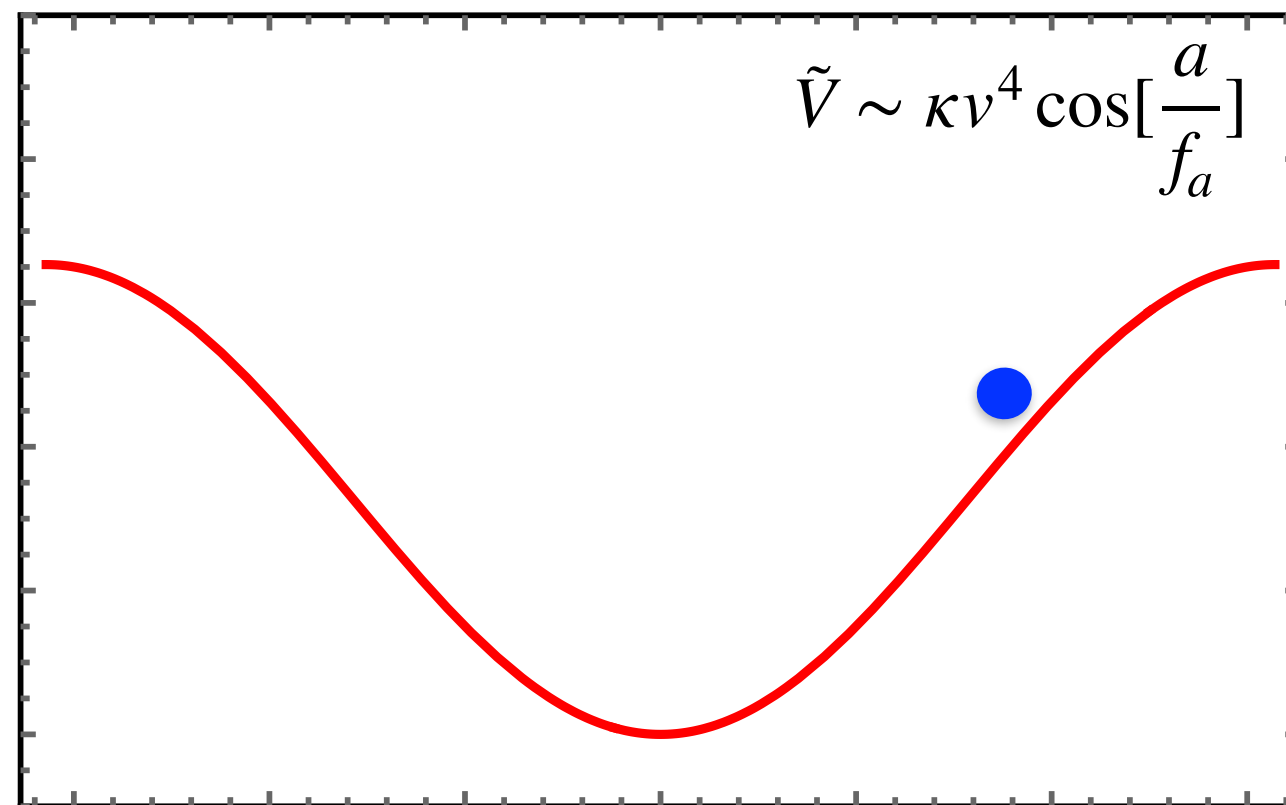
[Nakayama, WY, 2105.14549 \(See also Harigaya, Leedom 1910.04163\)](#)

⋮

Axion DM production in early Universe

Misalignment mechanism

Others (with interactions)



[Preskill et al, 1983;](#)
[Abbott, Sikivie, 1983;](#)
[Dine, Fishler, 1983;](#)

Energy density of
coherent oscillation
contributes to DM.

*Misalignment mechanism with
low-scale inflation

[Graham, Scherlis, 1805.07362;](#)
[Takahashi, WY, and Guth 1805.08763 etc](#)

⋮

*Inflaton decay to axion particles

[Moroi WY, 2011.09475;](#)

*Broad parametric resonance

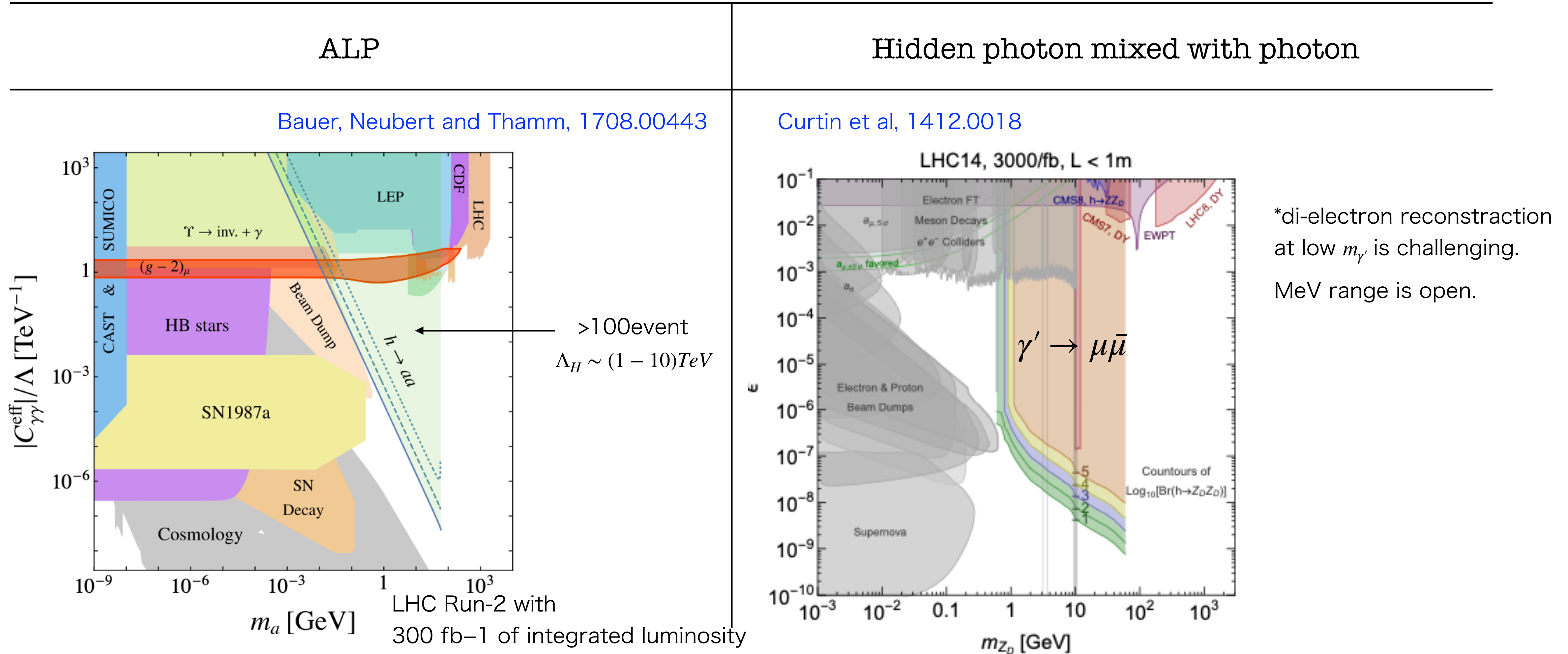
[Mazumdar, Qutub, 1508.04136;](#)[Co et al, 1711.10486](#)

*U(1) phase transition

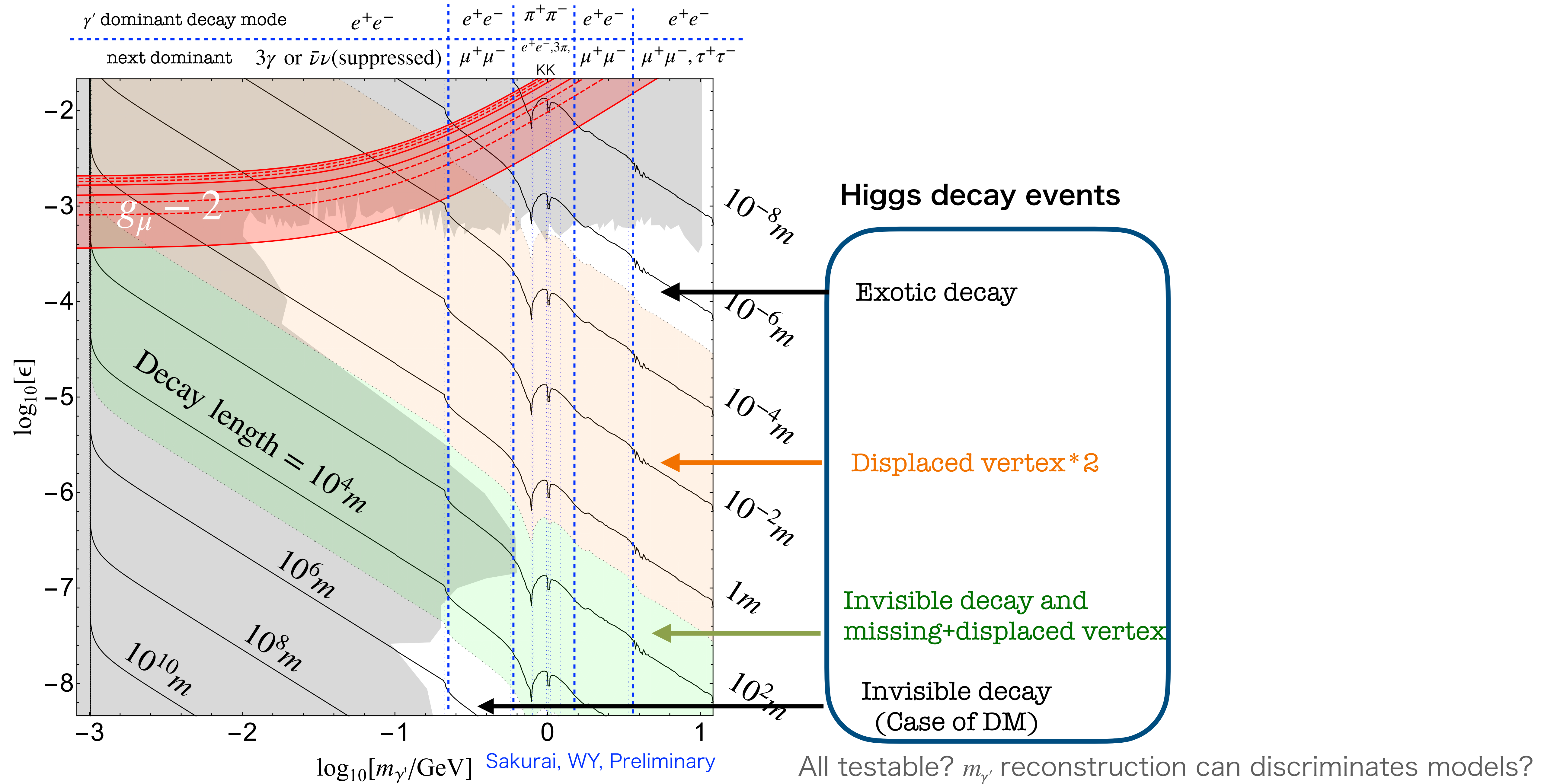
[Nakayama, WY, 2105.14549 \(See also Harigaya, Leedom 1910.04163\)](#)

⋮

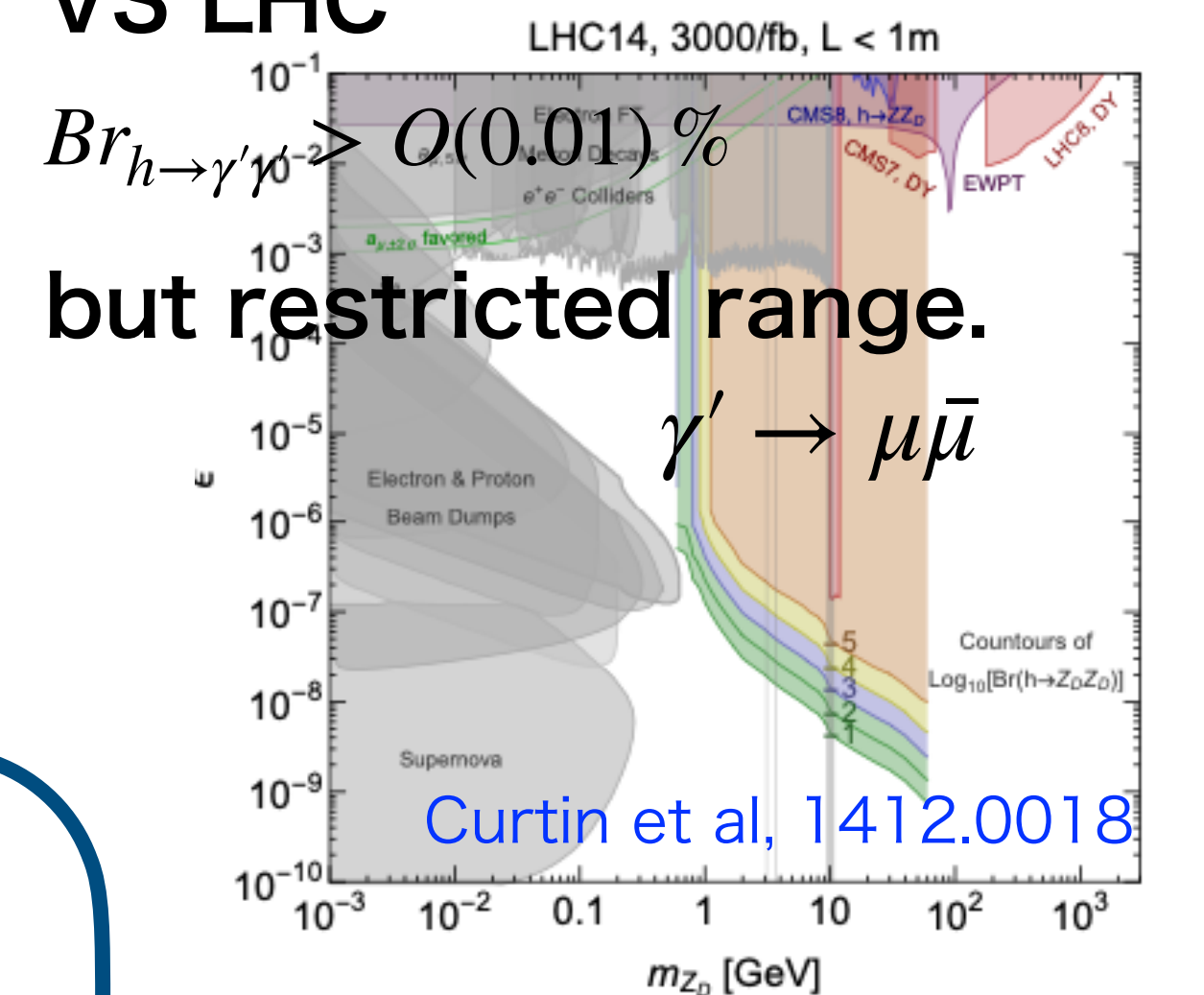
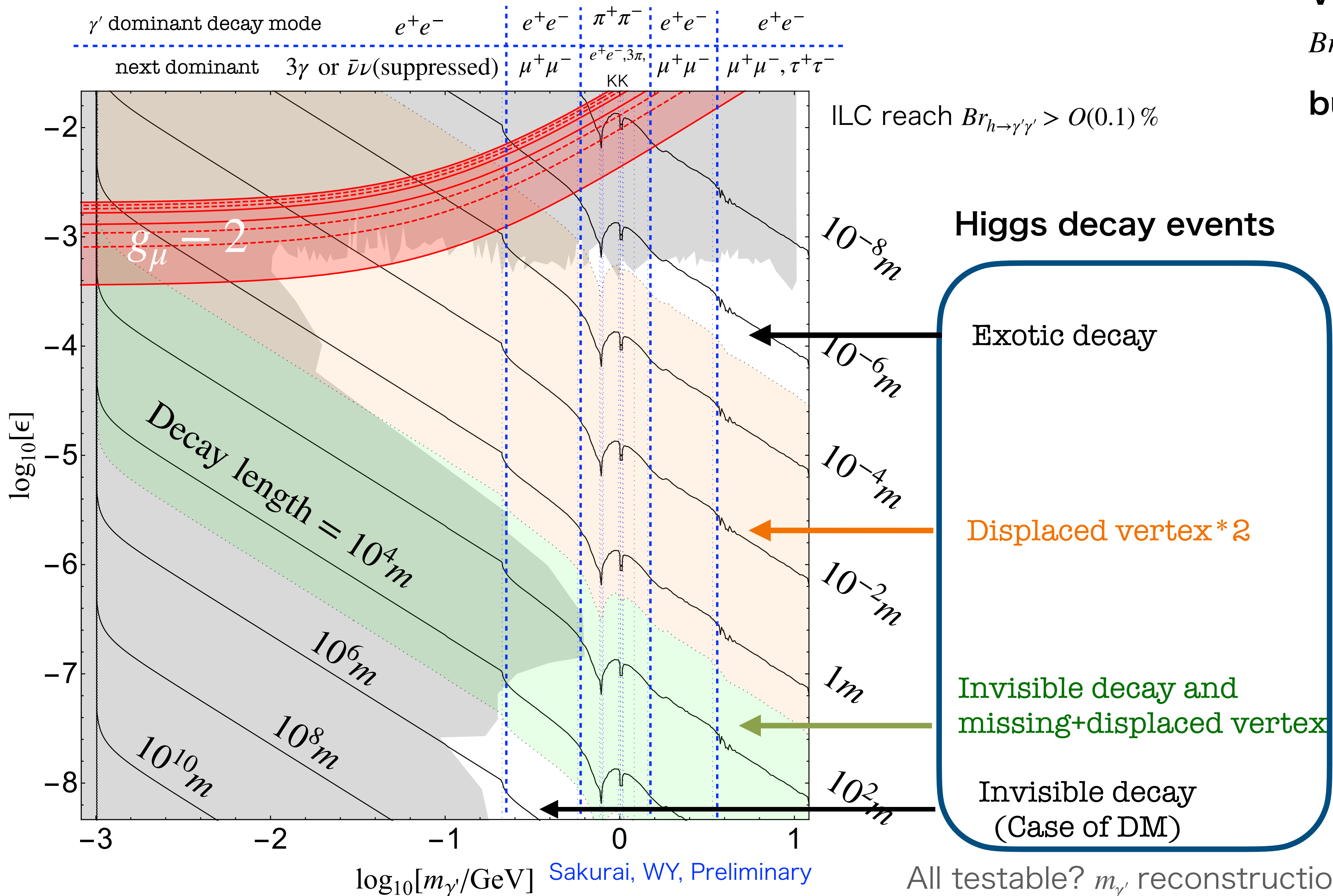
LHC (future-)search which reaches smaller couplings. This is the case if the event can be identified.



Case of hidden photon at ILC 250GeV $h \rightarrow \gamma'\gamma', \gamma' \rightarrow \text{SMs}$



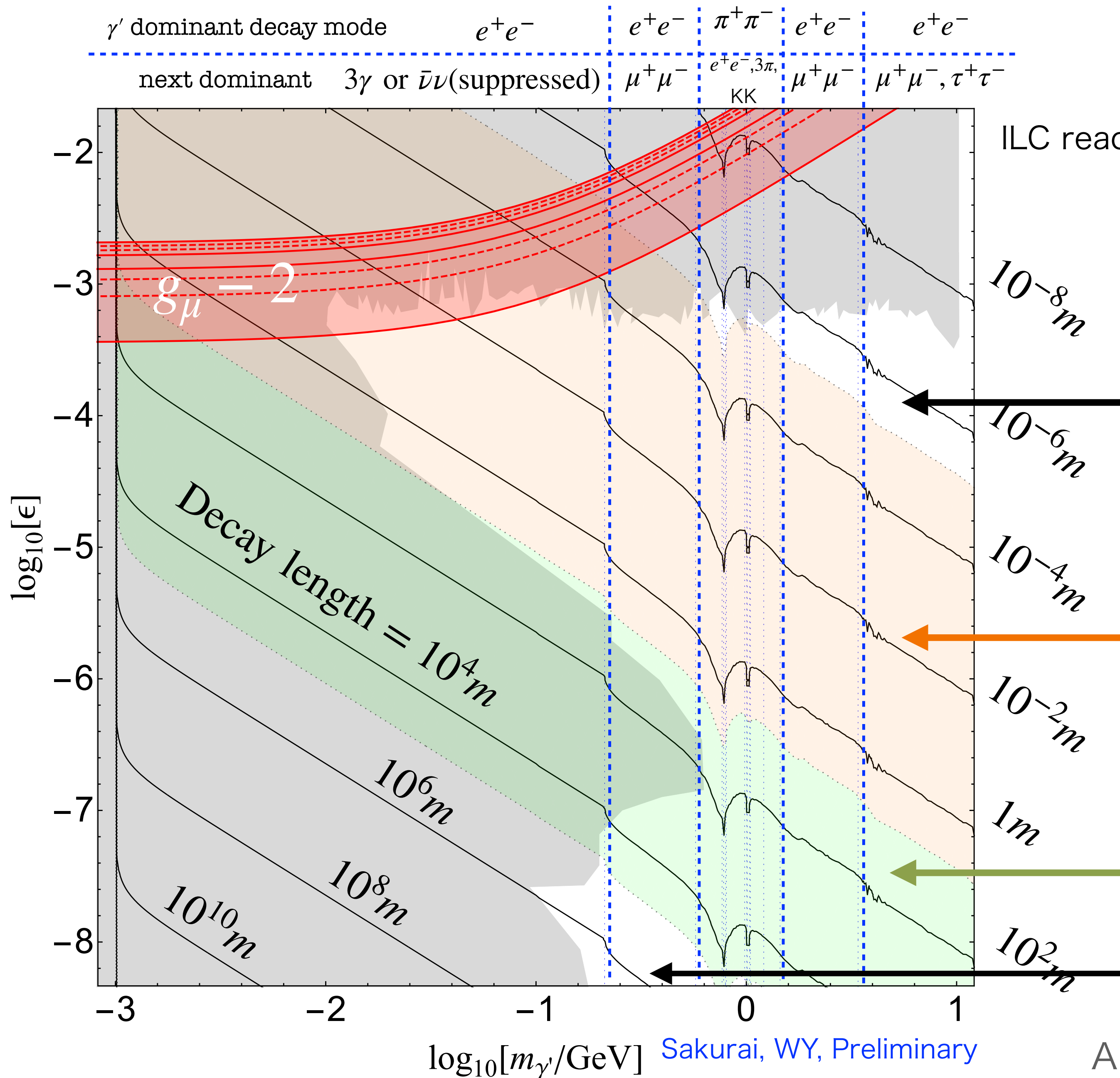
Case of hidden photon at ILC 250GeV $h \rightarrow \gamma' \gamma', \gamma' \rightarrow \text{SMs}$ VS LHC



*di-electron reconstruction at low $m_{\gamma'}$ is challenging?
MeV range is open.

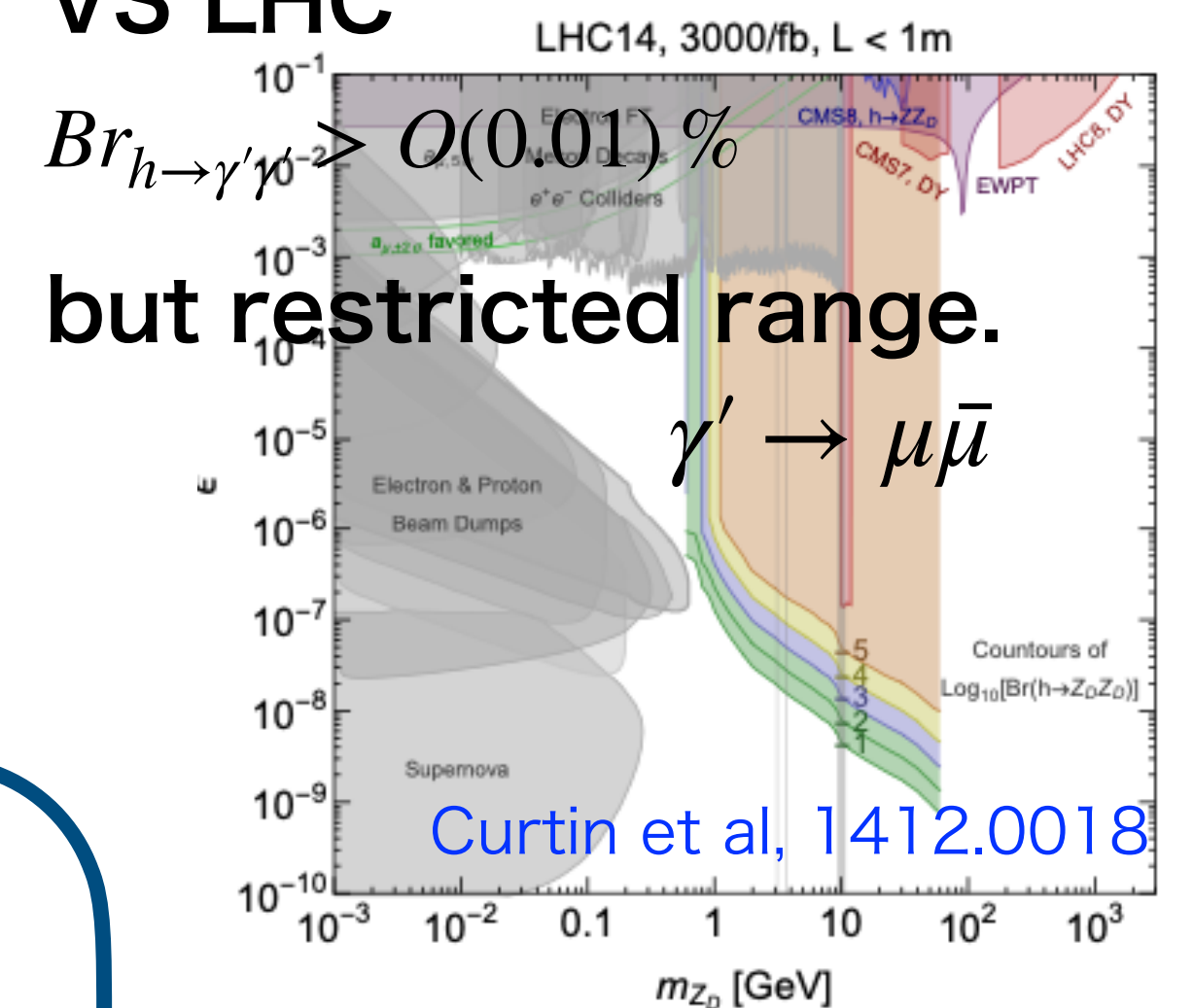
All testable? $m_{\gamma'}$ reconstruction can discriminates models?

Case of hidden photon at ILC 250GeV $h \rightarrow \gamma' \gamma', \gamma' \rightarrow \text{SMs}$ VS LHC



Higgs decay events

- Exotic decay
- Displaced vertex * 2
- Invisible decay and missing+displaced vertex
- Invisible decay (Case of DM)



*di-electron reconstruction at low $m_{\gamma'}$ is challenging?
MeV range is open.

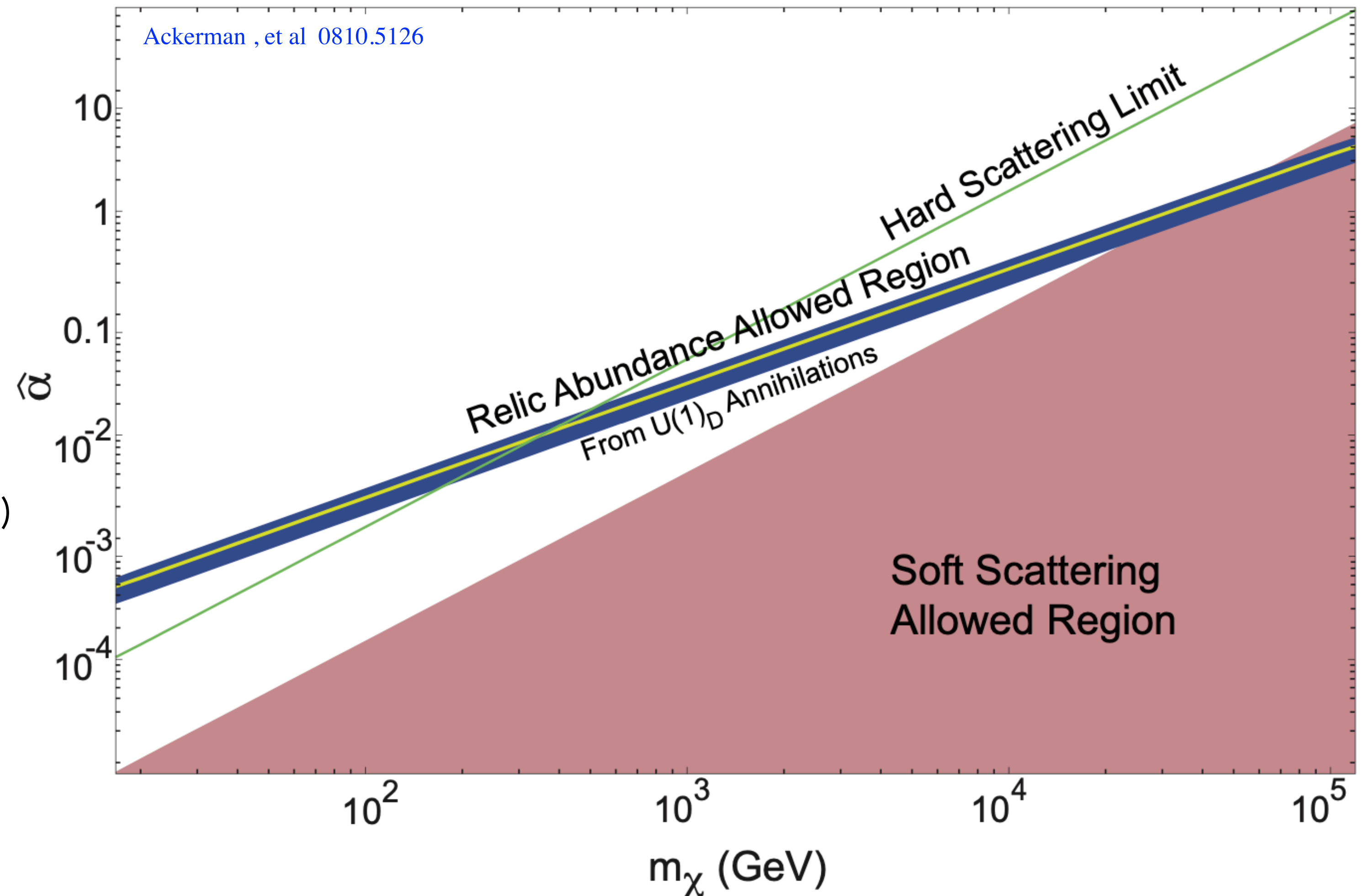
Decay length $\sim \Delta L_{\text{measured}}$

Decay length $\sim L_{\text{detector}} \frac{Br_{h \rightarrow \text{vis} + \text{missing}}}{Br_{h \rightarrow \text{inv}}}$

All testable? $m_{\gamma'}$ reconstruction can discriminates models?

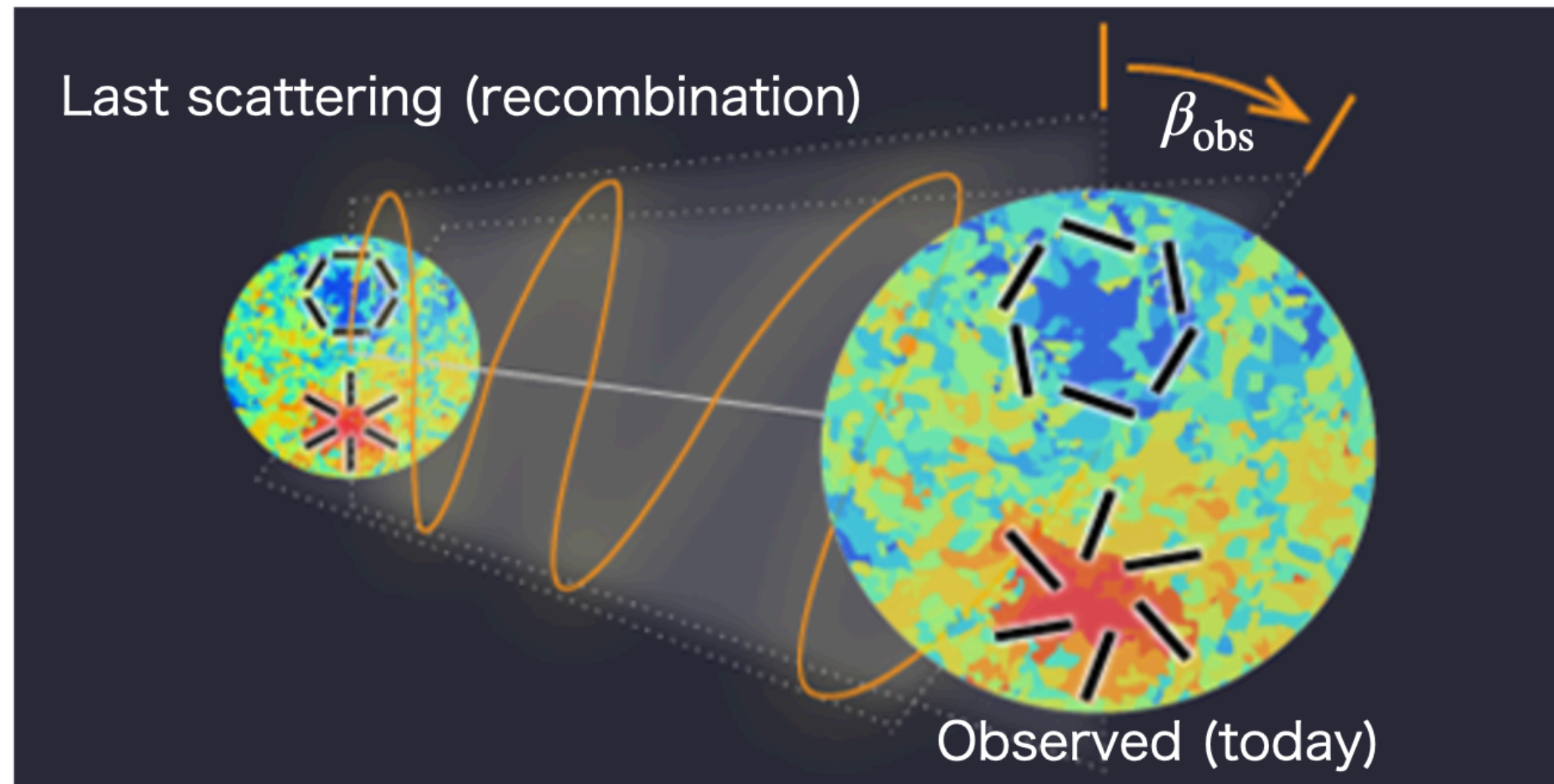
Constraint on DM self-interaction. (U(1)_{dark} gauge symmetry)

- $\hat{\alpha}$: dark fine-structure constant
- Screening is taken account
(I am not sure if there is study without screening. Anyway $m_\phi \gtrsim 10^{-30} eV \sim 1/Mpc$ should have a similar effect for screening.)



Light axion for CMB polarization?

A new analysis is recently performed to get a **parity-violating isotropic cosmic birefringence (CB)** from Planck2018 data.



$$\beta_{\text{obs}} = 0.35 \pm 0.14 \text{ deg}, \quad (2.4 \sigma)$$

Y. Minami/KEK

Minami and Komatsu, 2011.11254

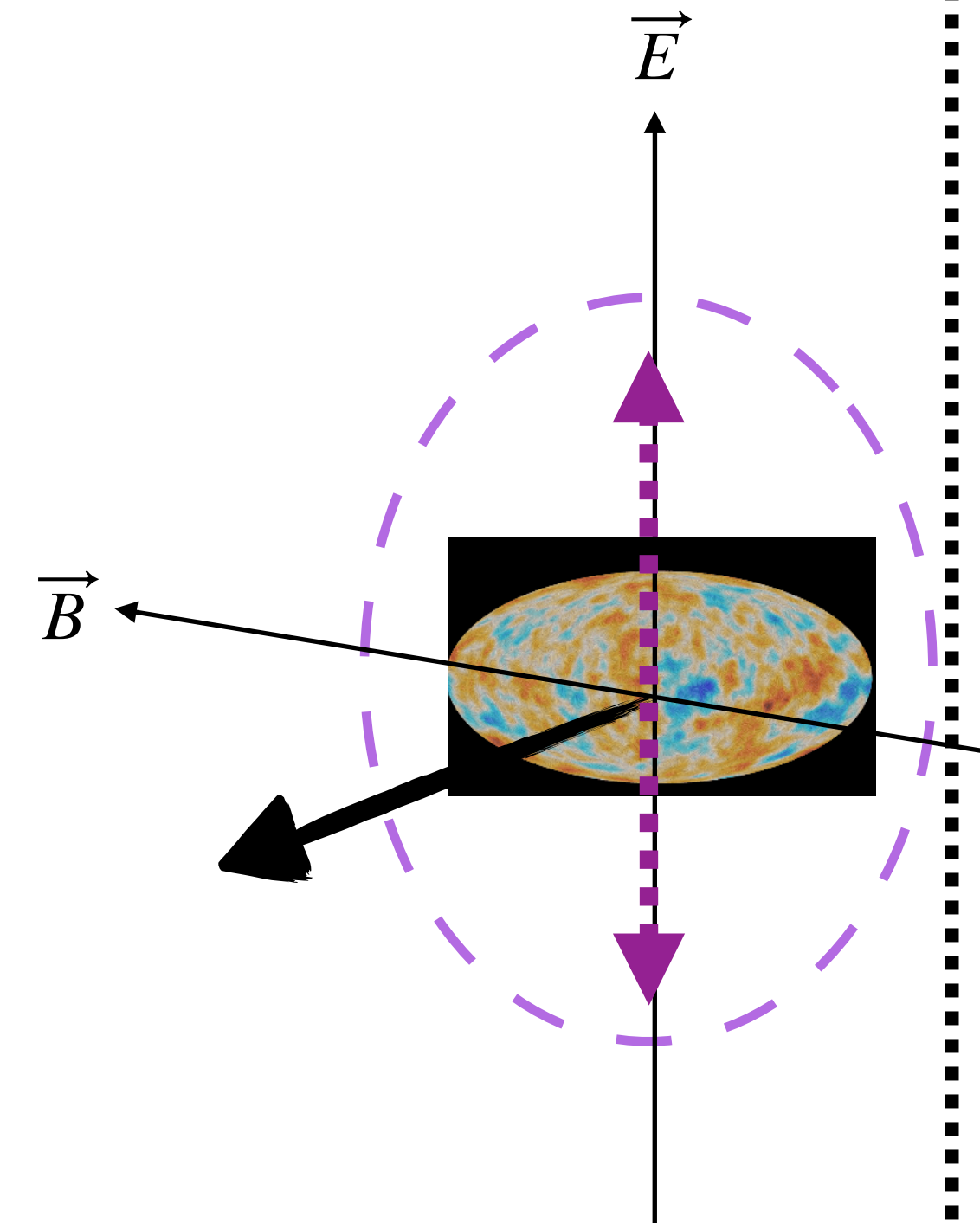
See also Clark et al, 2105.00120 for discussion.

Pogosian et al, 1904.07855 for future sensitivities.

$$\longrightarrow \mathcal{L} \supset \frac{g_{\phi\gamma\gamma}}{4} \phi F \tilde{F}$$

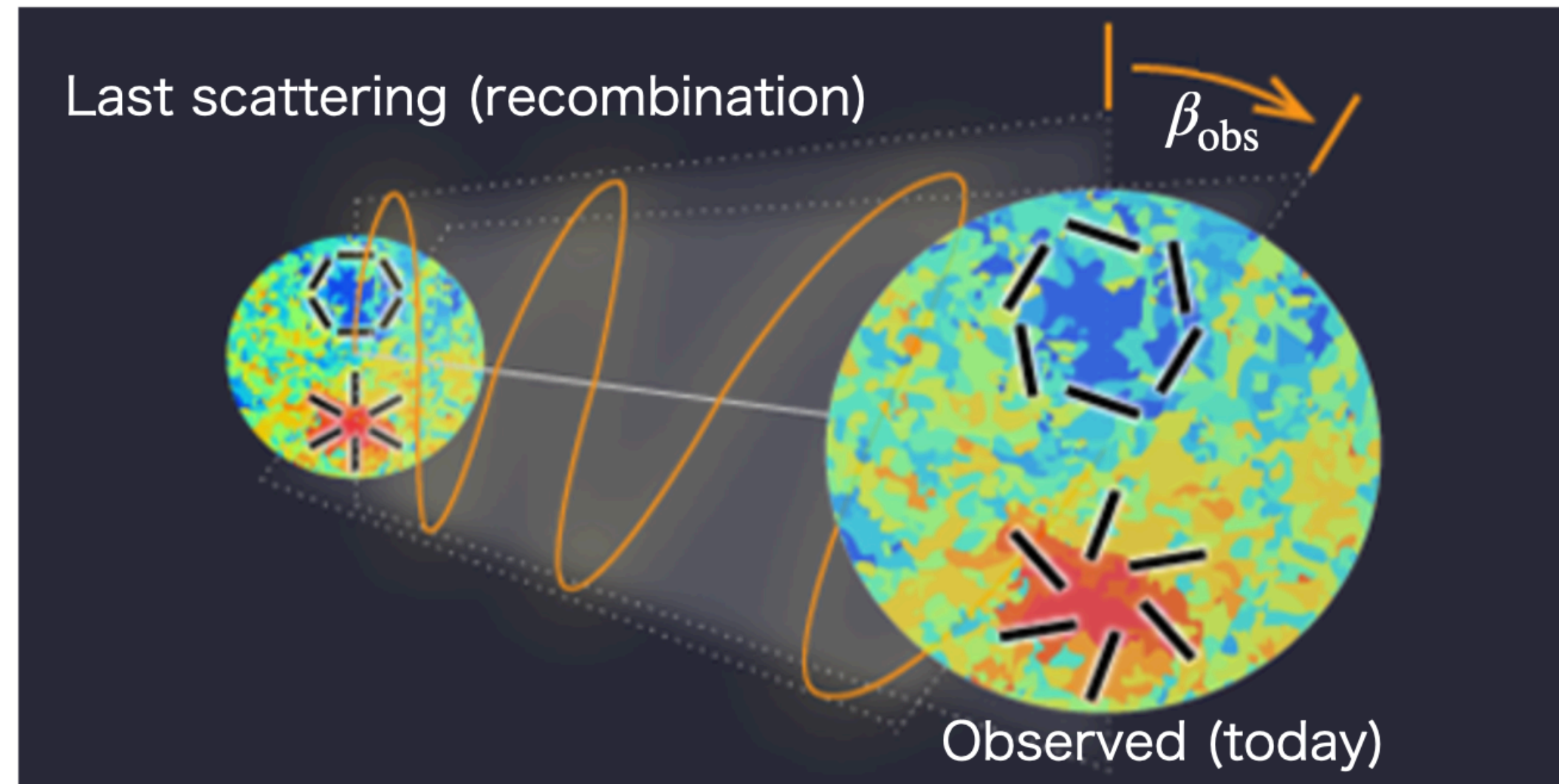
Carroll, Field, Jackiw, 1990; Harari, Sikivie, 1992; Carroll, 1998;

$$\mathcal{L} \approx \frac{1}{2} \left[(\vec{E} + \frac{1}{2} g_{\phi\gamma\gamma} \phi \vec{B})^2 - (\vec{B} - \frac{1}{2} g_{\phi\gamma\gamma} \phi \vec{E})^2 \right]$$



Light axion for CMB polarization?

A new analysis is recently performed to get a **parity-violating isotropic cosmic birefringence (CB)** from Planck2018 data.



$$\beta_{\text{obs}} = 0.35 \pm 0.14 \text{ deg}, \quad (2.4 \sigma)$$

Y. Minami/KEK

Minami and Komatsu, 2011.11254

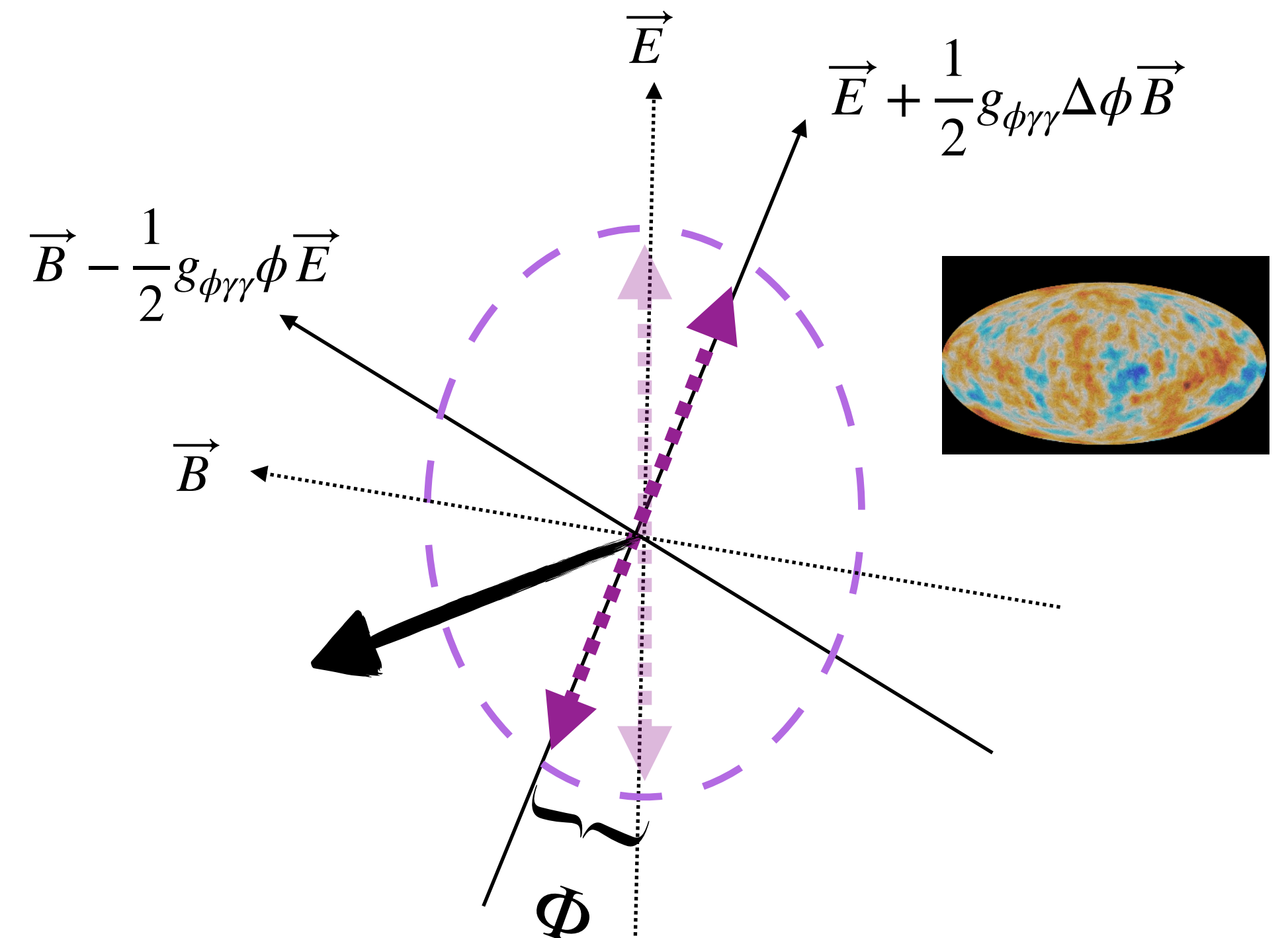
See also Clark et al, 2105.00120 for discussion.

Pogosian et al, 1904.07855 for future sensitivities.

$$\longrightarrow \mathcal{L} \supset \frac{g_{\phi\gamma\gamma}}{4} \phi F \tilde{F}$$

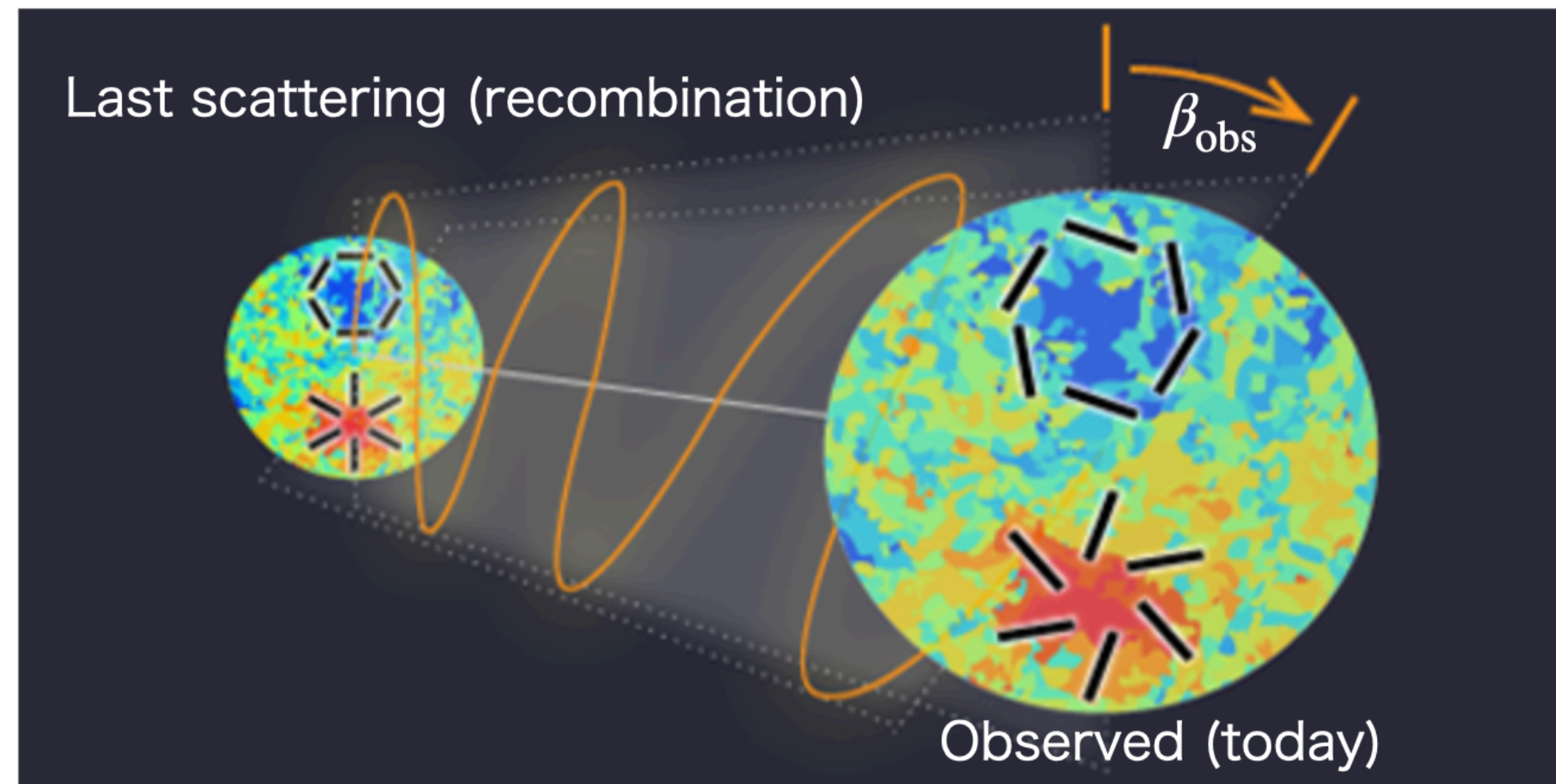
Carroll, Field, Jackiw, 1990; Harari, Sikivie, 1992; Carroll, 1998;

$$\mathcal{L} \approx \frac{1}{2} \left[(\vec{E} + \frac{1}{2} g_{\phi\gamma\gamma} \phi \vec{B})^2 - (\vec{B} - \frac{1}{2} g_{\phi\gamma\gamma} \phi \vec{E})^2 \right]$$



Light axion for CMB polarization?

A new analysis is recently performed to get a **parity-violating isotropic cosmic birefringence (CB)** from Planck2018 data.



$$\beta_{\text{obs}} = 0.35 \pm 0.14 \text{ deg}, \quad (2.4 \sigma)$$

Y. Minami/KEK

Minami and Komatsu, 2011.11254

See also Clark et al, 2105.00120 for discussion.

Pogosian et al, 1904.07855 for future sensitivities.

Explanation:

- Isotropic CB by $\dot{\phi} \neq 0$: Slow-rolling axion

Minami and Komatsu, 2011.11254, Fujita et al, 2011.11894, (CB and H_0 tension)

Mehta et al, 2103.06812, (Many ALPs); Nakagawa et al, 2103.08153, (Very light ALP); etc

- Isotropic CB by $|\partial_{\vec{x}}\phi| \neq 0$: axion domain walls

Takahashi, WY, 2012.11576

$$\longrightarrow \mathcal{L} \supset \frac{g_{\phi\gamma\gamma}}{4} \phi F\tilde{F}$$

Carroll, Field, Jackiw, 1990; Harari, Sikivie, 1992; Carroll, 1998;

$$\mathcal{L} \approx \frac{1}{2} \left[(\vec{E} + \frac{1}{2} g_{\phi\gamma\gamma} \phi \vec{B})^2 - (\vec{B} - \frac{1}{2} g_{\phi\gamma\gamma} \phi \vec{E})^2 \right]$$

