NATIONAL SCIENCE CENTRE
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SUSY $(g-2)_\mu$ with & without Neutralino Dark Matter

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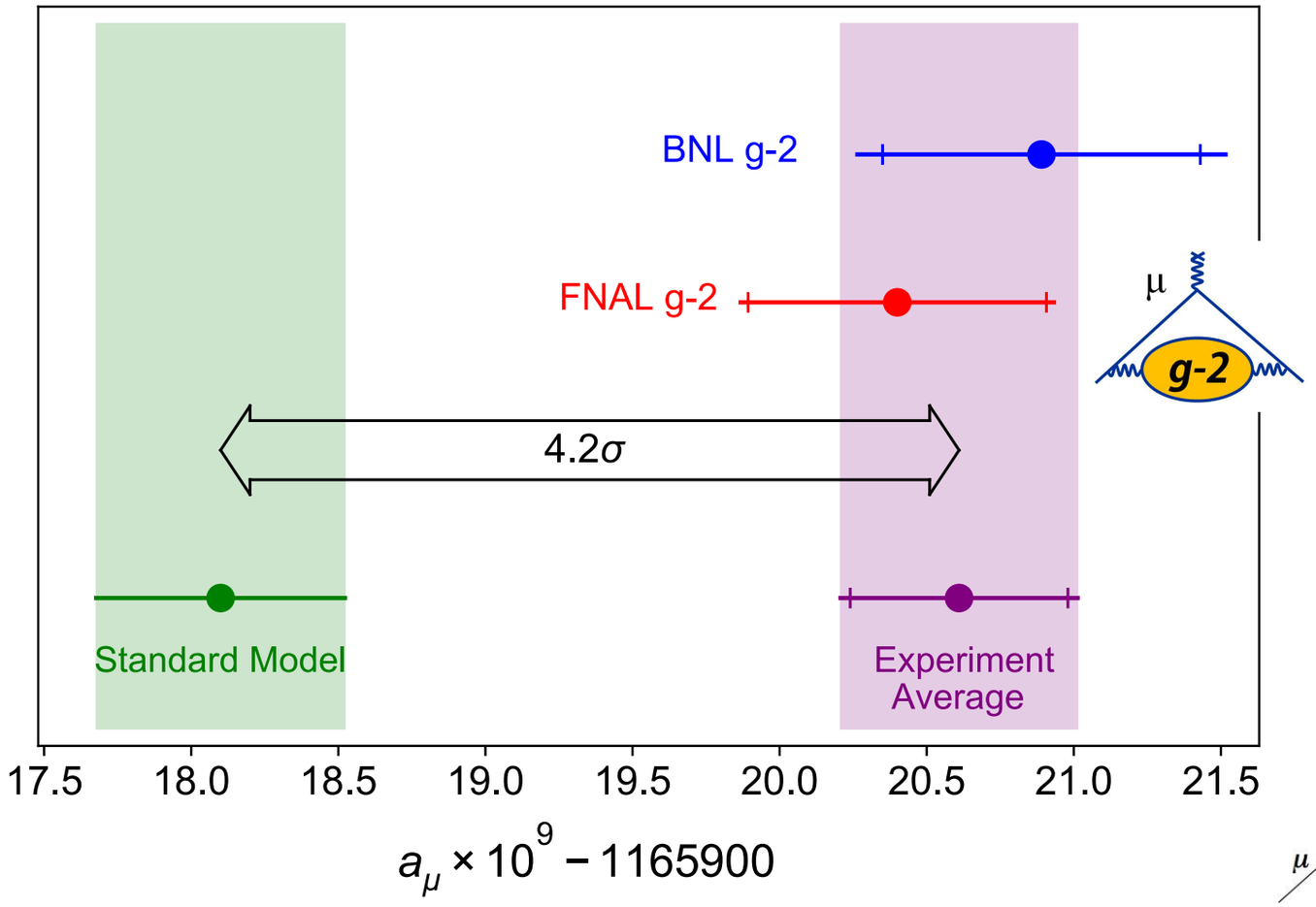
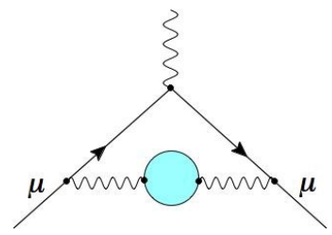
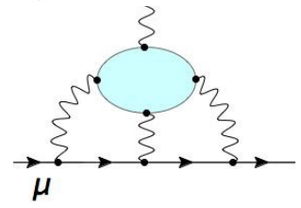
$(g-2)_\mu$ anomaly

[Phys. Rev. LeS. 126 (2021) 14, 141801]





from HVP, HLbL



		QED	HVP	EW	
a_μ^{theo}	= 0.00	1165	91	810	(43)
a_μ^{exp}	= 0.00	1165	92	061	(41)

stat err dominant

$$a_\mu^{\text{exp}} - a_\mu^{\text{theo}} \simeq (25 \pm 6) \times 10^{-10} \simeq \Delta a_\mu^{\text{BSM}} \; ?$$

Motivation

- There are many BSM scenarios that can explain the $(g\text{-}2)_\mu$ anomaly:

  Leptoquarks, Z', VLL, 2HDM, axion, ..

- Supersymmetry is particularly motivated since it offers:

  Coupling Unification, Radiative EWSB, Baryogenesis, DM, …

- There are many studies on SUSY g-2 already:

  [Athrona, Balazsa, Jacoba, Kotlarskic, Stockingerc, Stockinger-Kim]; [Chakraborti, Heinemeyer, Saha]; [Endo,Hamaguchi,Iwamoto,Kitahara]; [Cox, Han, Yanagida]; [Baum, Carena, Shah, Wagner]; [Badziak, KS]; [Hagiwara,Ma,Mukhopadhyay'18], …

- Most studies assume the neutralino is the Lightest SUSY Particle (LSP) and stable.

  Q: What happens if neutralino is unstable? (e.g. RPV, Gravitino LSP)

  A: DM constraints go away, but LHC constraints change. **How?**

$$
\begin{array}{lcccccc}
 & & & \text{QED} & \text{HVP} & \text{EW} & \\
a_\mu^{\text{theo}} & = & 0.00 & 1165 & 91 & 810 & (43) \\
a_\mu^{\text{exp}} & = & 0.00 & 1165 & 92 & 061 & (41)
\end{array}
$$

- The deviation is size of the EW correction in SM:

$$
a_\mu^{\text{exp}} - a_\mu^{\text{theo}} \simeq (25 \pm 6) \times 10^{-10} \sim \mathcal{O}\left(\Delta a_\mu^{\text{SM,EW}}\right)
$$

- We need very light BSM particles **OR** enhancement from couplings

$$
\Delta a_\mu^{\text{BSM}} \sim \Delta a^{\text{SM,EW}} \cdot \underbrace{\left(\frac{m_W^2}{m_{\text{BSM}}^2}\right) \cdot \left(\frac{g_{\text{BSM}}}{g_{\text{SM}}}\right)}_{\mathcal{O}(1)}
$$

Chiral (tanβ) enhancement in SUSY

- (g-2) operator requires chirality flip:

$$\vec{\mu} = g\left(\frac{e}{2m}\right)\vec{s}$$

$$a_\mu = \frac{(g-2)}{2} \equiv m_\mu \tilde{a}_\mu$$

$$\mathscr{L}_{\text{eff}} \ni i\tilde{a}_\mu \cdot \bar{\psi}_L \sigma^{\mu\nu} \psi_R F_{\mu\nu}$$

SM: $\tilde{a}_\mu^{\text{SM}} \propto Y_\mu \langle H \rangle = m_\mu$

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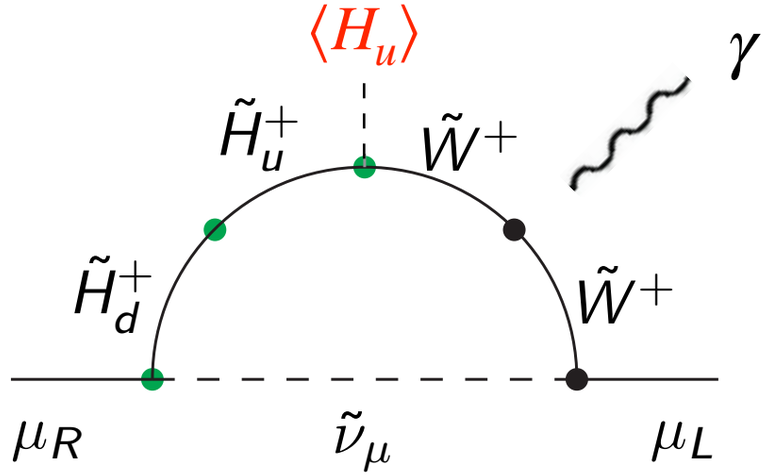
SM: $\tilde{a}_\mu^{\text{SM}} \propto Y_\mu \langle H \rangle = m_\mu$

SUSY: $\Delta\tilde{a}_\mu^{\text{SUSY}} \propto Y_\mu \langle H_u \rangle = m_\mu \cdot \tan\beta$

$m_\mu = Y_\mu \langle H_d \rangle \qquad \tan\beta \equiv \dfrac{\langle H_u \rangle}{\langle H_d \rangle}$

$\langle H_u \rangle^2 + \langle H_d \rangle^2 = \langle H \rangle^2$

$(246\,\text{GeV})^2$



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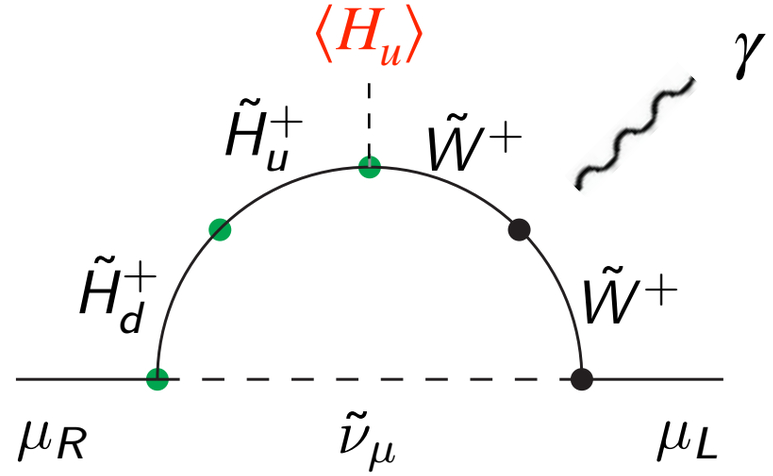


$$\langle H_u \rangle^2 + \langle H_d \rangle^2 = \langle H \rangle^2$$

$$(246\,\text{GeV})^2$$

$$\Delta a_\mu^{\text{BSM}} \sim \Delta a^{\text{SM,EW}} \cdot \left(\frac{m_W^2}{m_{\text{SUSY}}^2}\right) \cdot \tan\beta$$

$$\tan\beta \in [5-60] \Rightarrow m_{\text{SUSY}} \in [200-600]\,\text{GeV}$$

- Due to strong LHC constraints, we *decouple coloured SUSY particles* (they do not contribute to $(g-2)_\mu$ anyway).

- a_μ^{SUSY} depends on 5 mass parameters and tanβ :

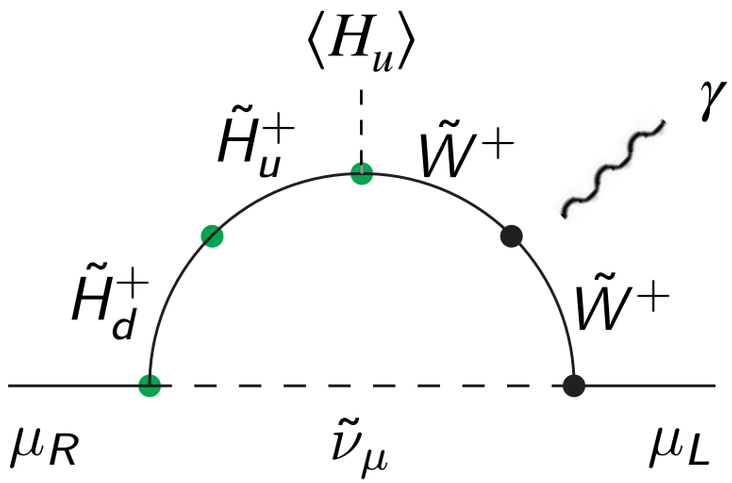
$$M_1 : \text{Bino mass}$$
$$M_2 : \text{Wino mass}$$
$$\mu : \text{Higgsino mass}$$

$$m_{\tilde{l}_R} \equiv \widetilde{m}^2_{\tilde{e}_R} = \widetilde{m}^2_{\tilde{\mu}_R} = \widetilde{m}^2_{\tilde{\tau}_R}$$
$$m_{\tilde{l}_L} \equiv \widetilde{m}_{\tilde{\nu}_e} = \widetilde{m}_{\tilde{\nu}_\mu} = \widetilde{m}_{\tilde{\nu}_\tau} = \widetilde{m}_{\tilde{e}_L} = \widetilde{m}_{\tilde{\mu}_L} = \widetilde{m}_{\tilde{\tau}_L}$$
$$\tan\beta \equiv \langle H_u \rangle / \langle H_d \rangle$$

no LFV due to universal soft masses: avoid strong constraint from $\mu \to e\,\gamma$

$$\Delta a_\mu^{\mathrm{SUSY}} = \Delta a_\mu^{\mathrm{WHL}} + \Delta a_\mu^{\mathrm{BHL}} + \Delta a_\mu^{\mathrm{BHR}} + \Delta a_\mu^{\mathrm{BLR}}$$

$$\Delta a_\mu^{\text{SUSY}} = \Delta a_\mu^{\text{WHL}} + \Delta a_\mu^{\text{BHL}} + \Delta a_\mu^{\text{BHR}} + \Delta a_\mu^{\text{BLR}}$$



$$\Delta a_\mu^{\text{WHL}}(M_2, \mu, m_{\tilde{l}_L}) = \frac{\alpha_W}{8\pi} \frac{m_\mu^2}{M_2 \mu} \tan\beta \cdot f_{\text{W}}(\{\mathbf{m}\})$$

M_1 : Bino ($\tilde{B}$) mass

M_2 : Wino ($\tilde{W}$) mass

μ : Higgsino ($\tilde{H}_u, \tilde{H}_d$) mass

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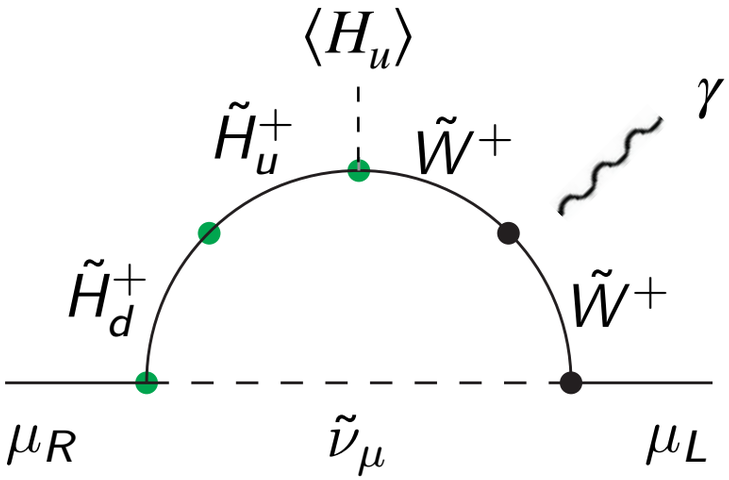
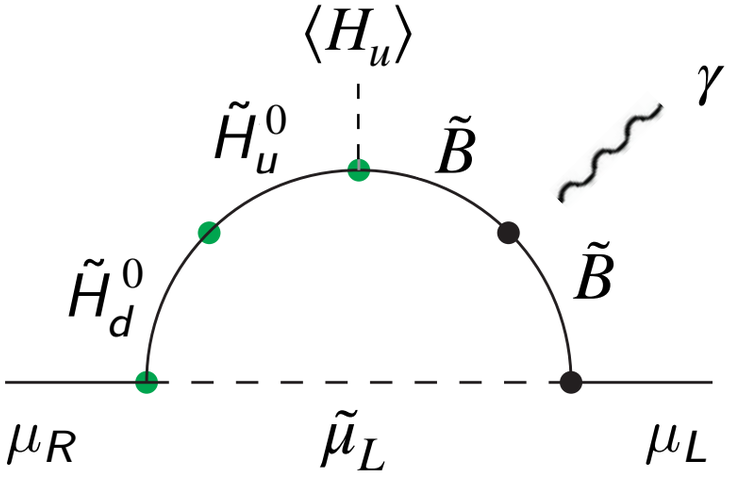


$$\Delta a_\mu^{\text{WHL}}(M_2, \mu, m_{\tilde{l}_L}) = \frac{\alpha_W}{8\pi} \frac{m_\mu^2}{M_2 \mu} \tan\beta \cdot f_{\text{W}}(\{\mathbf{m}\})$$

$$\Delta a_\mu^{\text{BHL}}(M_1, \mu, m_{\tilde{l}_L}) = \frac{\alpha_Y}{8\pi} \frac{m_\mu^2}{M_1 \mu} \tan\beta \cdot f_{\text{N}}(\{\mathbf{m}\})$$



M_1 : Bino ($\tilde{B}$) mass

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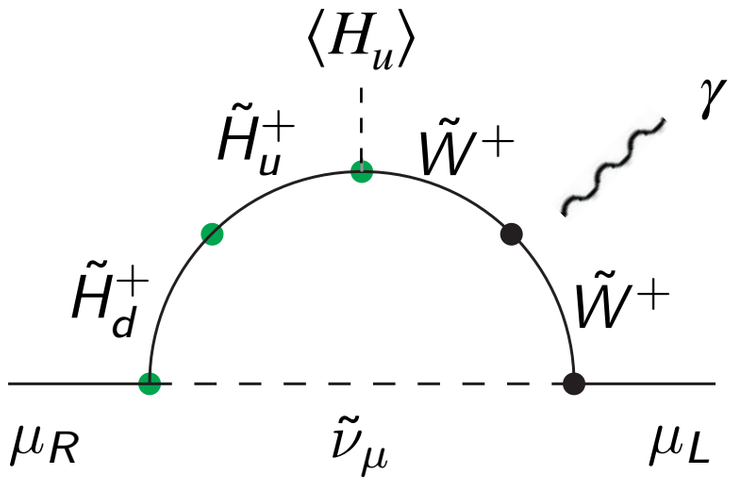
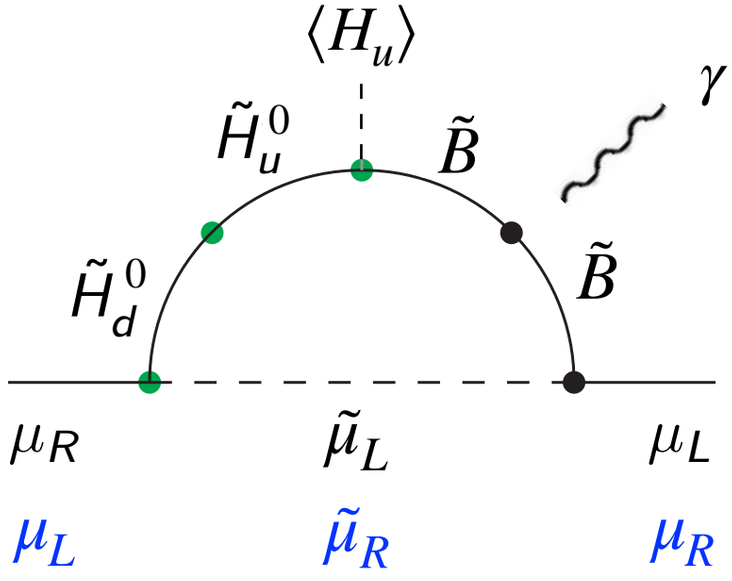
$$\Delta a_\mu^{\rm SUSY} = \Delta a_\mu^{\rm WHL} + \Delta a_\mu^{\rm BHL} + \Delta a_\mu^{\rm BHR} + \Delta a_\mu^{\rm BLR}$$



$$\Delta a_\mu^{\rm WHL}(M_2, \mu, m_{\tilde{l}_L}) = \frac{\alpha_W}{8\pi}\frac{m_\mu^2}{M_2\mu}\tan\beta \cdot f_{\rm W}(\{\mathbf{m}\})$$

$$\Delta a_\mu^{\rm BHL}(M_1, \mu, m_{\tilde{l}_L}) = \frac{\alpha_Y}{8\pi}\frac{m_\mu^2}{M_1\mu}\tan\beta \cdot f_{\rm N}(\{\mathbf{m}\})$$

$$\Delta a_\mu^{\rm BHR}(M_1, \mu, m_{\tilde{l}_R}) = -\frac{\alpha_Y}{8\pi}\frac{m_\mu^2}{M_1\mu}\tan\beta \cdot f_{\rm N}(\{\mathbf{m}\})$$



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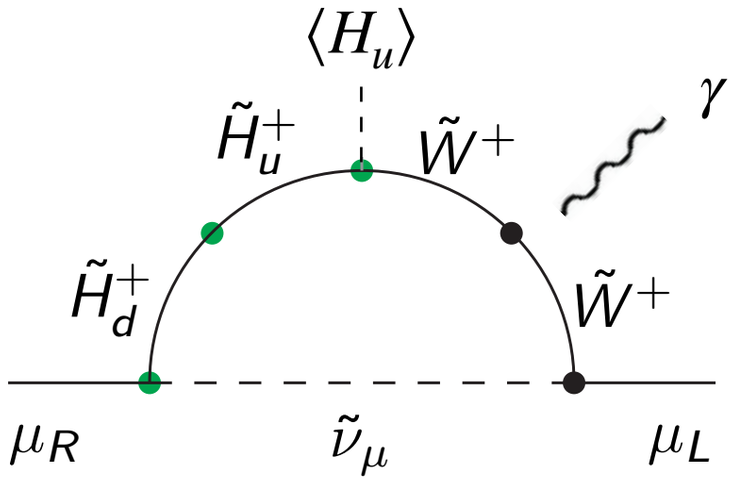
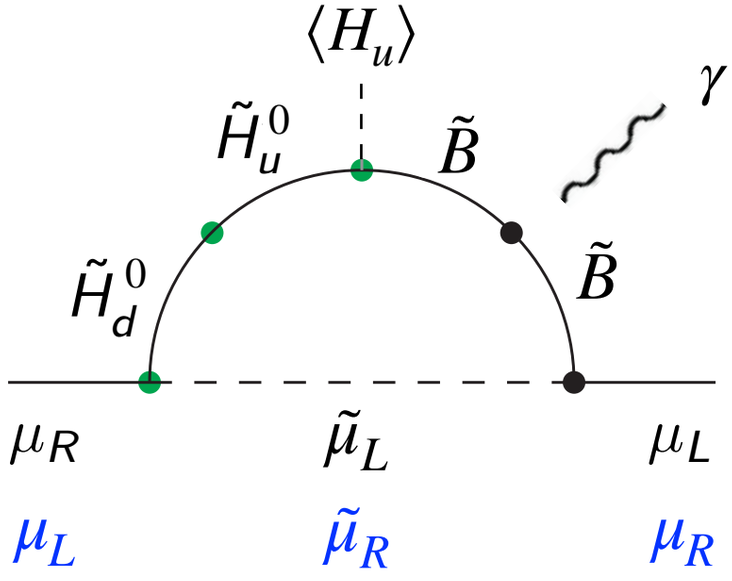


$$\Delta a_\mu^{\text{WHL}}(M_2, \mu, m_{\tilde{l}_L}) = \frac{\alpha_W}{8\pi}\frac{m_\mu^2}{M_2 \mu}\tan\beta \cdot f_{\text{W}}(\{\mathbf{m}\})$$

$$\Delta a_\mu^{\text{BHL}}(M_1, \mu, m_{\tilde{l}_L}) = \frac{\alpha_Y}{8\pi}\frac{m_\mu^2}{M_1 \mu}\tan\beta \cdot f_{\text{N}}(\{\mathbf{m}\})$$

$$\Delta a_\mu^{\text{BHR}}(M_1, \mu, m_{\tilde{l}_R}) = -\frac{\alpha_Y}{8\pi}\frac{m_\mu^2}{M_1 \mu}\tan\beta \cdot f_{\text{N}}(\{\mathbf{m}\})$$



M_1 : Bino ($\tilde{B}$) mass

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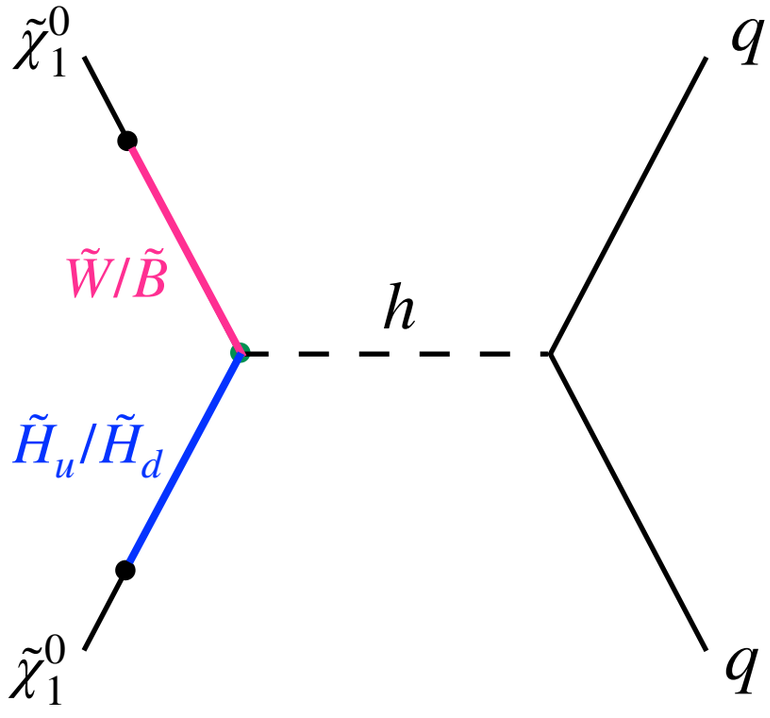
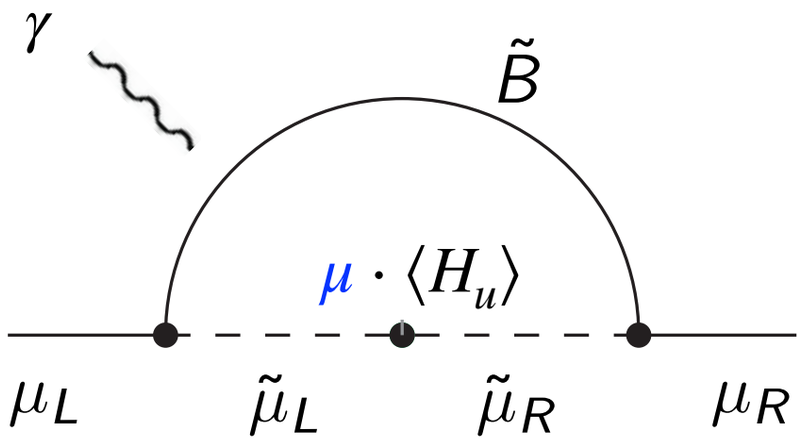
μ : Higgsino ($\tilde{H}_u, \tilde{H}_d$) mass

Large gaugino-Higgsino mixing leads to a **large cross-section for DM Direct Detection:**



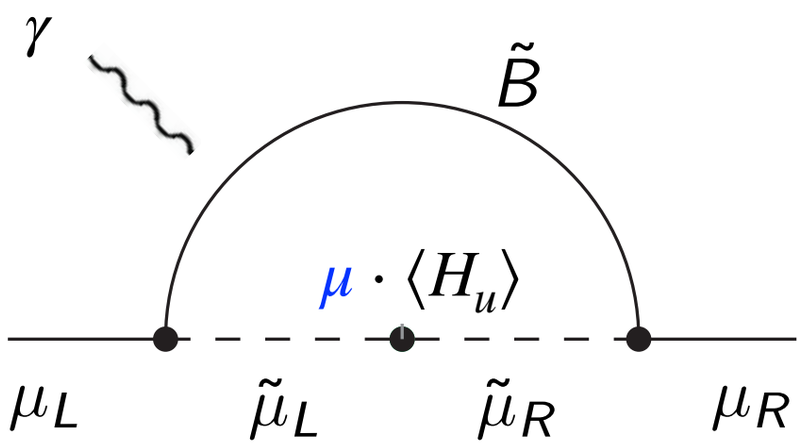
$$\Delta a_\mu^{\text{SUSY}} = \Delta a_\mu^{\text{WHL}} + \Delta a_\mu^{\text{BHL}} + \Delta a_\mu^{\text{BHR}} + \Delta a_\mu^{\text{BLR}}$$



$$\Delta a_\mu^{\text{BLR}}(M_1, m_{\tilde{l}_L}, m_{\tilde{l}_R}; \mu) = \frac{\alpha_Y}{4\pi} \frac{m_\mu^2 M_1 \mu}{m_{\mu_L}^2 m_{\mu_R}^2} \tan\beta \cdot f_{\text{BLR}}(\{\mathbf{m}\})$$

large μ needed

$$\Delta a_\mu^{\rm SUSY} = \Delta a_\mu^{\rm WHL} + \Delta a_\mu^{\rm BHL} + \Delta a_\mu^{\rm BHR} + \Delta a_\mu^{\rm BLR}$$



$$\Delta a_\mu^{\rm BLR}(M_1, m_{\tilde{l}_L}, m_{\tilde{l}_R}; \mu) = \frac{\alpha_Y}{4\pi}\frac{m_\mu^2 M_1 \mu}{m_{\mu_L}^2 m_{\mu_R}^2}\tan\beta \cdot f_{\rm BLR}(\{\mathbf{m}\})$$

large μ needed

Constraints:

- charge breaking vacuum: $m^2_{\rm stau1} > 0$

❖ Stau mass² becomes negative or too small!

$$(\tilde{\tau}\ \text{mass matrix}) \sim \begin{pmatrix} m_{\tilde{\tau}_R}^2 & Y_\tau \mu \langle H_u \rangle \\ Y_\tau \mu \langle H_u \rangle & m_{\tilde{\tau}_L}^2 \end{pmatrix}$$

- LEP bound: $m_{\rm stau1} > 90$ GeV

- stau LSP: $m_{\rm stau1} > m_{\rm neutralino1}$

- Vacuum (meta-)stability:

$$\left|m^2_{\tilde{\ell}_{LR}}\right| \leq \left[1.01\times10^2\,\text{GeV}\sqrt{m_{\tilde{\ell}_L} m_{\tilde{\ell}_R}} + 1.01\times10^2\,\text{GeV}(m_{\tilde{\ell}_L} + 1.03 m_{\tilde{\ell}_R}) - 2.27\times10^4\,\text{GeV}^2 + \frac{2.97\times10^6\,\text{GeV}^3}{m_{\tilde{\ell}_L} + m_{\tilde{\ell}_R}} - 1.14\times10^8\,\text{GeV}^4\left(\frac{1}{m^2_{\tilde{\ell}_L}} + \frac{0.983}{m^2_{\tilde{\ell}_R}}\right)\right]$$

[Kitahara, Yoshinaga 13]; [Endo, Hamaguchi, Kitahara, Yoshinaga 13]

❖ **Overproduction of Bino-like neutralinos** in the early universe: $\Omega_{\tilde{\chi}_1^0} < \Omega_{\rm DM}$

slepton-coannihilation needed ⟹ $m_{\rm slepton} \sim m_{\rm Bino}$

Summary of g-2 in MSSM

$$\Delta a_\mu^{\rm SUSY} = \Delta a_\mu^{\rm WHL} + \Delta a_\mu^{\rm BHL} + \Delta a_\mu^{\rm BHR} + \Delta a_\mu^{\rm BLR}$$

$\Delta a_\mu^{\rm WHL}(M_2, \mu, m_{\tilde{l}_L})$

$\Delta a_\mu^{\rm BHL}(M_1, \mu, m_{\tilde{l}_L})$

$\Delta a_\mu^{\rm BHR}(M_1, \mu, m_{\tilde{l}_R})$

Higgsino, one gaugino, one slepton all must be light:

⇒ **LHC constraint with large $\not{E}_T$**

gaugino-Higgsino mixing ⇒ **DM direct detection**

$\Delta a_\mu^{\rm BLR}(M_1, m_{\tilde{l}_L}, m_{\tilde{l}_R}; \mu)$

large

Bino and both L and R sleptons must be light:

⇒ **LHC constraint with large $\not{E}_T$**

⇒ **Bino abundance** $\Omega_{\tilde{\chi}_1^0} < \Omega_{\rm DM}$

⇒ **Charged LSP, Vacuum stability**

Unstable Neutralino (Gravitino, RPV)

$$\Delta a_\mu^{\rm SUSY} = \Delta a_\mu^{\rm WHL} + \Delta a_\mu^{\rm BHL} + \Delta a_\mu^{\rm BHR} + \Delta a_\mu^{\rm BLR}$$

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gaugino-Higgsino mixing ⇒ ~~**DM direct detection**~~

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Bino and both L and R sleptons must be light:

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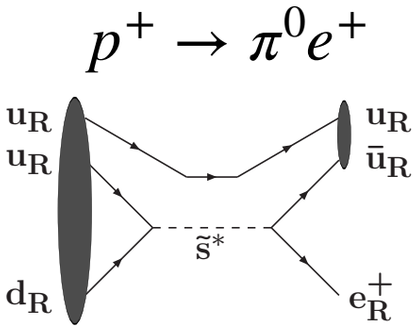
⇒ ~~**Bino abundance** $\Omega_{\tilde{\chi}_1^0} < \Omega_{\rm DM}$~~

⇒ **Charged LSP, Vacuum stability**

R-Parity Violation; UDD

$$W_{\rm RPV} = \underbrace{\lambda''_{ijk} U^c_i D^c_j D^c_k}_{\not B} + \underbrace{\lambda_{ijk} L_i L_j E^c_k + \lambda'_{ijk} L_i Q_j D^c_k + \kappa_i L_i H_u}_{\not L}$$



- Allowing both **B** and **L** violation leads to a rapid proton decay:

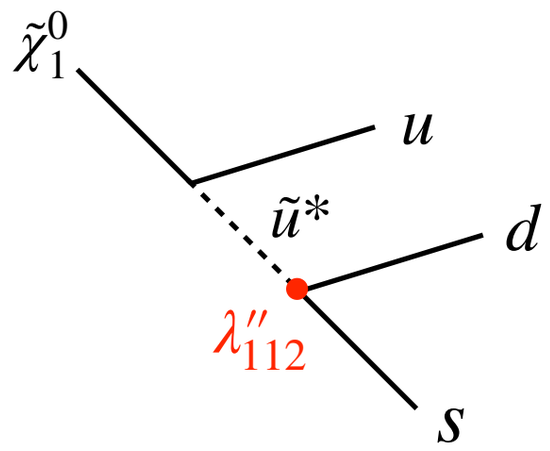
- We introduce only the **UDD** operator with: $\lambda''_{112} \neq 0$

- Constraint from K0-K0bar mixing can easily be satisfied:

$$|\lambda''_{112}\lambda''_{123}| \lesssim 2.8 \times 10^{-2} \left(\frac{m_{\tilde{s}_R,\tilde{u}_R}}{1\,\text{TeV}}\right)$$
$$|\lambda''_{112}\lambda''_{113}| \lesssim 1.2 \times 10^{-1} \left(\frac{m_{\tilde{d}_R,\tilde{u}_R}}{1\,\text{TeV}}\right)$$

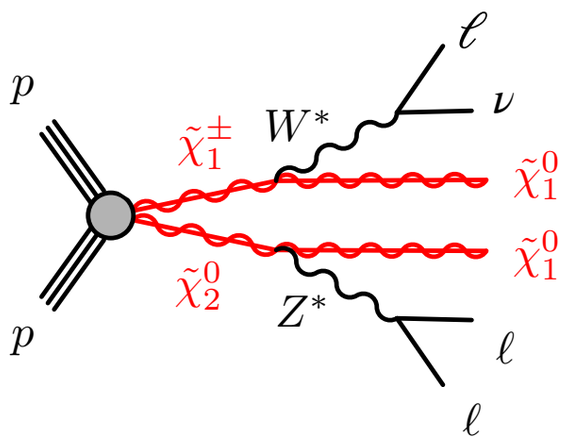
[1810.08228]

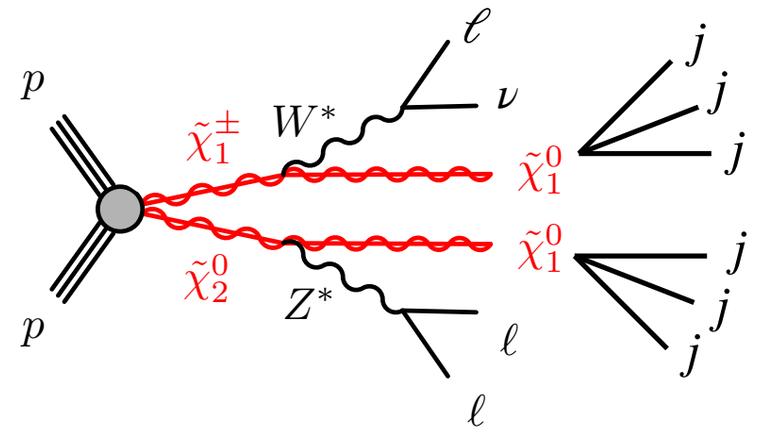
- **LHC signature is the most challenging:**
  no leptons, no b-jets in the neutralino decay



R-Parity Violation; UDD

neutralino LSP





RPV (UDD-type)

No missing energy, but multi-jet

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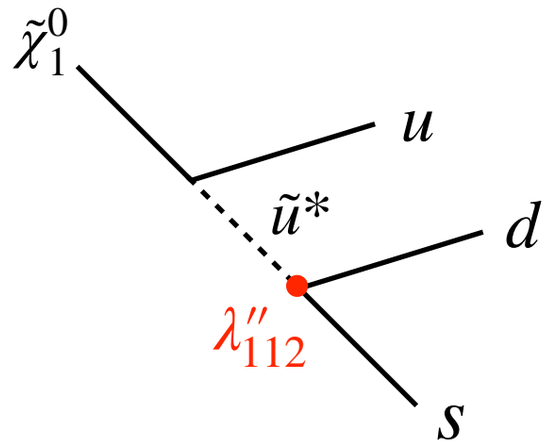
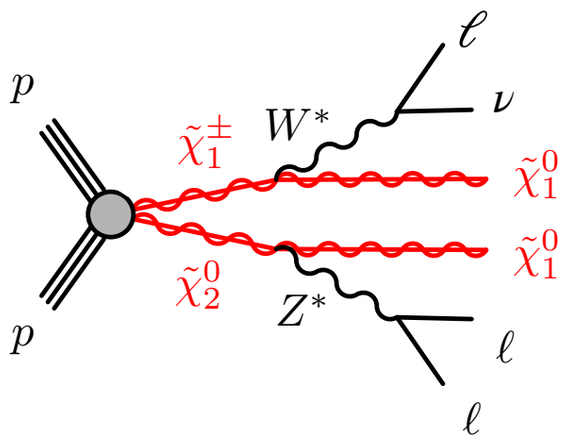
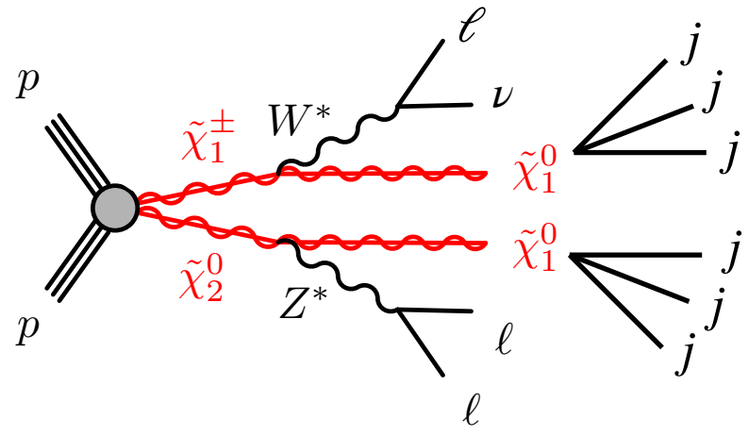


R-Parity Violation; UDD

neutralino LSP



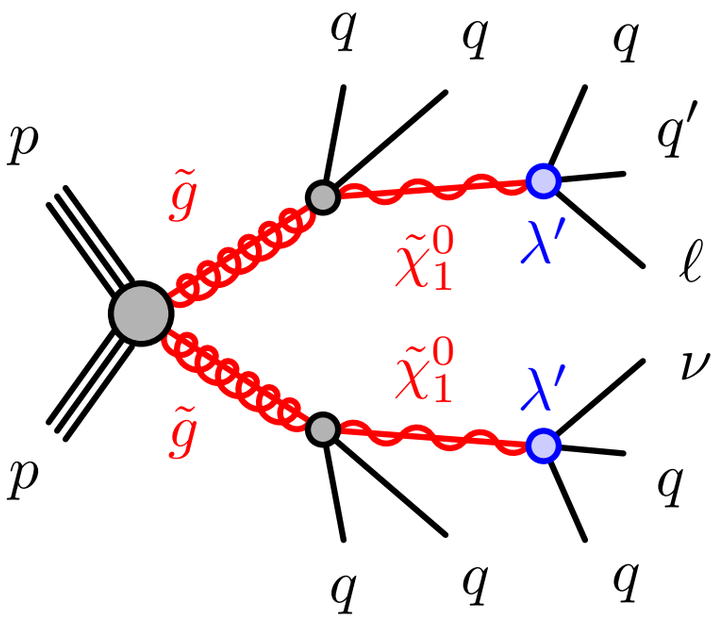


RPV (UDD-type)

No missing energy, but multi-jet

- There exist ATLAS and CMS analyses sensitive to such final states:

ATLAS [2106.09609]



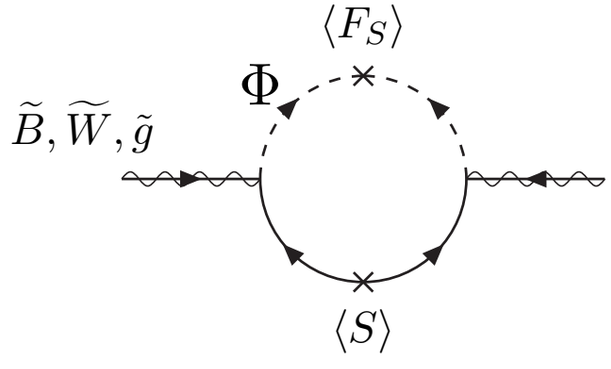
CMS [1709.05406]

Bin	Final state	Definition
1	2 SS leptons	0 jets, $M_{\mathrm{T}} > 100\,\mathrm{GeV}$ and $p_{\mathrm{T}}^{\mathrm{miss}} > 140\,\mathrm{GeV}$
2	2 SS leptons	1 jet , $M_{\mathrm{T}} < 100\,\mathrm{GeV}$, $p_{\mathrm{T}}^{\ell\ell} < 100\,\mathrm{GeV}$ and $p_{\mathrm{T}}^{\mathrm{miss}} > 200\,\mathrm{GeV}$
3	3 light leptons	$M_{\mathrm{T}} > 120\,\mathrm{GeV}$ and $p_{\mathrm{T}}^{\mathrm{miss}} > 200\,\mathrm{GeV}$
4	3 light leptons	$p_{\mathrm{T}}^{\mathrm{miss}} > 250\,\mathrm{GeV}$
5	2 light leptons and 1 tau	$M_{\mathrm{T2}}(\ell_1, \tau) > 50\,\mathrm{GeV}$ and $p_{\mathrm{T}}^{\mathrm{miss}} > 200\,\mathrm{GeV}$
6	1 light lepton and 2 taus	$M_{\mathrm{T2}}(\ell, \tau_1) > 50\,\mathrm{GeV}$ and $p_{\mathrm{T}}^{\mathrm{miss}} > 200\,\mathrm{GeV}$
7	1 light lepton and 2 taus	$p_{\mathrm{T}}^{\mathrm{miss}} > 75\,\mathrm{GeV}$
8	more than 3 leptons	$p_{\mathrm{T}}^{\mathrm{miss}} > 200\,\mathrm{GeV}$

Gravitino LSP

- In the gauge-mediated SUSY breaking (GMSB) scenario, **light gravitino is motivated by naturalness**:

$$\delta m_h^2 \propto m_{SUSY}^2 \ln\left(\frac{\Lambda_{\rm mess}}{M_{\rm PL}}\right) \qquad m_{3/2} = \frac{4\pi}{\sqrt{3}\alpha_W} M_2 \frac{\Lambda_{\rm mess}}{M_{\rm PL}}$$



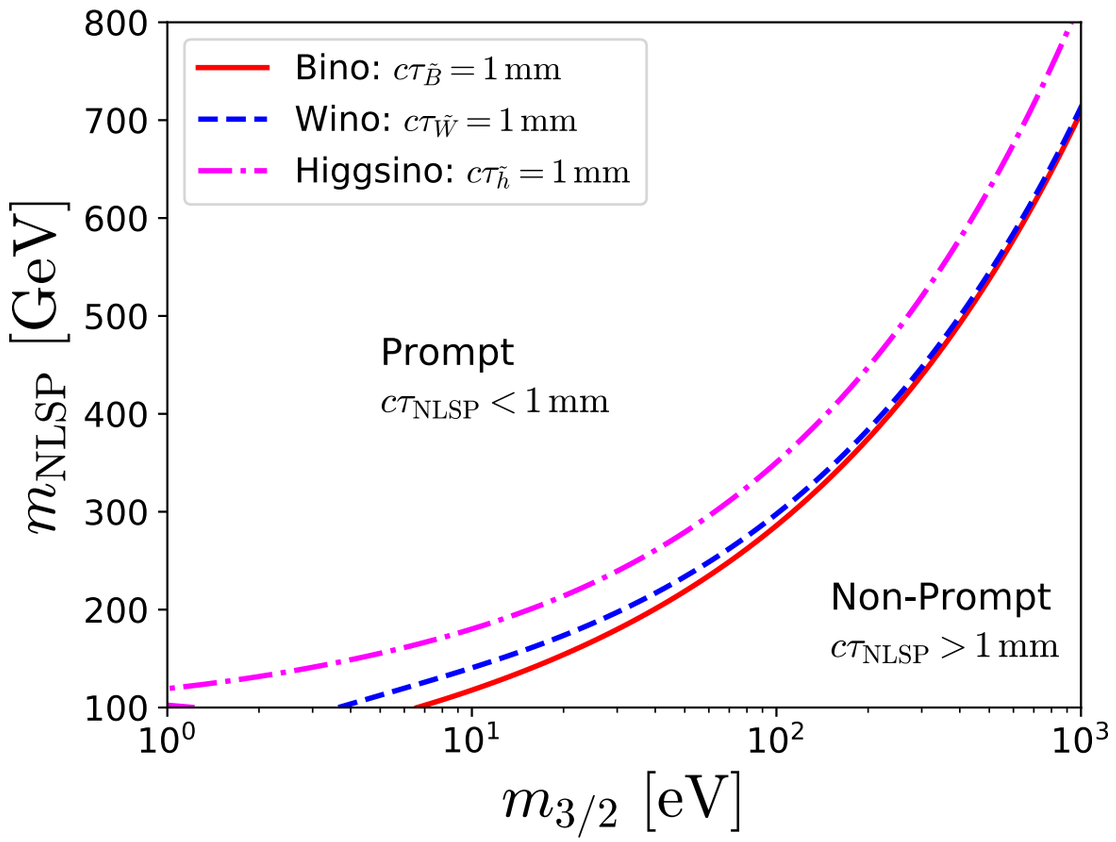
- The decay rate of the NLSP neutralino into the gravitino can be calculated. For light gravitinos (< 10-100 eV), the **neutralino decays are prompt**.

$$\Gamma(\tilde{\chi}_1^0 \to \tilde{G}\gamma) = \left|N_{11}c_W + N_{12}s_W\right|^2 \mathcal{A},$$

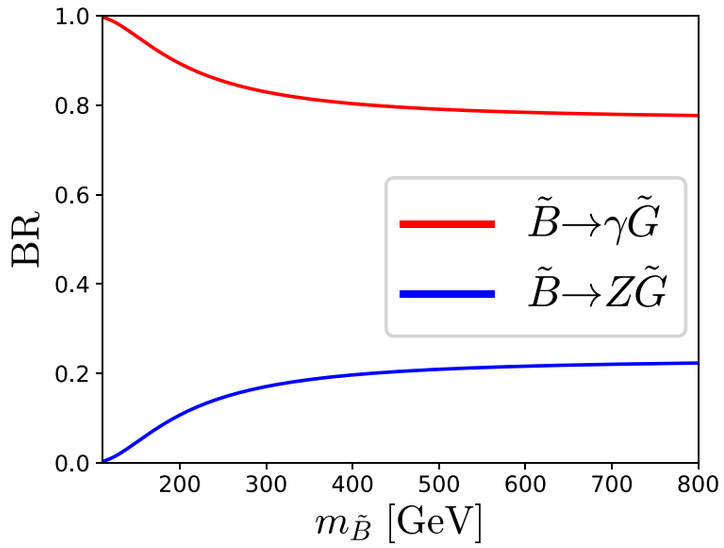
$$\Gamma(\tilde{\chi}_1^0 \to \tilde{G}Z) = \left(\left|N_{12}c_W - N_{11}s_W\right|^2 + \frac{1}{2}\left|N_{13}c_\beta - N_{14}s_\beta\right|^2\right)\left(1 - \frac{m_Z^2}{m_{\tilde{\chi}_1^0}^2}\right)^4 \mathcal{A},$$

$$\Gamma(\tilde{\chi}_1^0 \to \tilde{G}h) = \frac{1}{2}\left|N_{13}c_\beta + N_{14}s_\beta\right|^2\left(1 - \frac{m_h^2}{m_{\tilde{\chi}_1^0}^2}\right)^4 \mathcal{A},$$

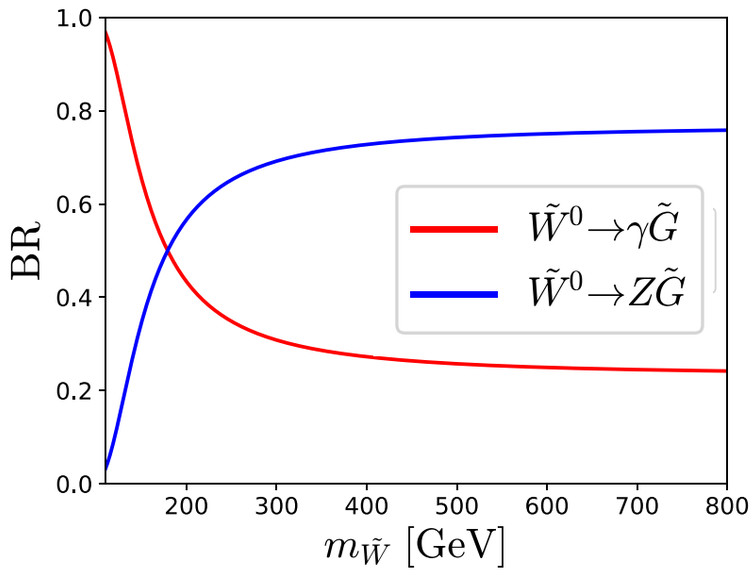
$$\mathcal{A} = \frac{m_{\tilde{\chi}_1^0}^5}{16\pi m_{3/2}^2 M_{\rm pl}^2} \sim \frac{1}{0.3\,\text{mm}}\left(\frac{m_{\tilde{\chi}_1^0}}{100\,\text{GeV}}\right)^5\left(\frac{m_{3/2}}{10\,\text{eV}}\right)^{-2}$$



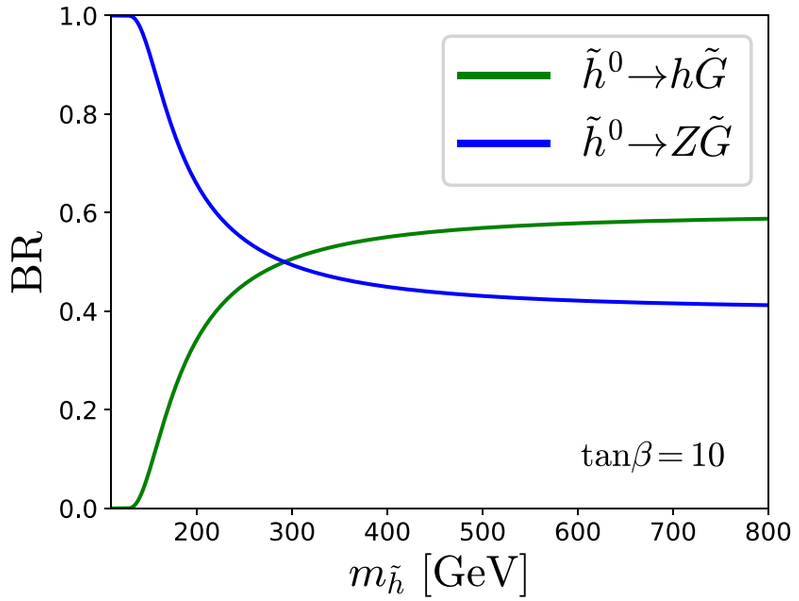
Bino-like

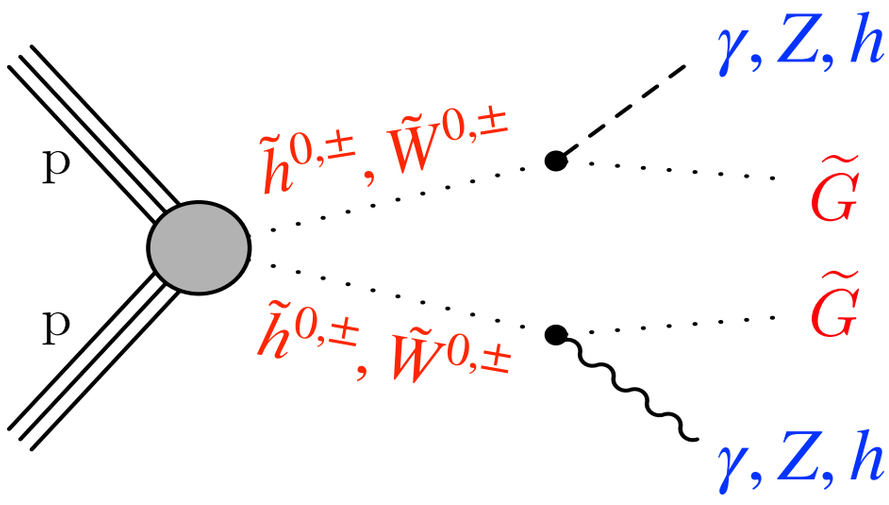


Wino-like

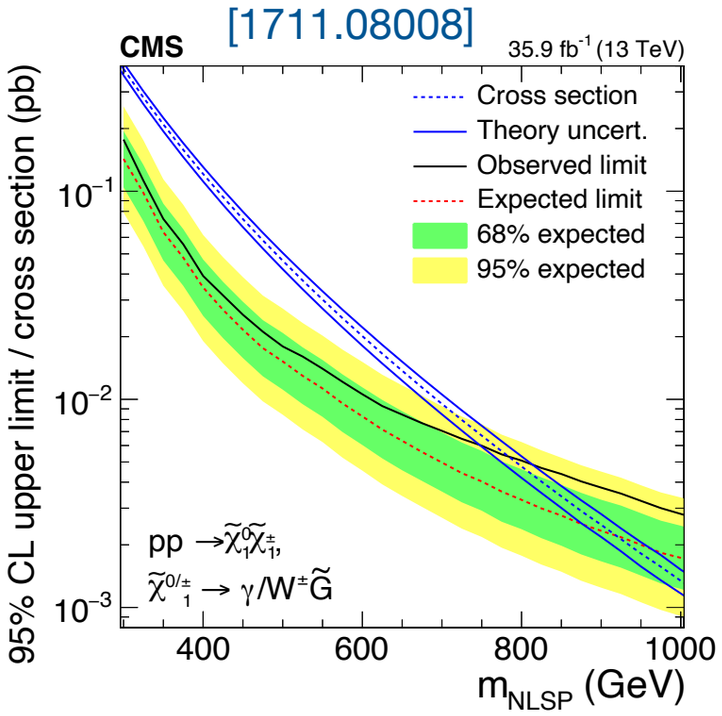


Higgsino-like

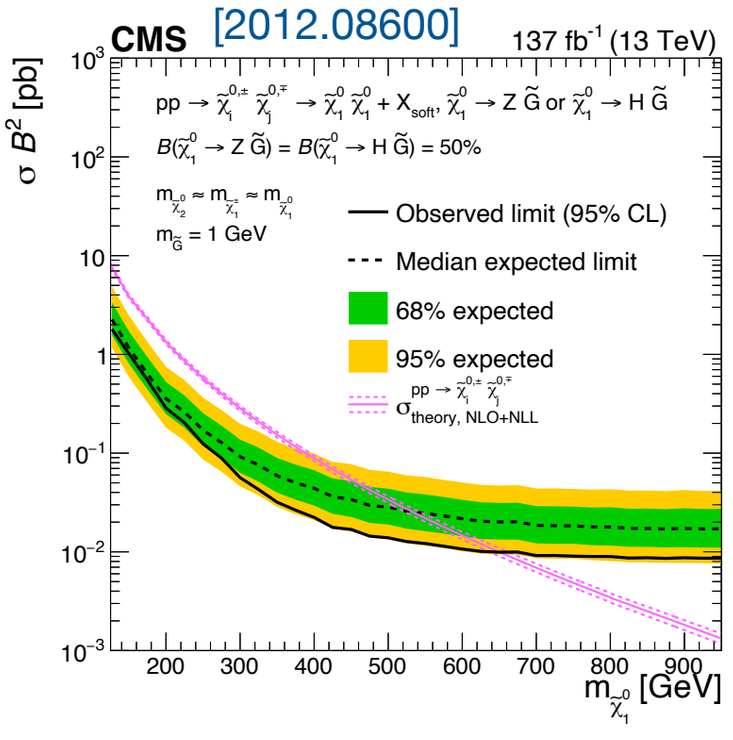




[1711.08008]



[2012.08600]



- Higgsino, Wino direct production excluded up to ~ 700GeV
- SUSY g-2 requires Higgsino or Wino with m < 600 GeV

SUSY $(g-2)_\mu$ incompatible with LHC

Analysis Framework

SUSY g-2: 1-loop + leading 2-loop GM2Calc [Eur.Phys.J. C76 (2016) no.2, 62]

Neutralino abundance, Direct Detection: MicrOMEGAs [2003.08621]

Decay of SUSY particles: SUSY-HIT [hep-ph/0609292]

LHC constraints:

- **MSSM:** ① Mapping simplified model limits to the model point (σ BR)
- **RPV:** ② Pythia 8 + CheckMATE 2 [1907.09874], [1611.09856]
- **Gravitino LSP:** Both ① and ②

Results are preliminary

List of ATLAS & CMS searches included in our analysis

13 TeV

Name	E/TeV	$\mathcal{L}$/fb^{-1}	Description
atlas_1604_01306	13	3.2	Monophoton
atlas_1605_09318	13	3.3	3 b-jets + 0-1 lepton + MET
atlas_1609_01599	13	36	Monophoton
atlas_1704_03848	13	36	Monophoton
atlas_conf_2015_082	13	3.2	2 leptons (Z) + jets + MET
atlas_conf_2016_013	13	3.2	1 lepton + jets (4 tops, VVL quarks)
atlas_conf_2016_050	13	13.3	1 lepton + (b) jets + MET
atlas_conf_2016_054	13	13.3	1 lepton + (b) jets + MET
atlas_conf_2016_076	13	13.3	2 lepton + jets + MET
atlas_conf_2016_096	13	13.3	Multi-lepton + MET
atlas_conf_2017_060	13	36	Monojet
atlas_conf_2016_066	13	13.3	Photons, jets and MET
atlas_1712_08119	13	36	soft leptons (compressed EWKinos)
atlas_1712_02332	13	36	squarks and gluinos, 0 lepton, 2-6 jets
atlas_1709_04183	13	36	Jets + MET (stops)
atlas_1802_03158	13	36	search for GMSB with photons
atlas_1708_07875	13	36	EWKino search with taus and MET
atlas_1706_03731	13	36	Multilepton + Jets + MET (RPC and RPV)
atlas_1908_08215	13	36	2 leptons + MET (EWKinos)
atlas_1909_08457	13	139	SS lepton + MET (squark, gluino)
atlas_conf_2019_040	13	139	Jets + MET (squark, gluino)
atlas_conf_2019_020	13	139	3 leptons (EWKino)
atlas_1803_02762	13	36	2 or 3 leptons (EWKino)
atlas_conf_2018_041	13	80	Multi-b-jets (stops, sbottoms)
atlas_2101_01629	13	139	1 lepton + jets + MET
atlas_conf_2020_048	13	139	Monojet
atlas_2004_14060	13	139	$t\bar{t}$ + MET
atlas_1908_03122	13	139	Higgs bosons + b-jets + MET
atlas_2103_11684	13	139	4 or more leptons (RPV, GMSB)
atlas_2106_09609	13	139	Multijets + leptons (RPV)
atlas_1911_06660	13	139	Search for Direct Stau Production
cms_pas_sus_15_011	13	2.2	2 leptons + jets + MET
cms_sus_16_039	13	35.9	electrowekinos in multilepton final state
cms_sus_16_025	13	12.9	electroweakino and stop compressed spectra
cms_sus_16_048	13	35.9	two soft opposite sign leptons

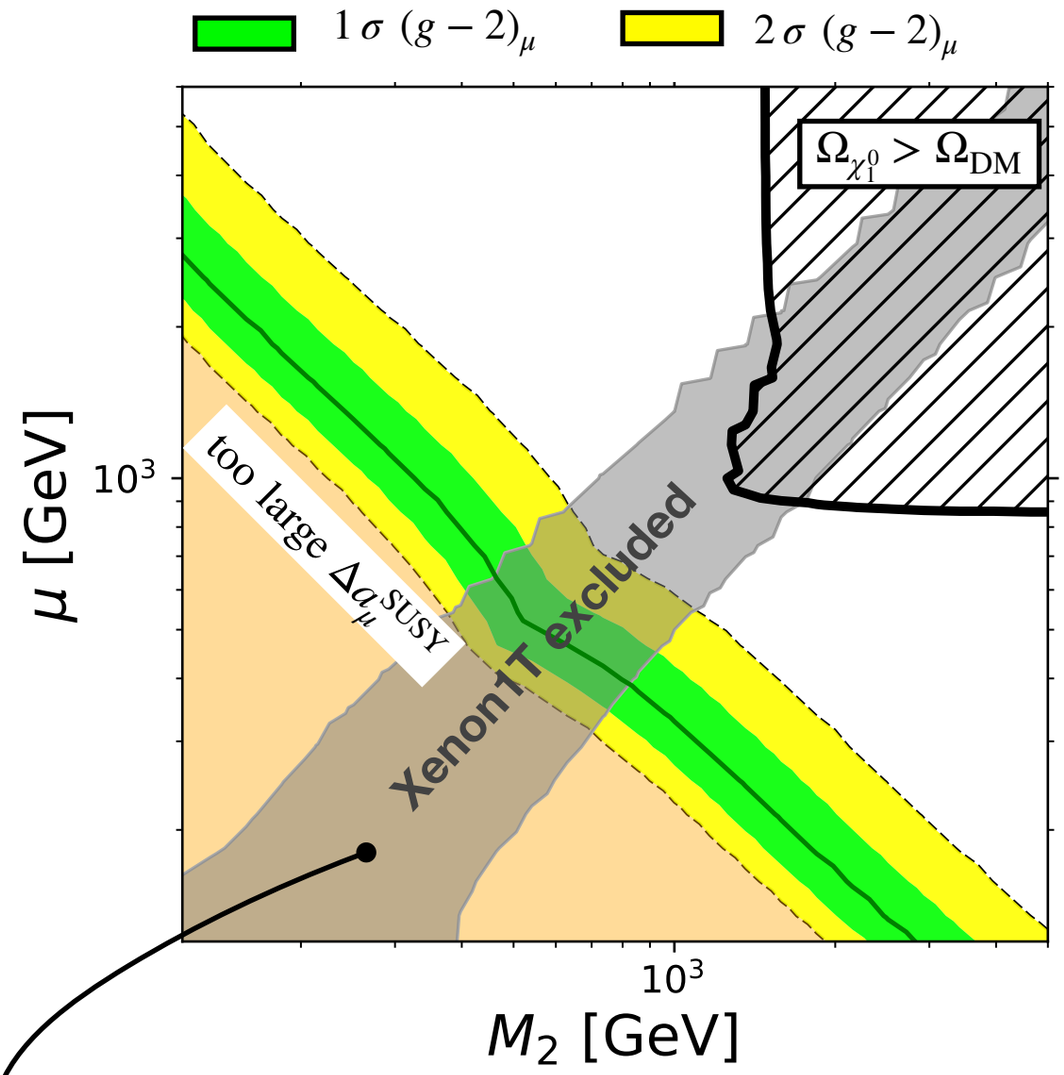
8 TeV

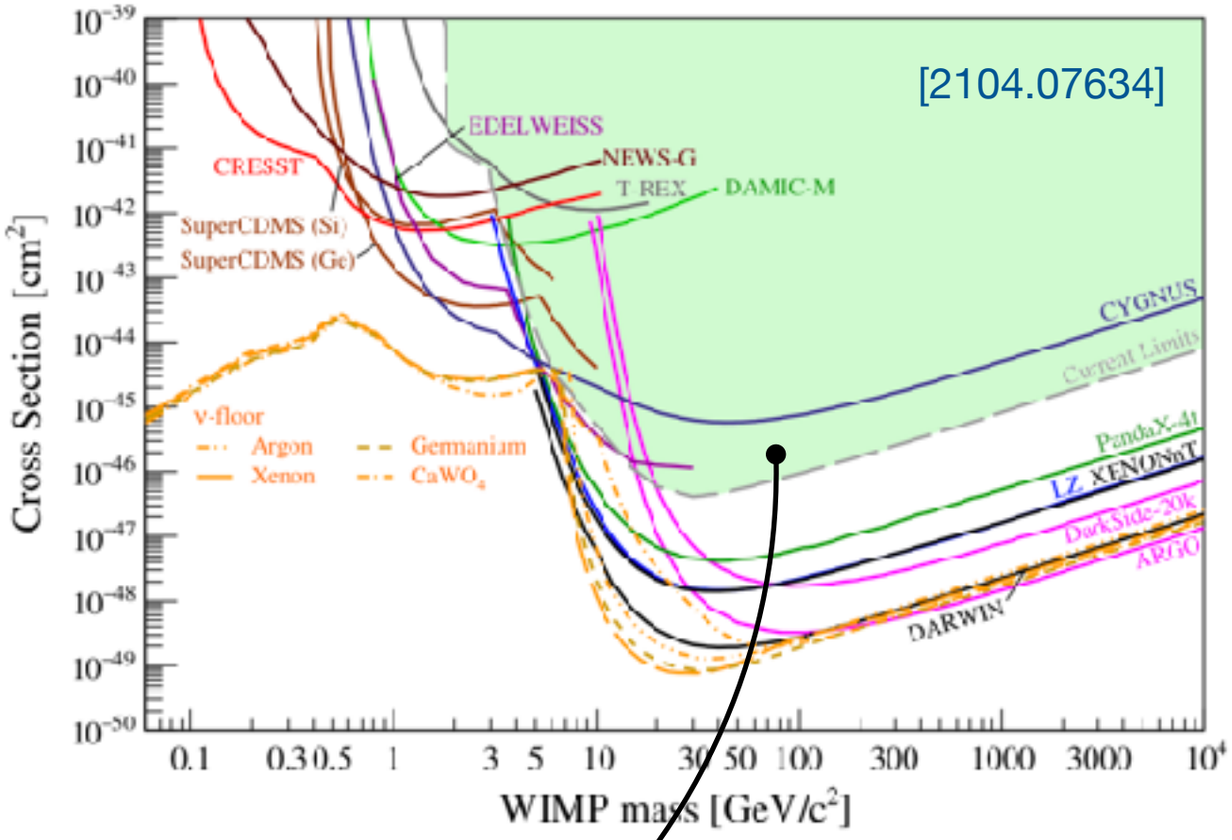
Name	E/TeV	$\mathcal{L}$/fb^{-1}	Description
atlas_1308_1841	8	20.3	0 lepton + $\geq$ 7 jets + MET
atlas_1308_2631	8	20.1	0 leptons + 2 b-jets + MET
atlas_1402_7029	8	20.3	3 leptons + MET (chargino+neutralino)
atlas_1403_4853	8	20.3	2 leptons + MET (direct stop)
atlas_1403_5222	8	20.3	stop production with Z boson and b-jets
atlas_1404_2500	8	20.3	Same sign dilepton or 3 lepton
atlas_1405_7875	8	20.3	0 lepton + 2-6 jets + MET
atlas_1407_0583	8	20.3	ATLAS, 1 lepton + (b-)jets + MET (stop)
atlas_1407_0608	8	20.3	Monojet or charm jet (stop)
atlas_1411_1559	8	20.3	monophoton plus MET
atlas_1501_07110	8	20.3	1 lepton + 125GeV Higgs + MET
atlas_1502_01518	8	20.3	Monojet + MET
atlas_1503_03290	8	20.3	2 leptons + jets + MET
atlas_1506_08616	8	20.3	di-lepton and 2b-jets + lepton
atlas_1507_05493	8	20.3	photonic signatures of gauge-mediated SUSY
atlas_conf_2012_104	8	20.3	1 lepton + $\geq$ 4 jets + MET
atlas_conf_2013_024	8	20.3	0 leptons + 6 (2 b-)jets + MET
atlas_conf_2013_049	8	20.3	2 leptons + MET
atlas_conf_2013_061	8	20.3	0-1 leptons + $\geq$ 3 b-jets + MET
atlas_conf_2013_089	8	20.3	2 leptons (razor)
atlas_conf_2015_004	8	20.3	invisible Higgs decay in VBF
atlas_1403_5294	8	20.3	2 leptons + MET, (SUSY electroweak)
atlas_higg_2013_03	8	20.3	2 leptons + MET, (invisible Higgs)
atlas_1502_05686	8	20.3	search for massive sparticles decaying to many jets
cms_1303_2985	8	11.7	α_T + b-jets
cms_1408_3583	8	19.7	monojet + MET
cms_1502_06031	8	19.4	2 leptons, jets, MET (only on-Z)
cms_1504_03198	8	19.7	1 lepton, $\geq$ 3 jets, $\geq$ 1 b-jet, MET (DM + 2 top)
cms_sus_13_016	8	19.5	OS lepton 3+ b-tags

WHL (MSSM)

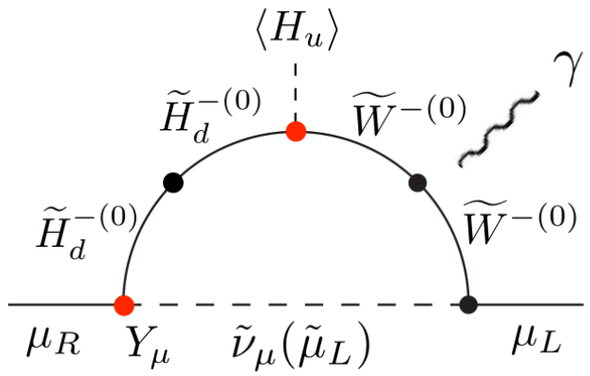
$$m_{\tilde{l}_L} = \min(M_2, \mu) + 20\,\text{GeV}$$

$$\tan\beta = 50, \quad M_1 = m_{\tilde{l}_R} = 10\,\text{TeV}$$





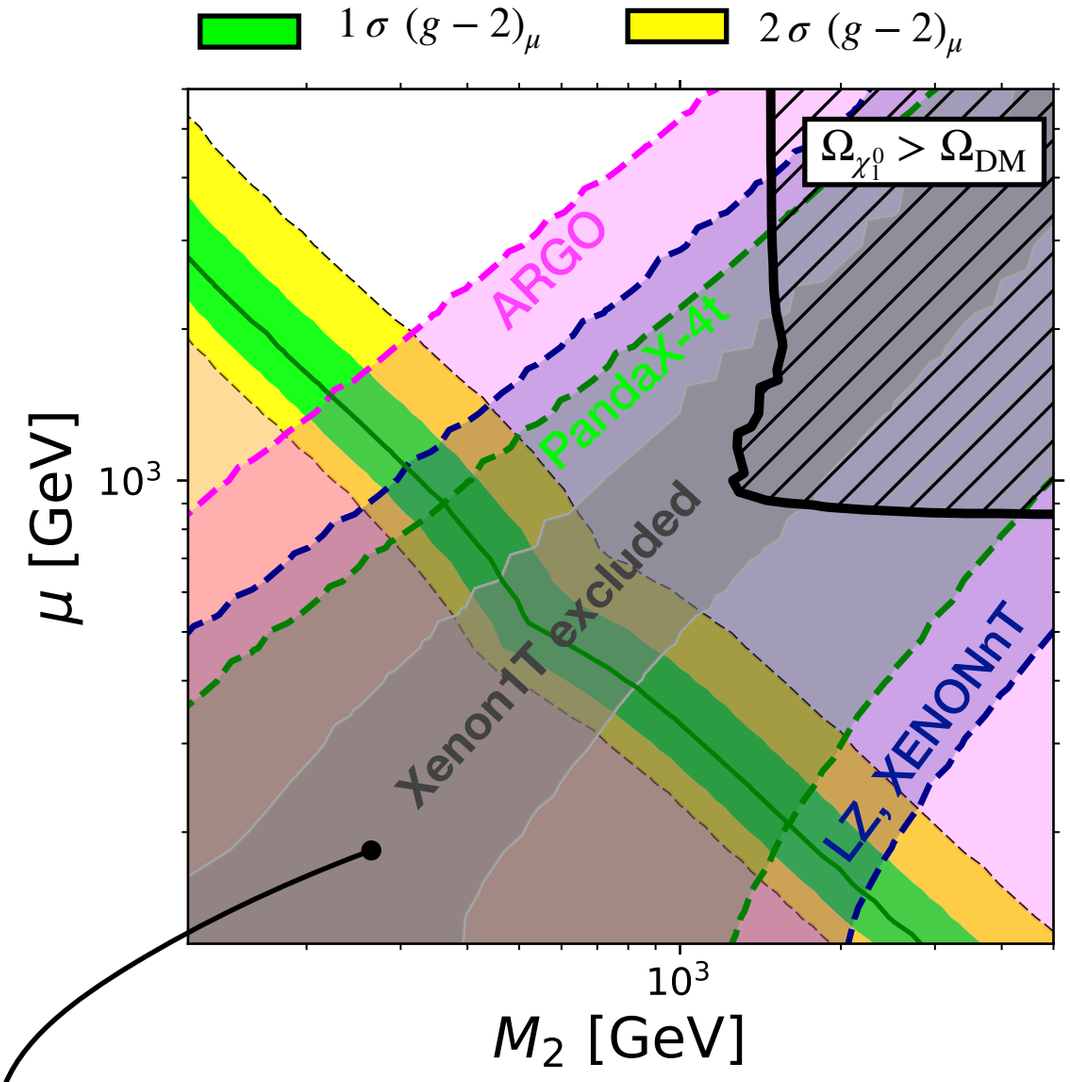
$$\sigma^{\rm SI}_{\chi N\to\chi N}(m_{\tilde{\chi}_1^0}) \cdot \frac{\Omega_{\tilde{\chi}_1^0}}{\Omega_{\rm DM}} > \sigma^{\rm SI}_{\rm Xenon1T}(m_{\rm DM})$$

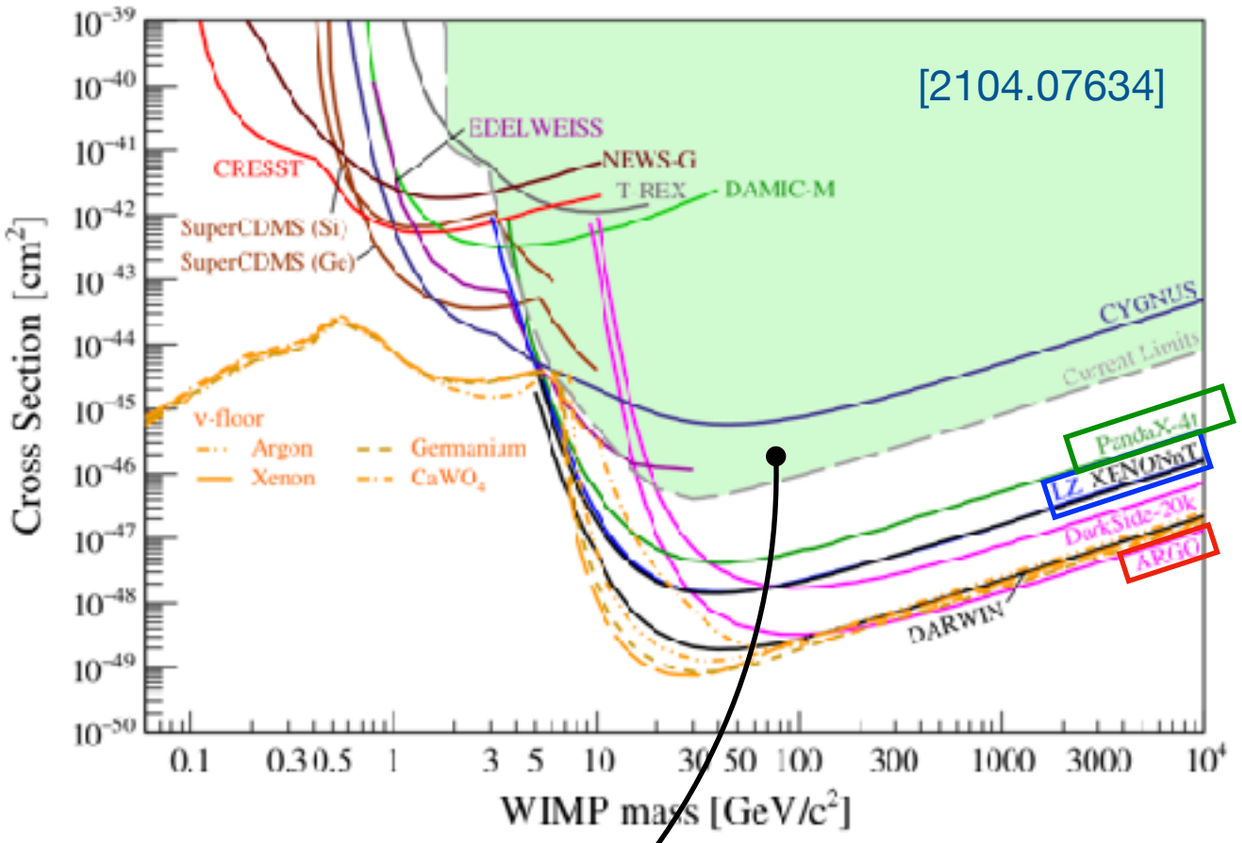


WHL

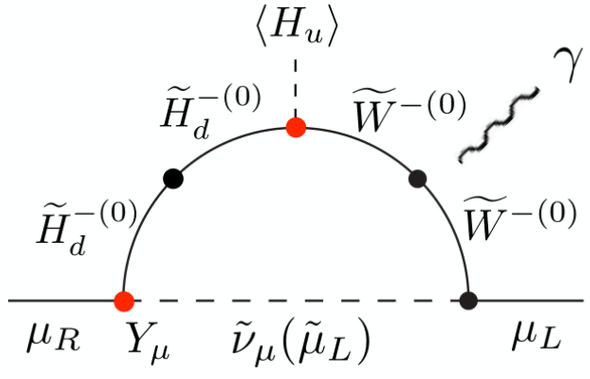
WHL (MSSM, future DM-DD)

$$m_{\tilde{l}_L} = \min(M_2, \mu) + 20\,\text{GeV}$$
$$\tan\beta = 50, \quad M_1 = m_{\tilde{l}_R} = 10\,\text{TeV}$$





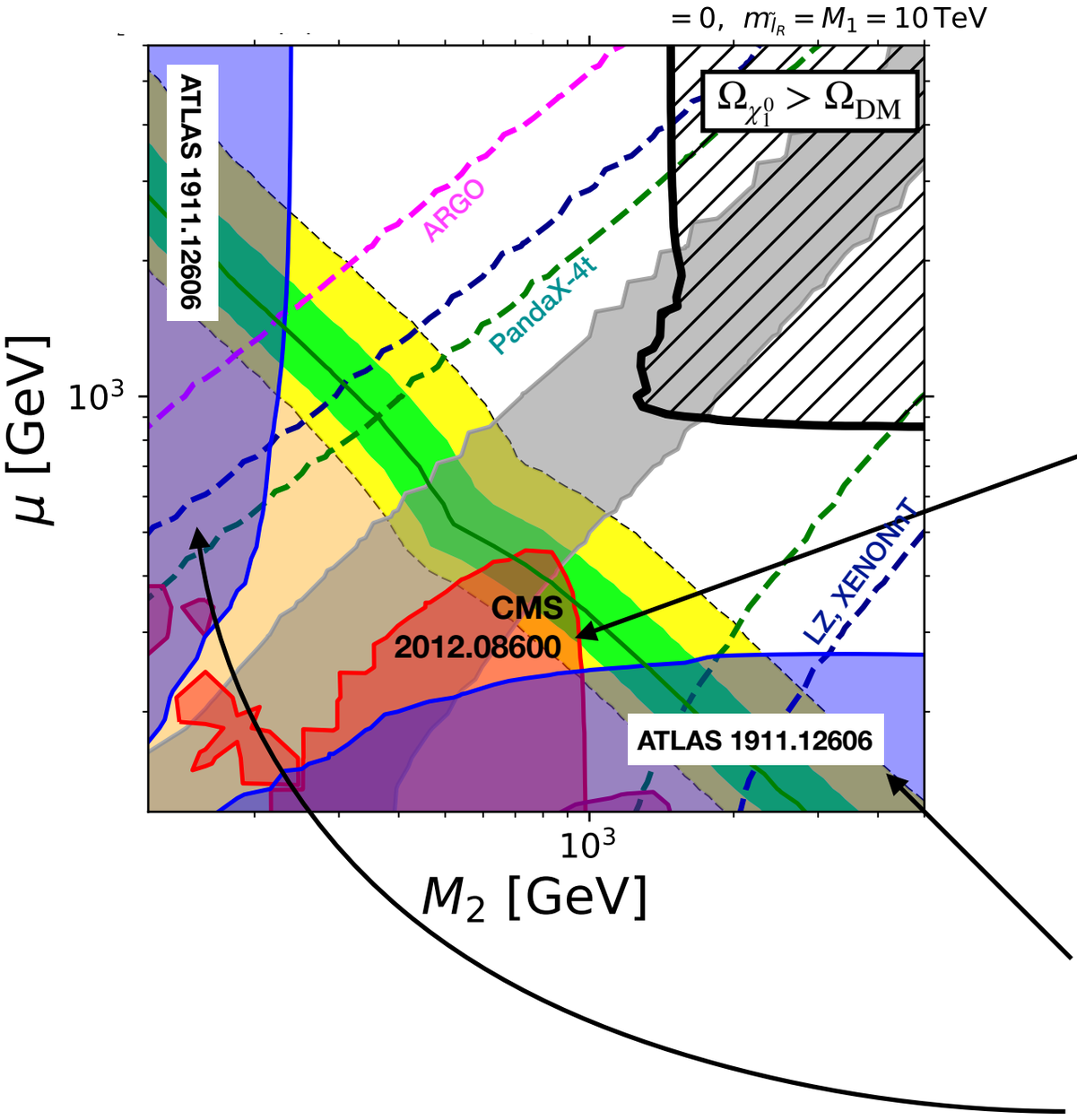
$$\sigma^{\rm SI}_{\chi N\to\chi N}(m_{\tilde{\chi}_1^0}) \cdot \frac{\Omega_{\tilde{\chi}_1^0}}{\Omega_{\rm DM}} > \sigma^{\rm SI}_{\rm Xenon1T}(m_{\rm DM})$$



WHL

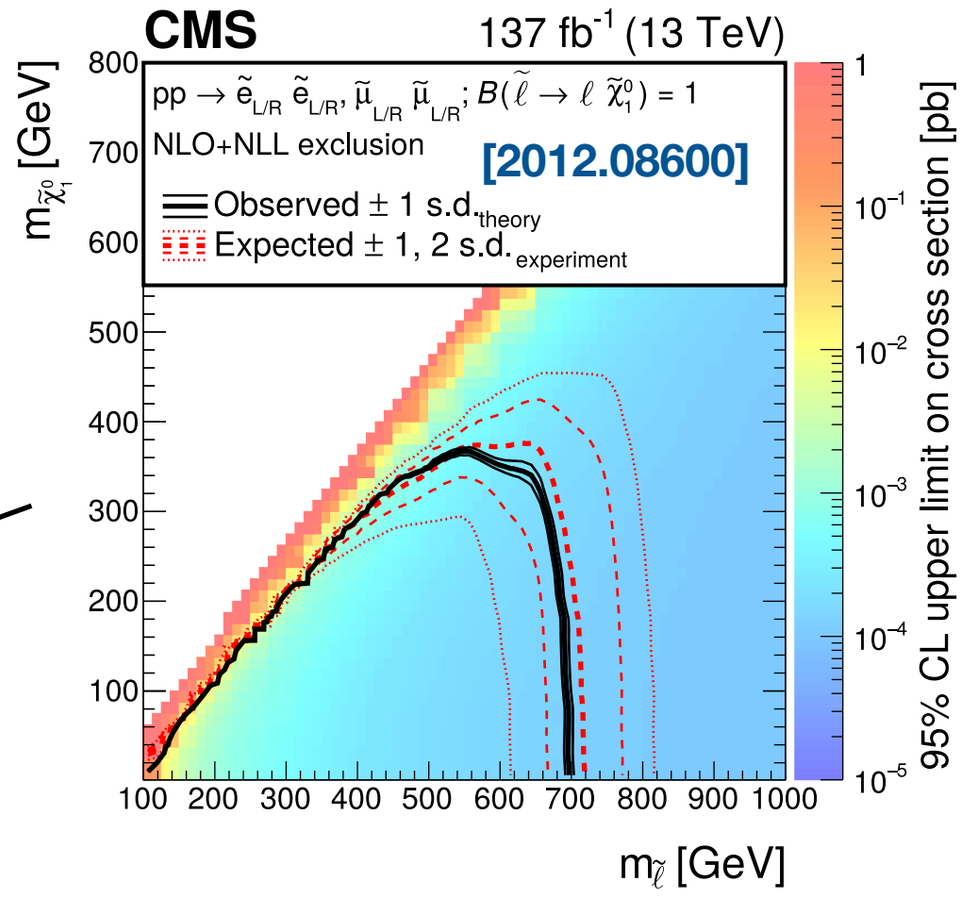
WHL (MSSM, LHC)

$$pp \to \widetilde{W}\widetilde{W},\ \widetilde{W}^{0,\pm} \to \ell + (\tilde{\ell}, \tilde{\nu})$$

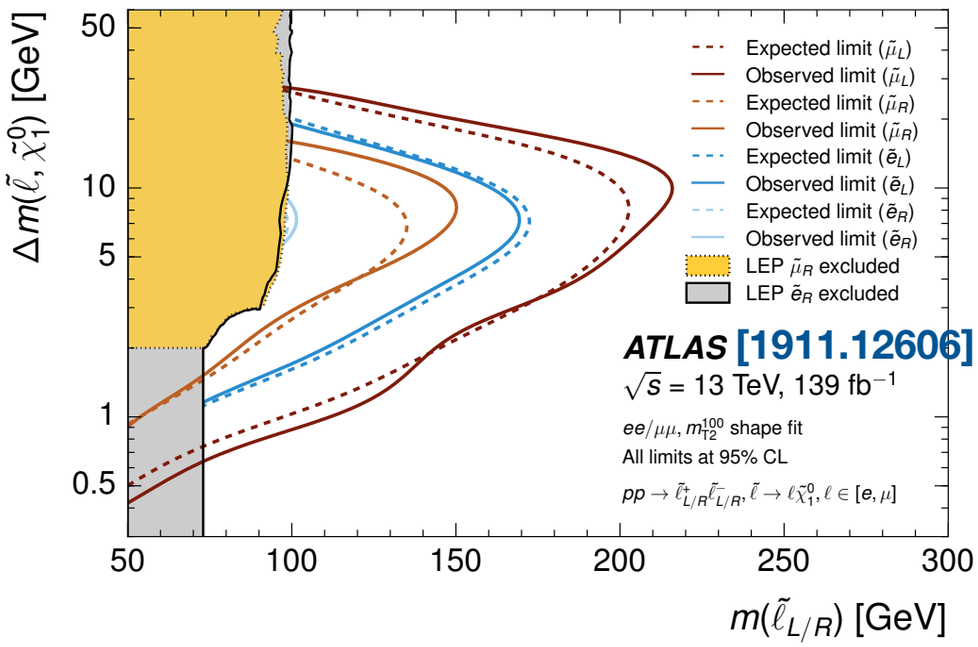


$$m_{\tilde{l}_L} = \min(M_2, \mu) + 20\,\text{GeV}$$

$$\tan\beta = 50,\ \ M_1 = m_{\tilde{l}_R} = 10\,\text{TeV}$$

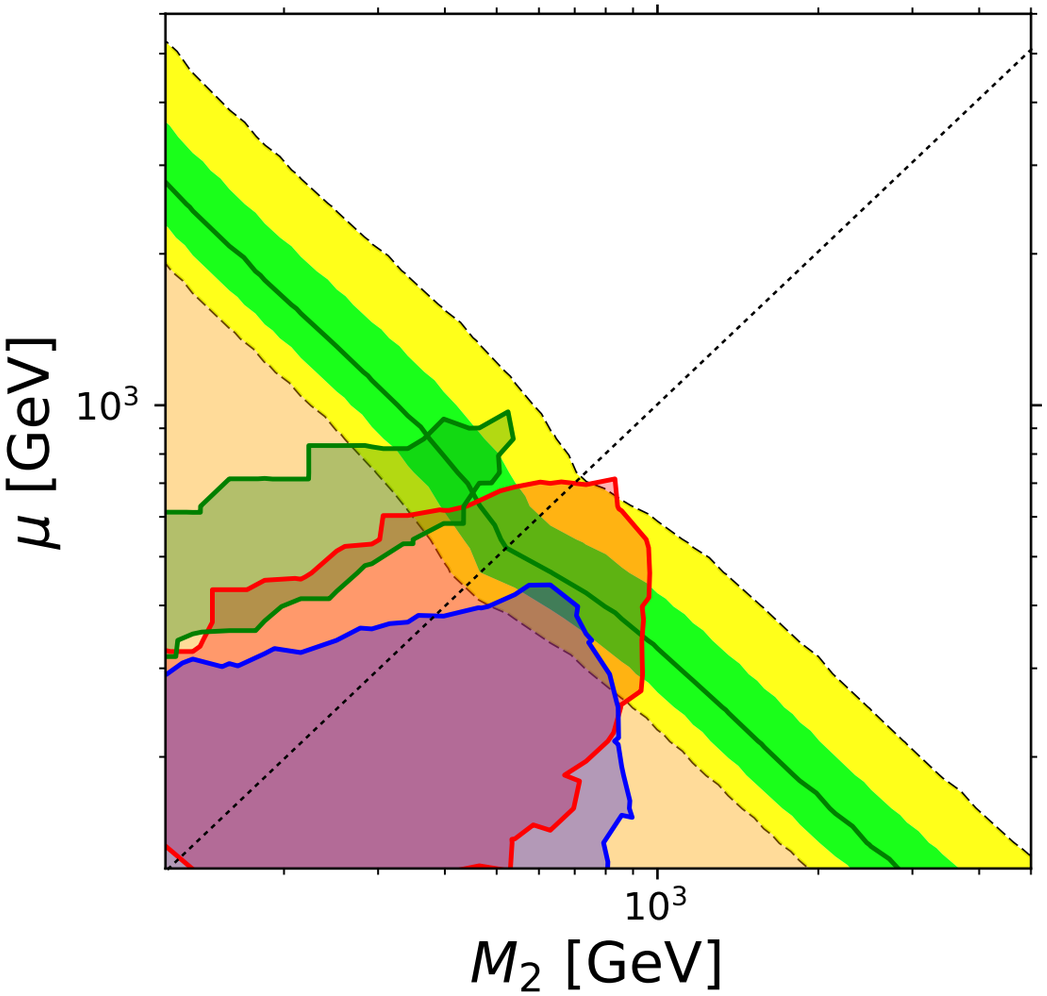


$$pp \to \tilde{\ell}\tilde{\ell},\ \tilde{\ell} \to \ell + \tilde{\chi}_1^0$$

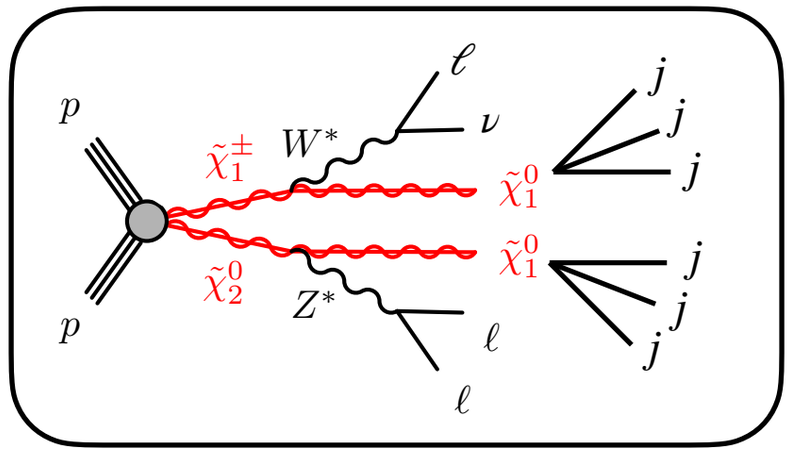


WHL (RPV UDD)

$$m_{\tilde{l}_L} = \min(M_2, \mu) + 20\,\text{GeV}$$
$$\tan\beta = 50, \quad M_1 = m_{\tilde{l}_R} = 10\,\text{TeV}$$

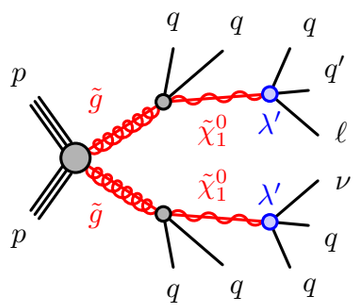


$pp \to W^{\pm}W^{0,\mp},\ \tilde{h}^{0,\pm}\tilde{h}^{0,\mp}$



soft lepton + multi-jet final state

More g-2 region available due to absence of DM constraints



RPV ATLAS13 139/fb [2106.09609]

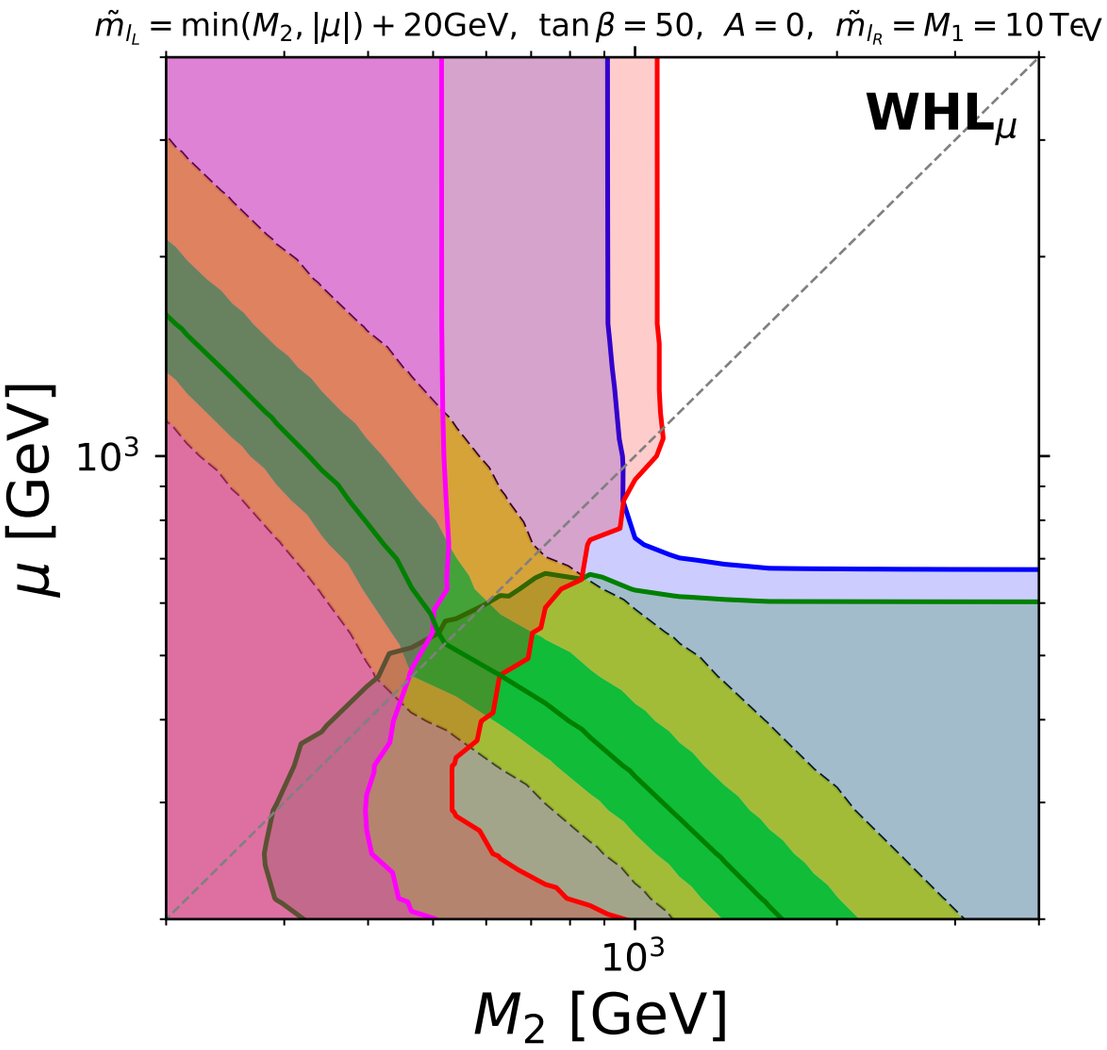
Multi & SS-leptons CMS13 36/fb [1709.05406]

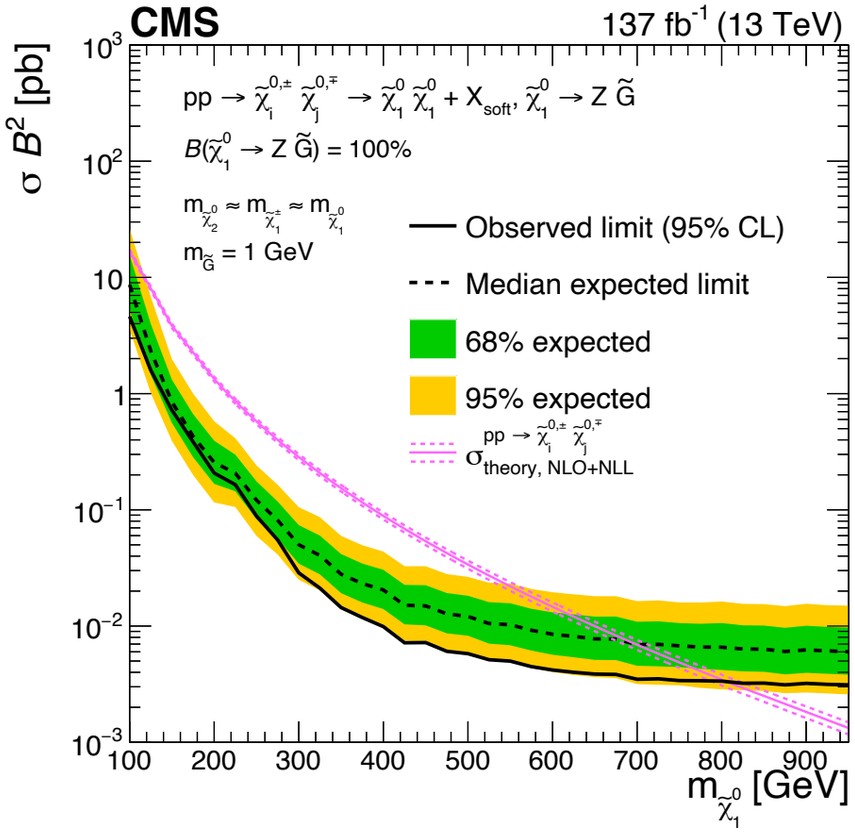
Multijet ATLAS13 139/fb [2106.09609]

Bin	Final state	Definition
1	2 SS leptons	0 jets, $M_{\rm T} > 100\,\text{GeV}$ and $p_{\rm T}^{\rm miss} > 140\,\text{GeV}$
2	2 SS leptons	1 jet , $M_{\rm T} < 100\,\text{GeV}$, $p_{\rm T}^{\ell\ell} < 100\,\text{GeV}$ and $p_{\rm T}^{\rm miss} > 200\,\text{GeV}$
3	3 light leptons	$M_{\rm T} > 120\,\text{GeV}$ and $p_{\rm T}^{\rm miss} > 200\,\text{GeV}$
4	3 light leptons	$p_{\rm T}^{\rm miss} > 250\,\text{GeV}$
5	2 light leptons and 1 tau	$M_{\rm T2}(\ell_1, \tau) > 50\,\text{GeV}$ and $p_{\rm T}^{\rm miss} > 200\,\text{GeV}$
6	1 light lepton and 2 taus	$M_{\rm T2}(\ell, \tau_1) > 50\,\text{GeV}$ and $p_{\rm T}^{\rm miss} > 200\,\text{GeV}$
7	1 light lepton and 2 taus	$p_{\rm T}^{\rm miss} > 75\,\text{GeV}$
8	more than 3 leptons	$p_{\rm T}^{\rm miss} > 200\,\text{GeV}$

WHL (Gravitino LSP)

$$m_{\tilde{l}_L} = \min(M_2, \mu) + 20\,\text{GeV}$$
$$\tan\beta = 50, \quad M_1 = m_{\tilde{l}_R} = 10\,\text{TeV}$$





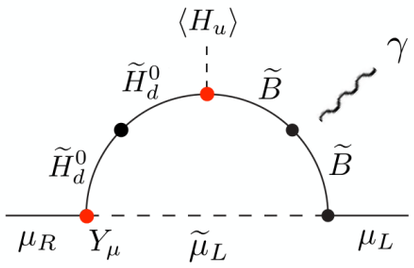
$[\gamma\tilde{G}][\gamma\tilde{G}]$ CMS $\gamma + \not{E}_T$ [1711.08008]

$[\gamma\tilde{G}][Z(h)\tilde{G}]$ CMS $\gamma + \not{E}_T$ [1711.08008]

$[Z\tilde{G}][Z\tilde{G}]$ CMS $\ell^+\ell^-$ [2012.08600]

$[h\tilde{G}][Z\tilde{G}]$ CMS $\ell^+\ell^-$ [2012.08600]

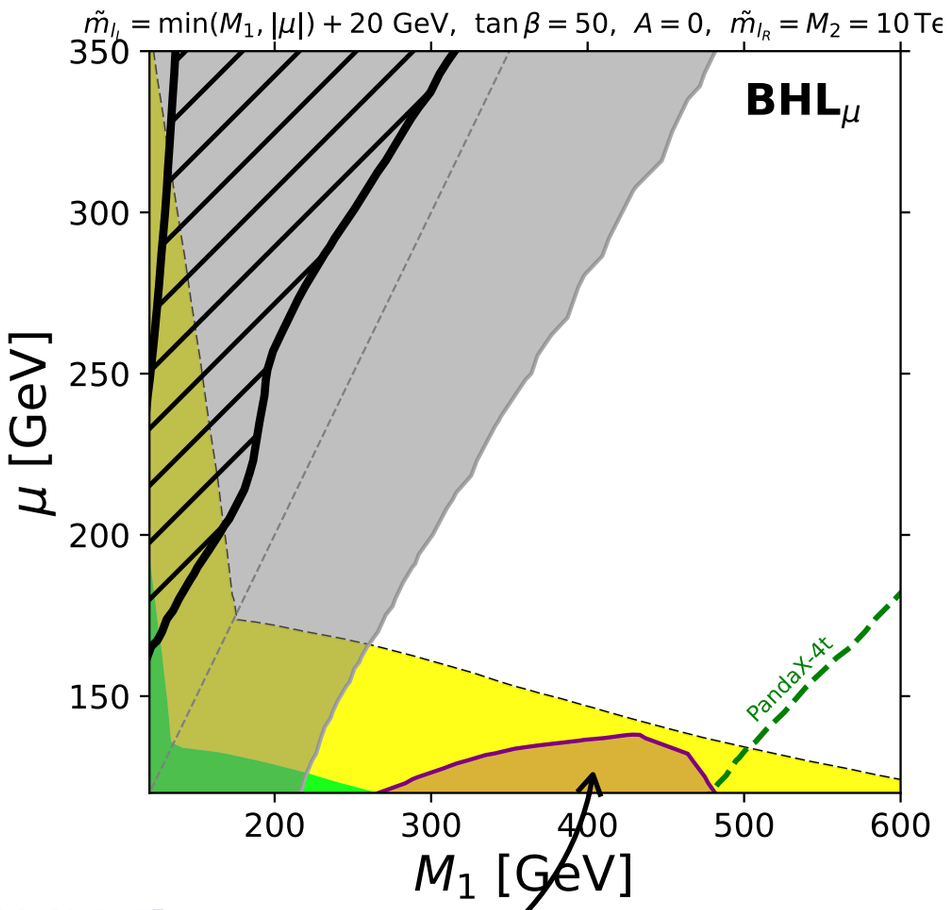
MSSM



BHL

$$m_{\tilde{l}_L} = \min(M_1, \mu) + 20\,\text{GeV}$$

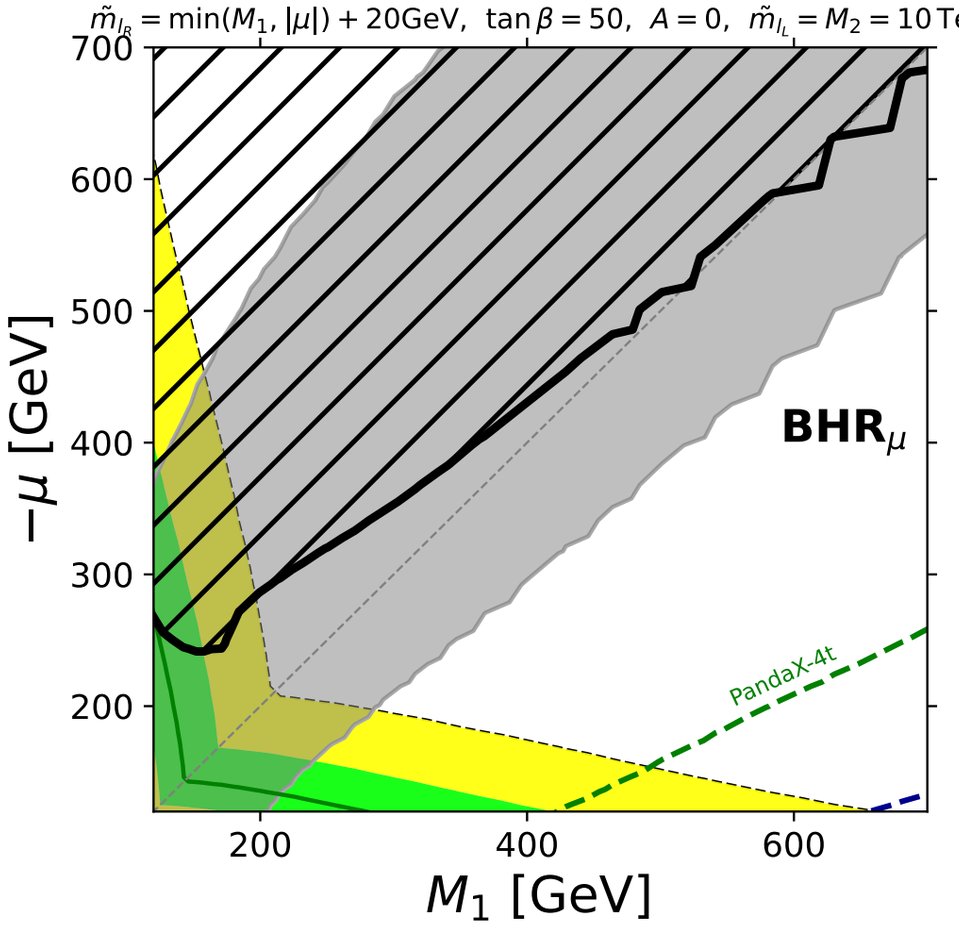
$$\tan\beta = 50, \quad M_2 = m_{\tilde{l}_R} = 10\,\text{TeV}$$



BHR

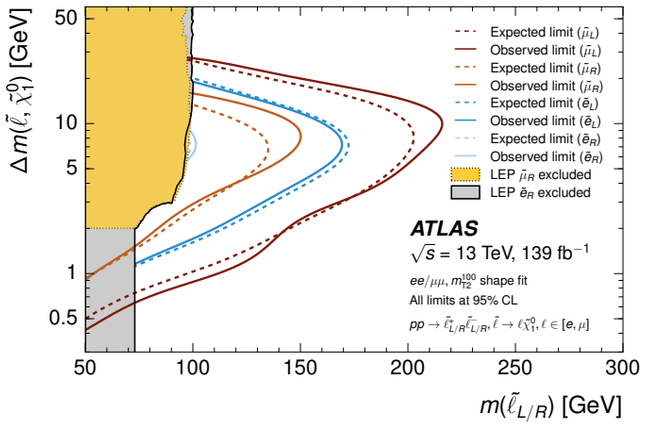
$$m_{\tilde{l}_R} = \min(M_1, |\mu|) + 20\,\text{GeV}$$

$$\tan\beta = 50, \quad M_2 = m_{\tilde{l}_L} = 10\,\text{TeV}$$



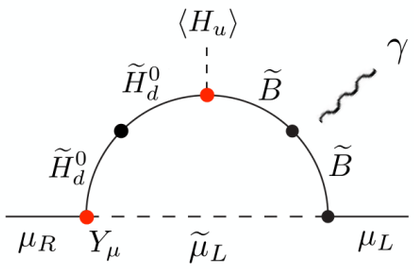
[1911.12606]

$$pp \to \tilde{\ell}\tilde{\ell}, \;\; \tilde{\ell} \to \ell + \tilde{\chi}_1^0$$



- Large regions are excluded by $\Omega_{\tilde{\chi}_1^0} > \Omega_{\text{DM}}$ and DM-DD.
- Future DM-DD experiments will explore the entire region
- LHC limits very weak

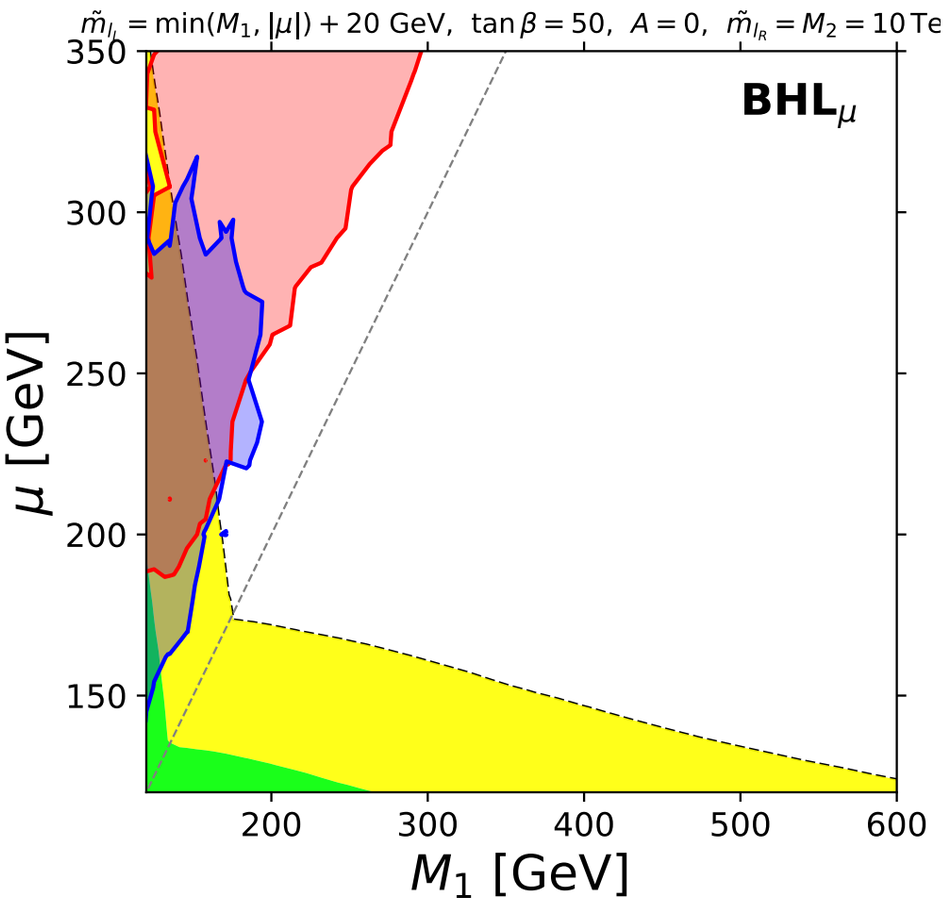
RPV

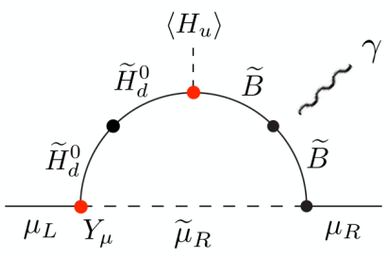


BHL

$$m_{\tilde{l}_L} = \min(M_1, \mu) + 20\,\text{GeV}$$

$$\tan\beta = 50, \quad M_2 = m_{\tilde{l}_R} = 10\,\text{TeV}$$

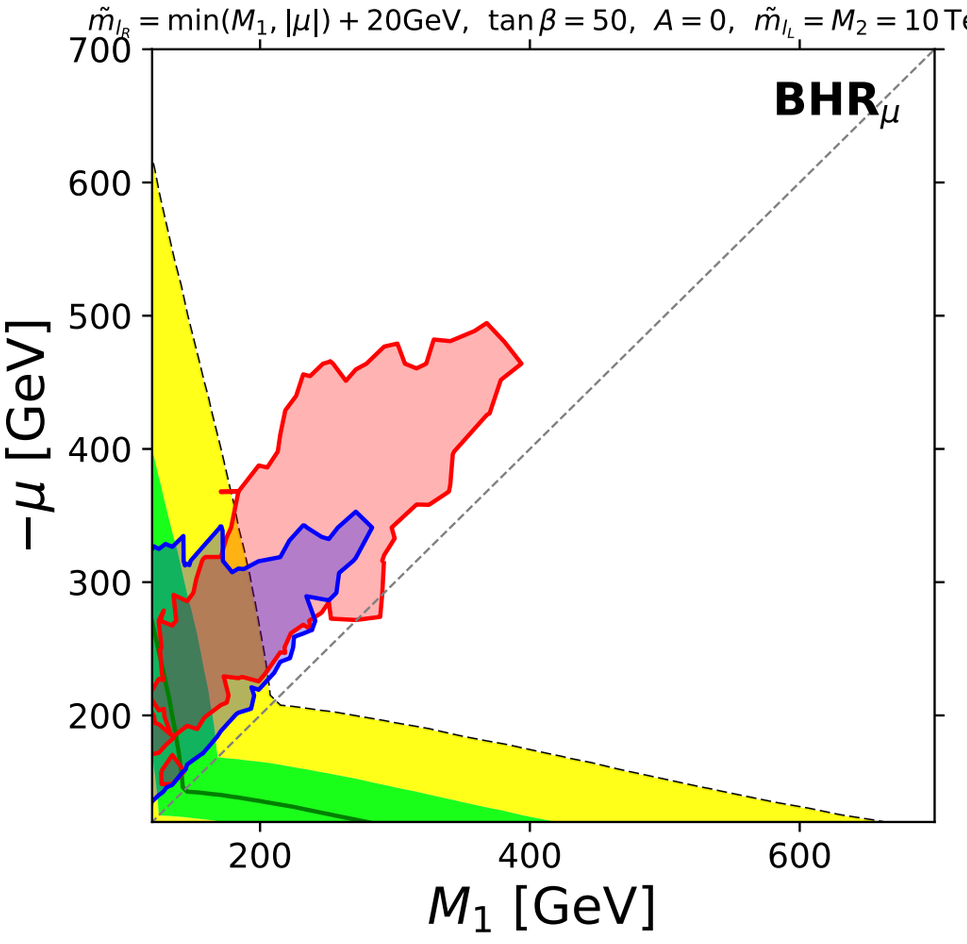




BHR

$$m_{\tilde{l}_R} = \min(M_1, |\mu|) + 20\,\text{GeV}$$

$$\tan\beta = 50, \quad M_2 = m_{\tilde{l}_L} = 10\,\text{TeV}$$

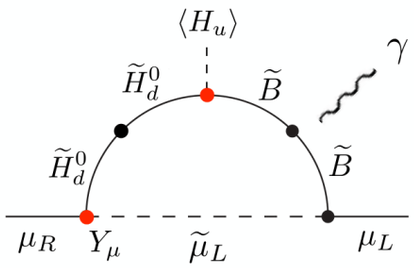


RPV ATLAS13 139/fb [2106.09609]

Multi & SS-leptons CMS13 36/fb [1709.05406]

- **Stronger LHC limits**
- **More g-2 region available**

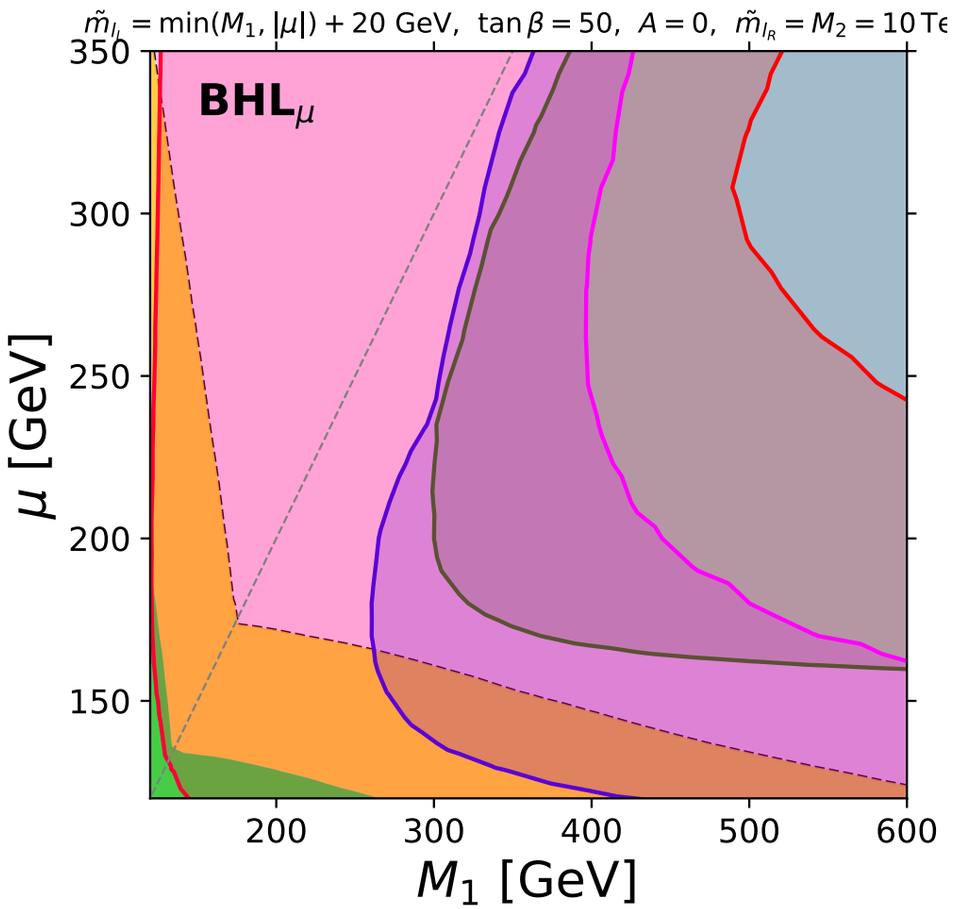
Gravitino LSP



BHL

$$m_{\tilde{l}_L} = \min(M_1, \mu) + 20\,\text{GeV}$$

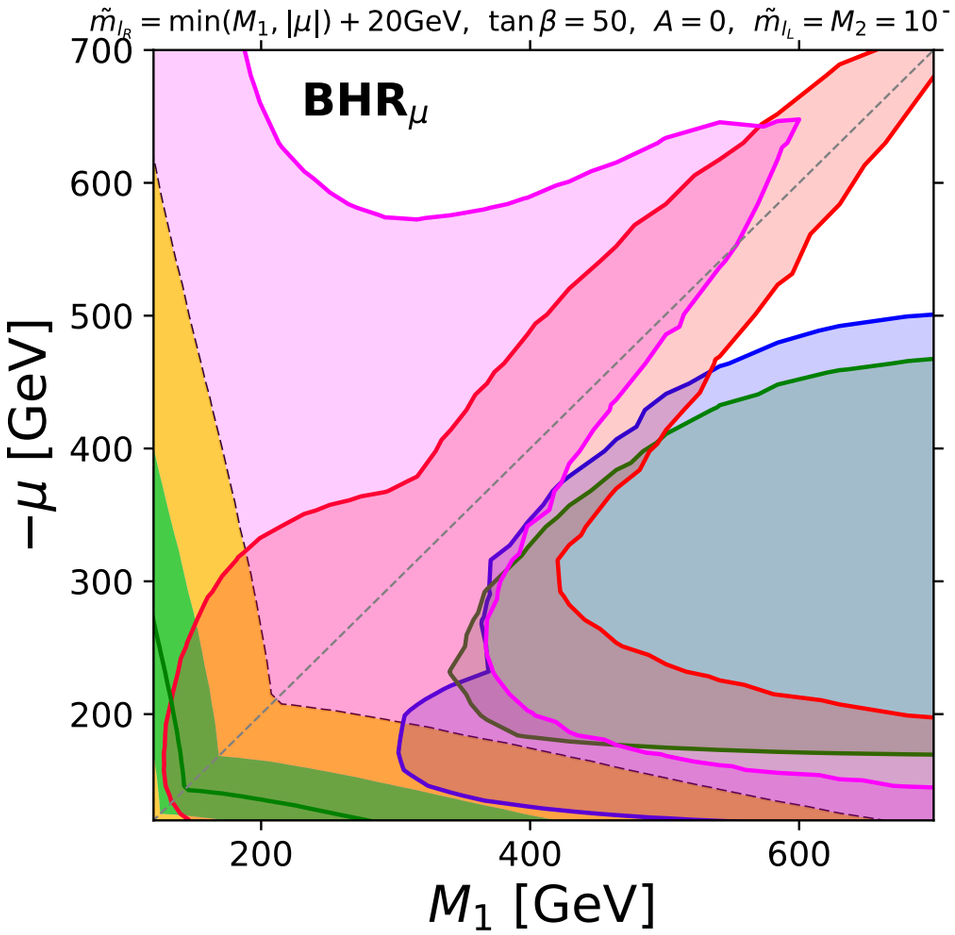
$$\tan\beta = 50, \quad M_2 = m_{\tilde{l}_R} = 10\,\text{TeV}$$



BHR

$$m_{\tilde{l}_R} = \min(M_1, |\mu|) + 20\,\text{GeV}$$

$$\tan\beta = 50, \quad M_2 = m_{\tilde{l}_L} = 10\,\text{TeV}$$



$[\gamma\widetilde{G}][\gamma\widetilde{G}]$ CMS $\gamma + \not{E}_T$ [1711.08008]

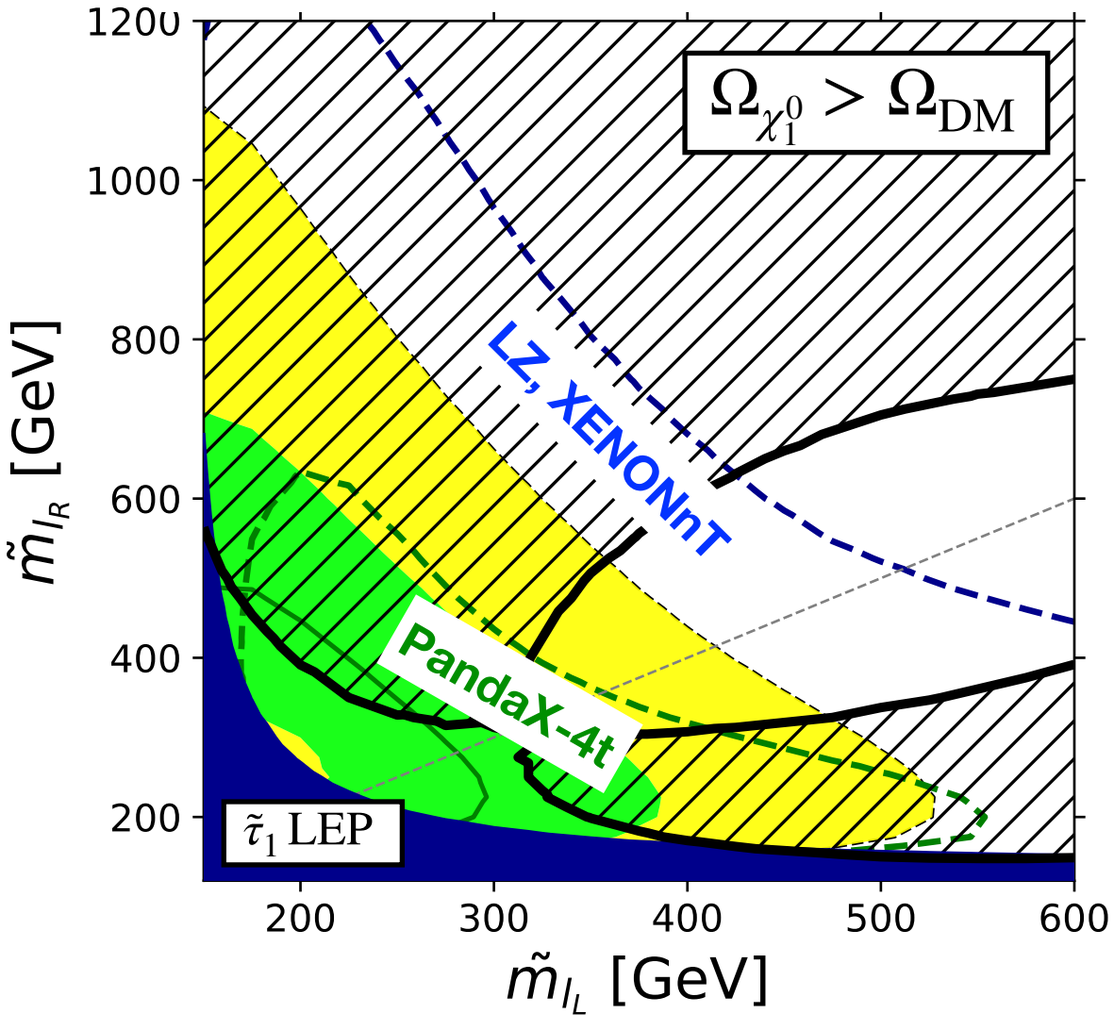
$[\gamma\widetilde{G}][Z(h)\widetilde{G}]$ CMS $\gamma + \not{E}_T$ [1711.08008]

$[Z\widetilde{G}][Z\widetilde{G}]$ CMS $\ell^+\ell^-$ [2012.08600]

$[h\widetilde{G}][Z\widetilde{G}]$ CMS $\ell^+\ell^-$ [2012.08600]

BLR

MSSM

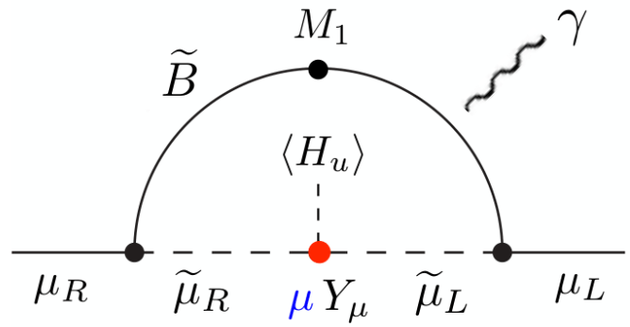


$$M_1 = m_{\tilde{\tau}_1} - 20\,\text{GeV}, \quad M_2 = 10\,\text{TeV}$$

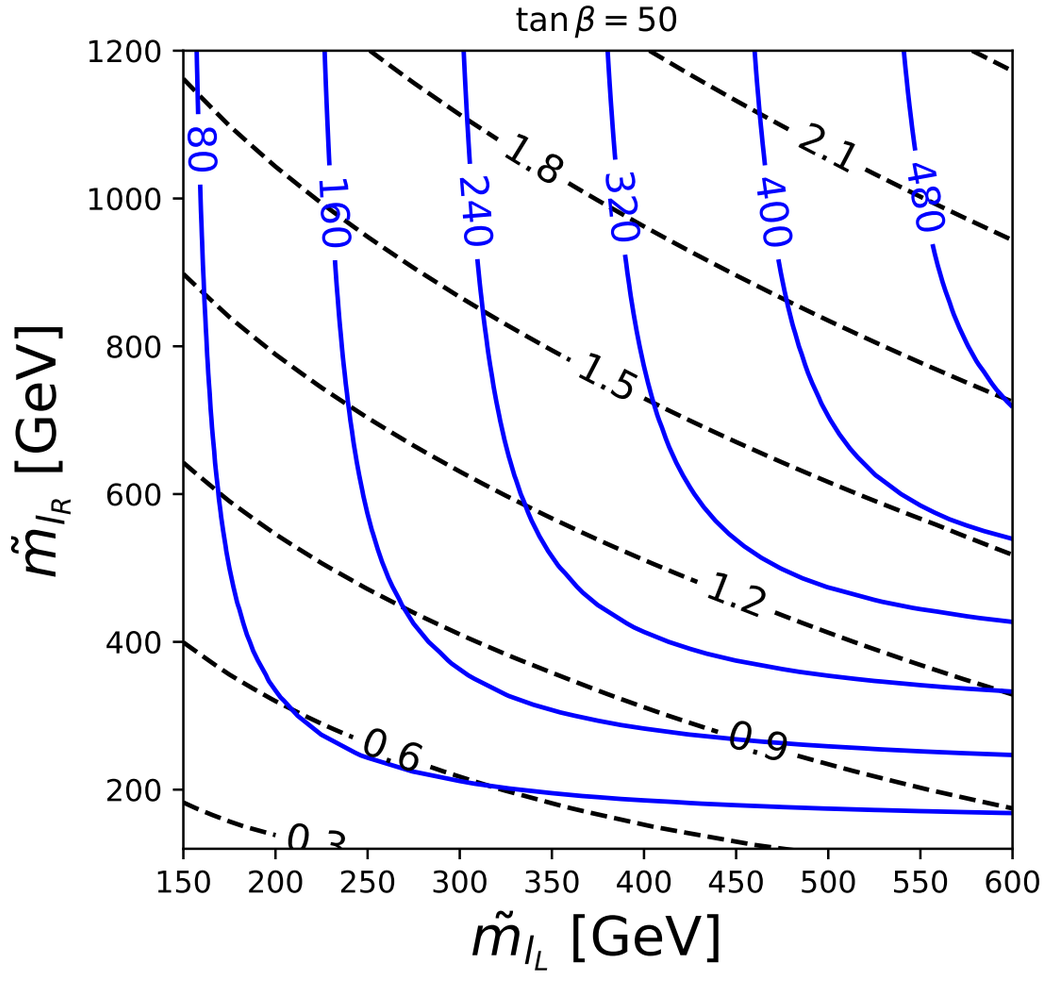
$$\mu = \mu_{\max}, \quad \tan\beta = 50$$

maximum allowed by vacuum (meta-)stability

$$\Delta a_\mu^{\rm BLR}(M_1, m_{\tilde{l}_L}, m_{\tilde{l}_R}; \mu)$$



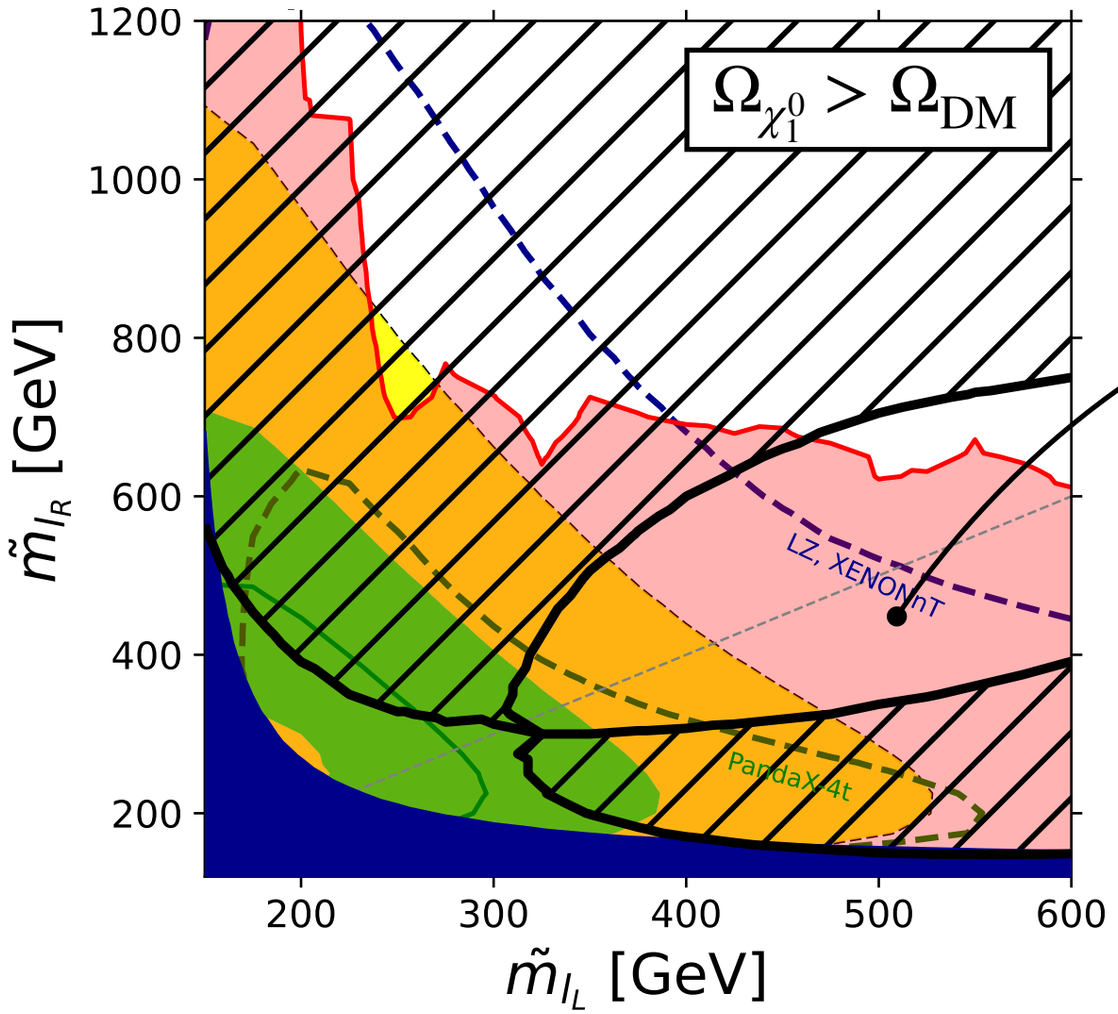
μ/TeV, M_1/GeV

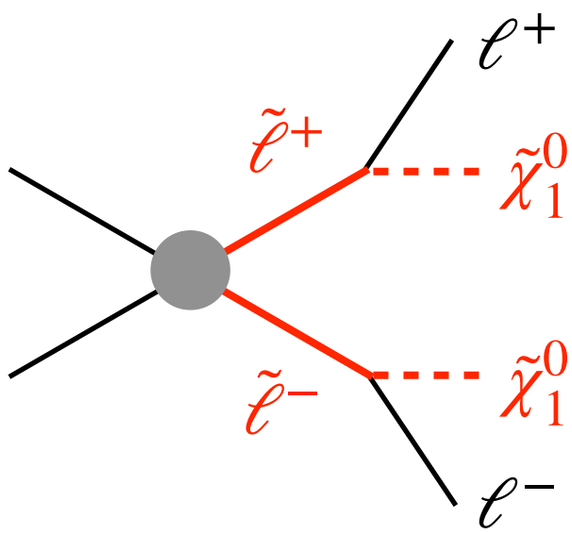


BLR

$$\Delta a_\mu^{\rm BLR}(M_1, m_{\tilde{l}_L}, m_{\tilde{l}_R}; \mu)$$

MSSM

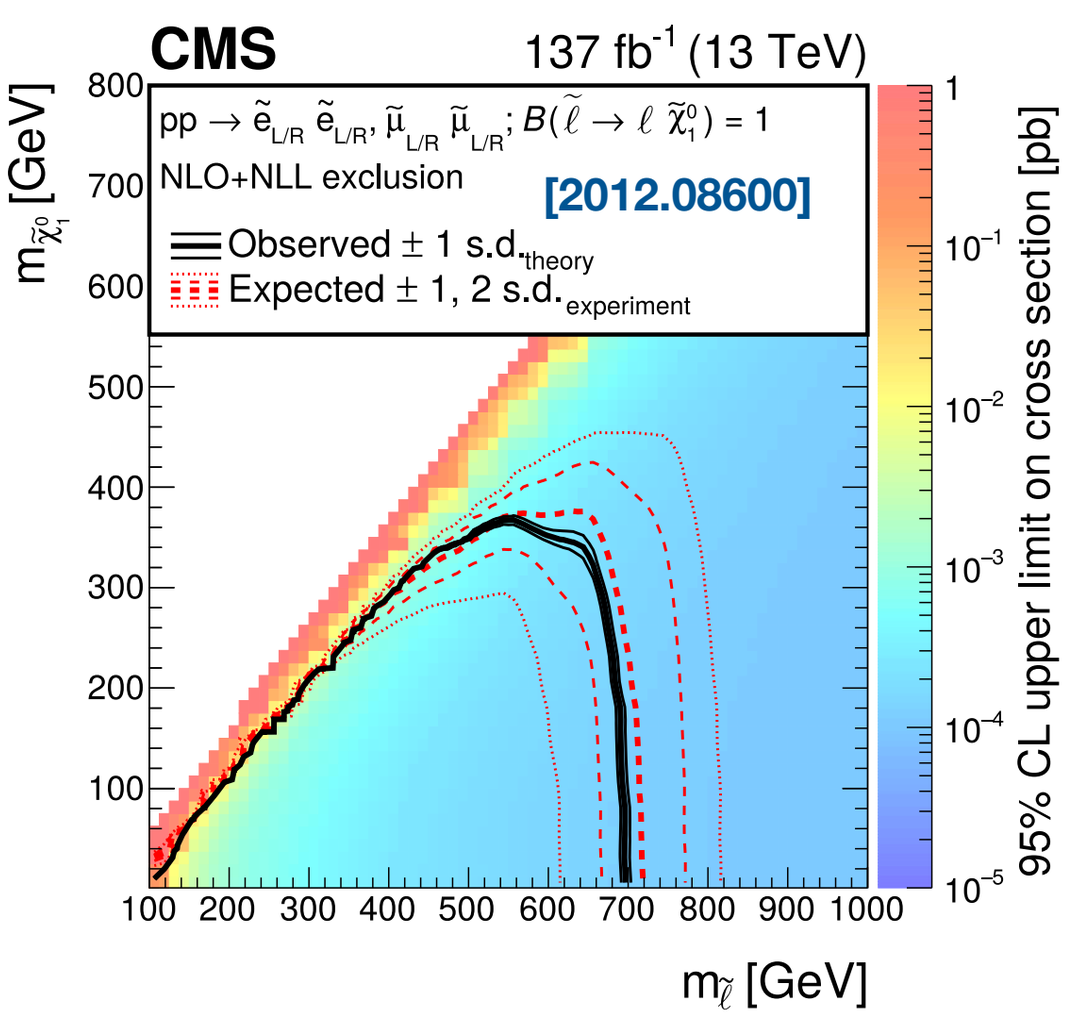




$M_1 = m_{\tilde{\tau}_1} - 20\,\text{GeV},$ $M_2 = 10\,\text{TeV}$

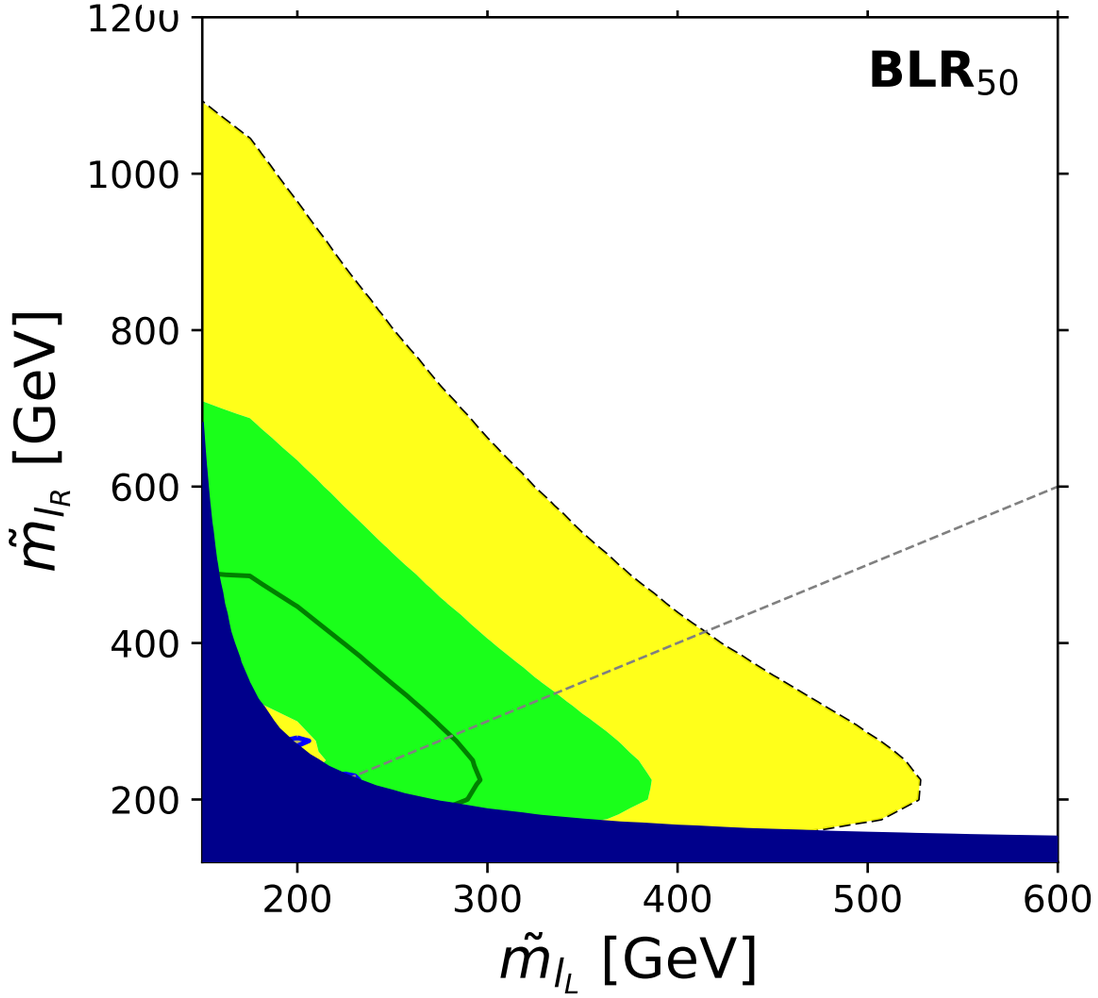
$\mu = \mu_{\rm max},$ $\tan\beta = 50$

maximum allowed by vacuum (meta-)stability

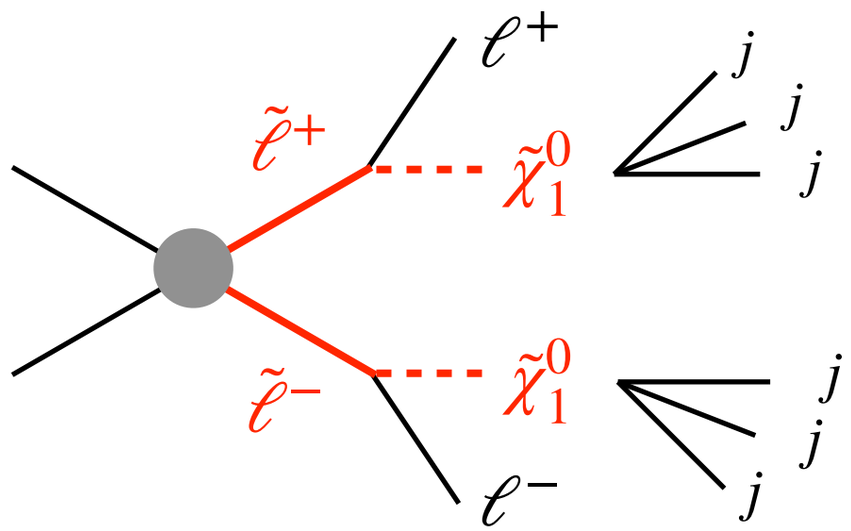


BLR

RPV



$$\Delta a_\mu^{\rm BLR}(M_1, m_{\tilde{l}_L}, m_{\tilde{l}_R}; \mu)$$



g-2 region is unconstrained

$$\boxed{M_1 = m_{\tilde{\tau}_1} - 20\,\text{GeV},}\quad M_2 = 10\,\text{TeV}$$

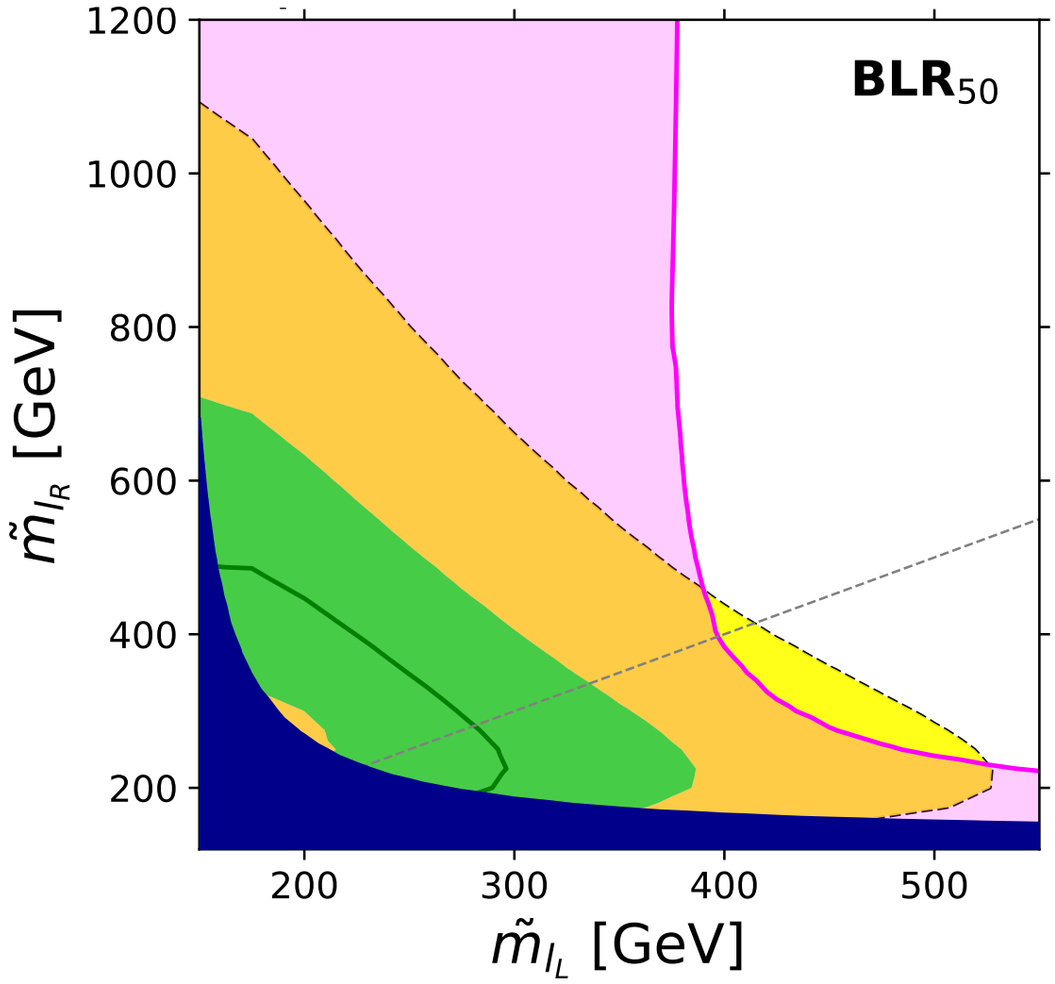
$$\boxed{\mu = \mu_{\max},}\quad \tan\beta = 50$$

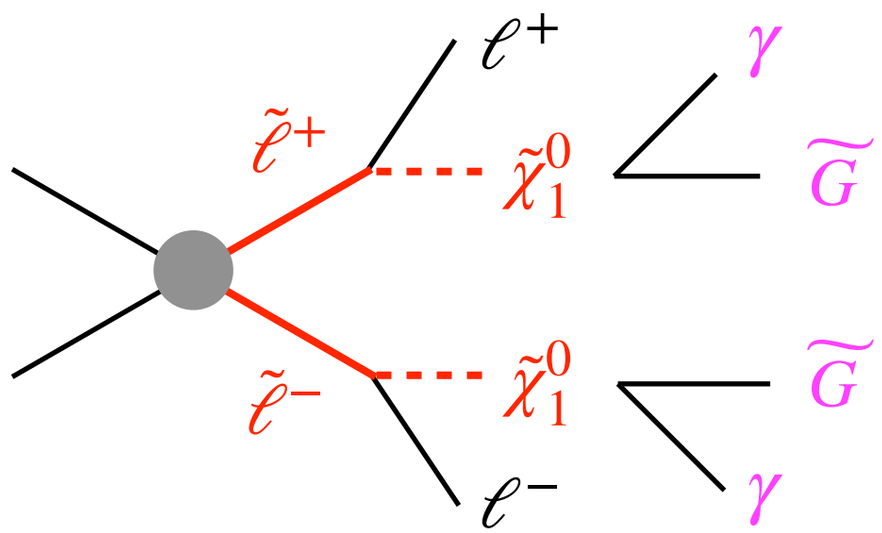
maximum allowed by vacuum (meta-)stability

BLR

Gravitino LSP

$$\Delta a_\mu^{\rm BLR}(M_1, m_{\tilde{l}_L}, m_{\tilde{l}_R}; \mu)$$





$[\gamma\widetilde{G}][\gamma\widetilde{G}]$ CMS $\gamma + E_T$ [1711.08008]

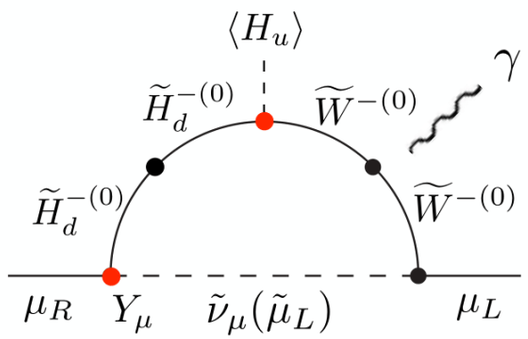
g-2 region is excluded by LHC

$M_1 = m_{\tilde{\tau}_1} - 20\,\text{GeV},$ $M_2 = 10\,\text{TeV}$

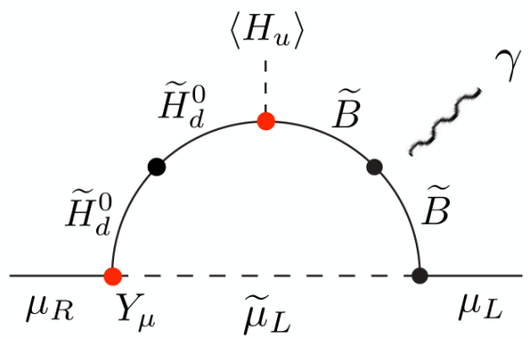
$\mu = \mu_{\max},$ $\tan\beta = 50$

maximum allowed by vacuum (meta-)stability

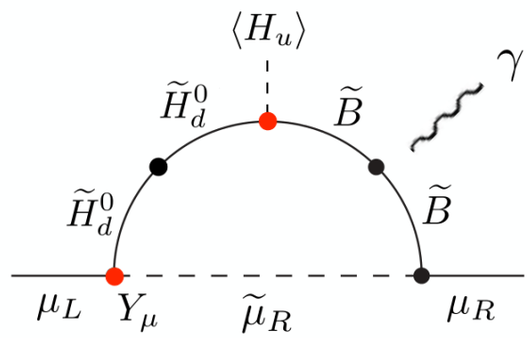
Short Summary



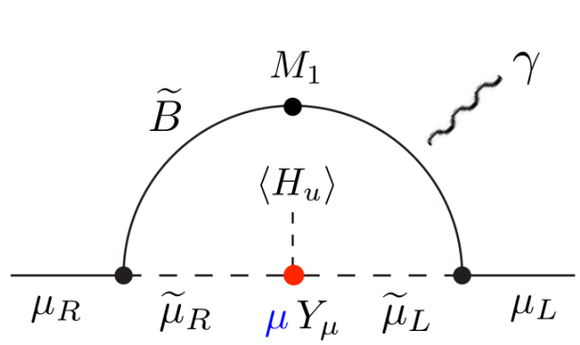
WHL



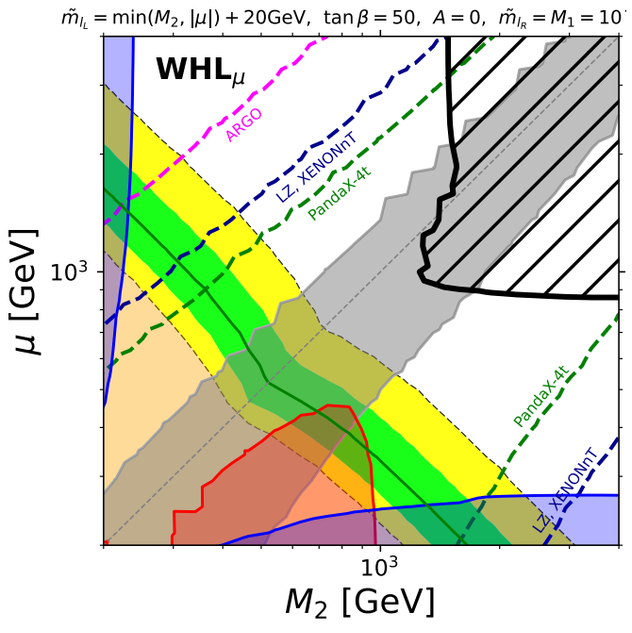
BHL

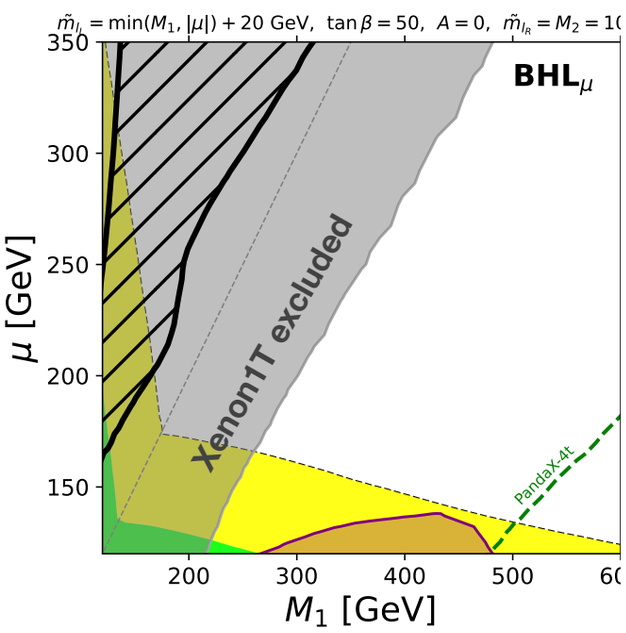


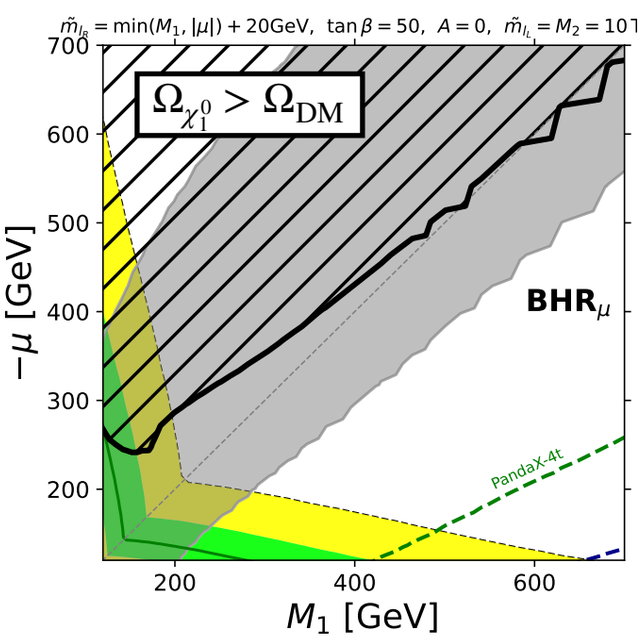
BHR

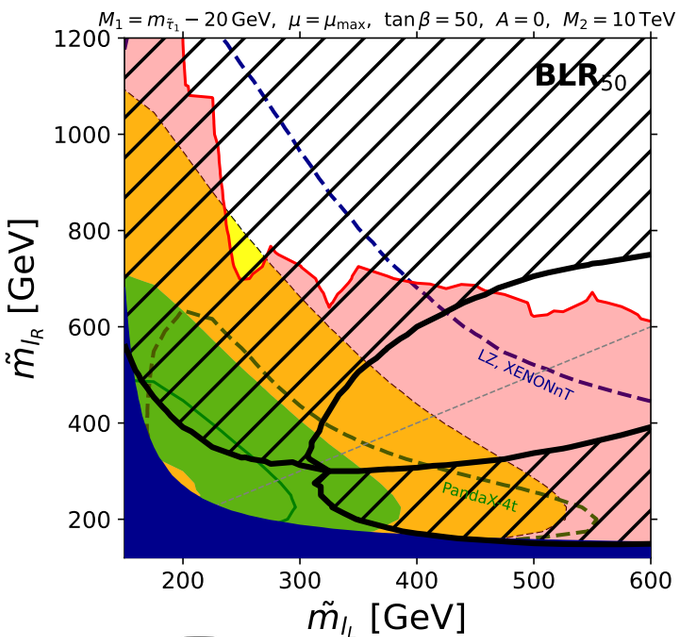


BLR

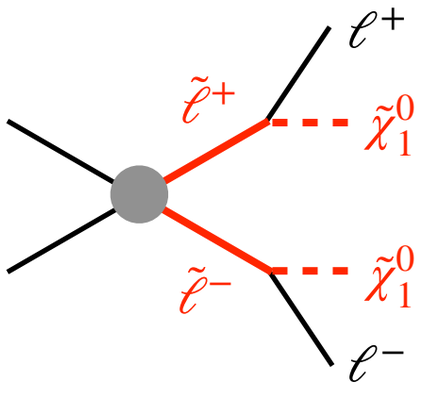






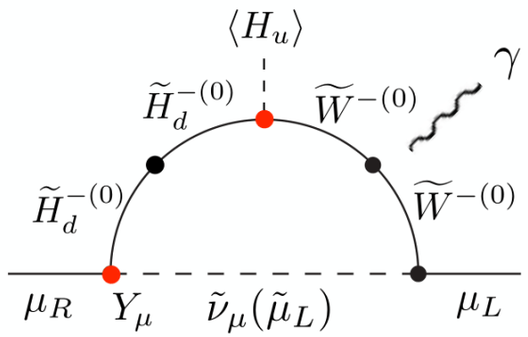


MSSM

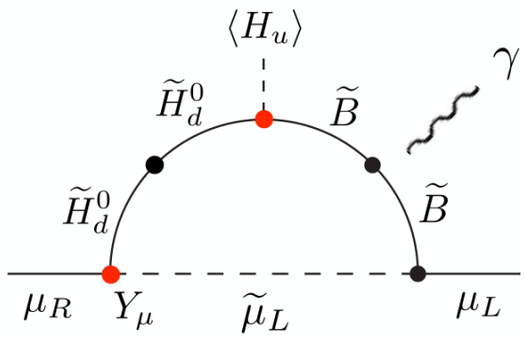


- Large regions are excluded by $\Omega_{\tilde{\chi}_1^0} > \Omega_{\text{DM}}$ and DM-DD.
- LHC constraints from lepton + $\not{E}_T$

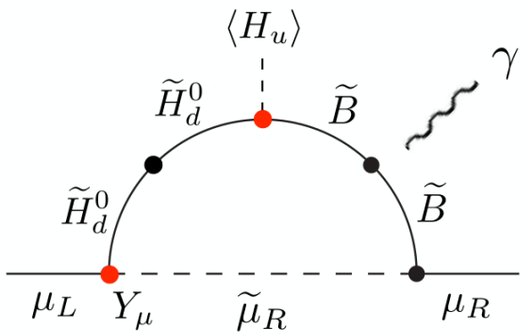
Short Summary



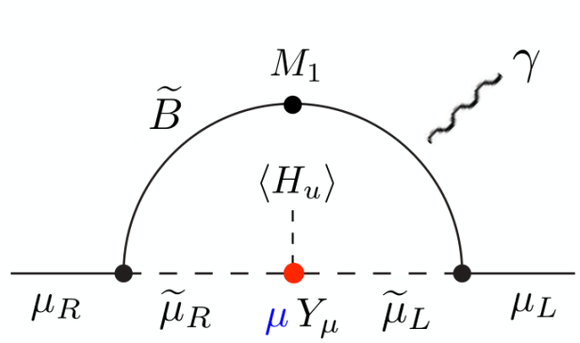
WHL



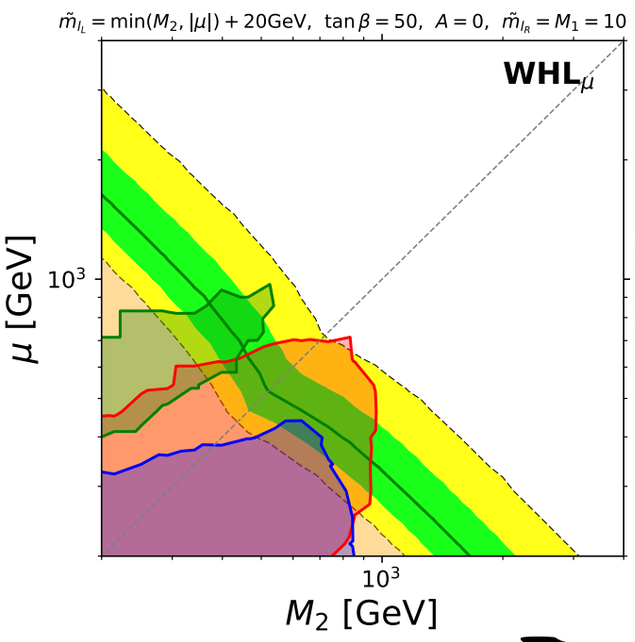
BHL

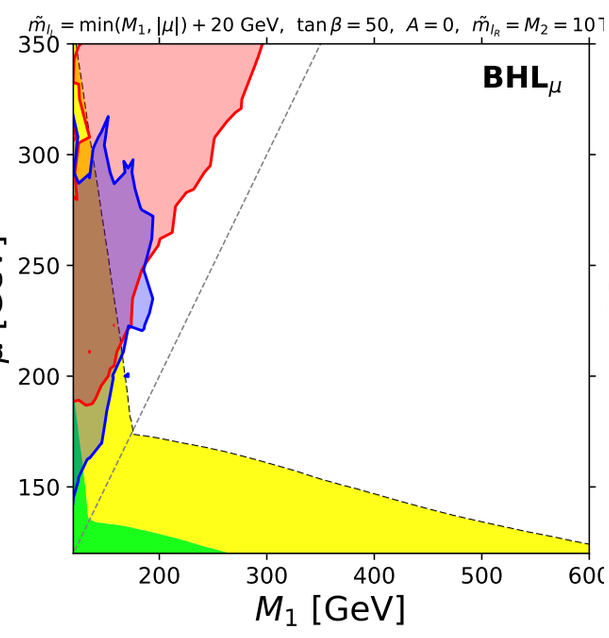


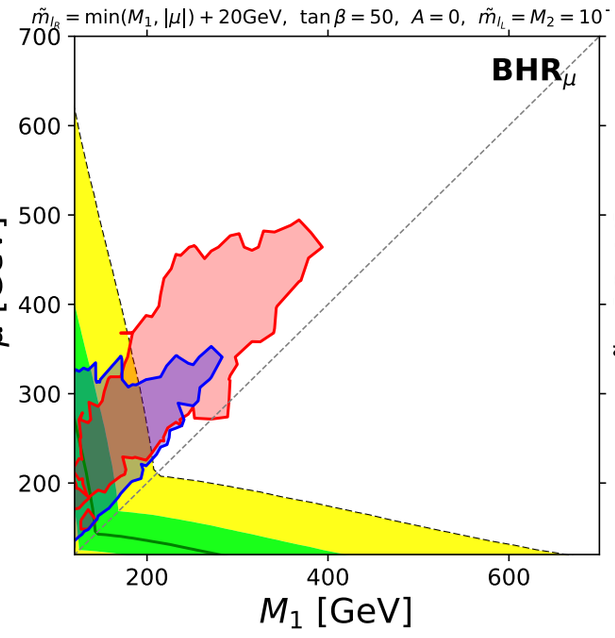
BHR

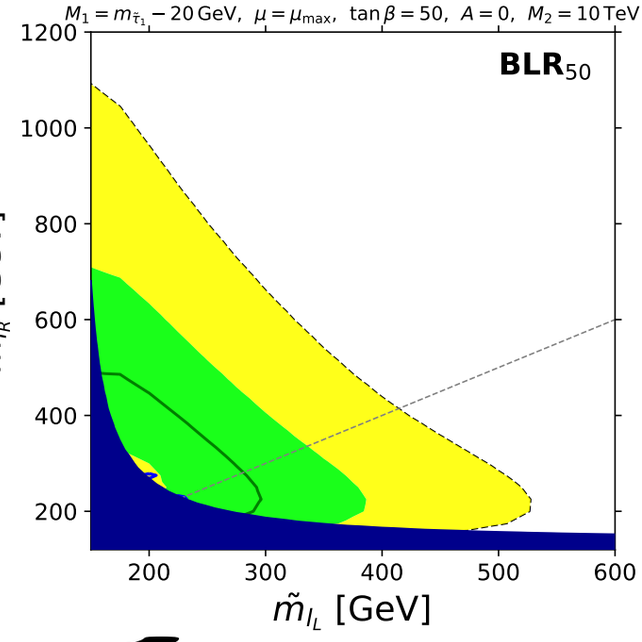


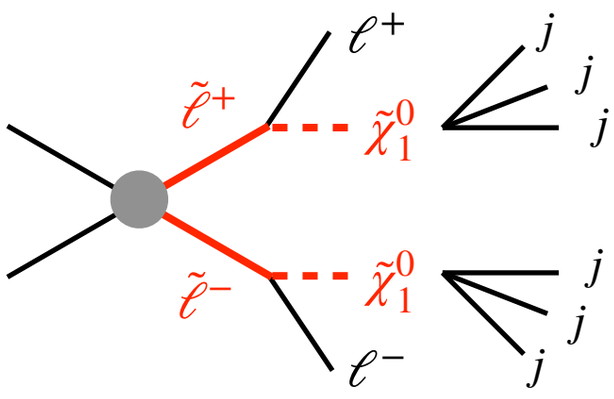
BLR







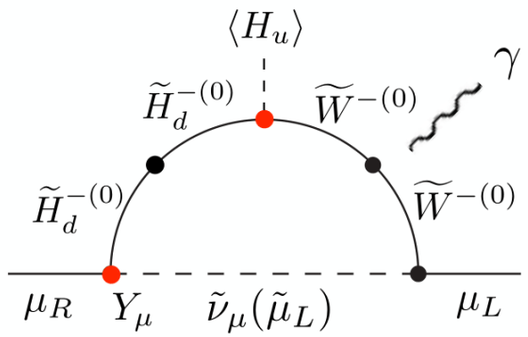




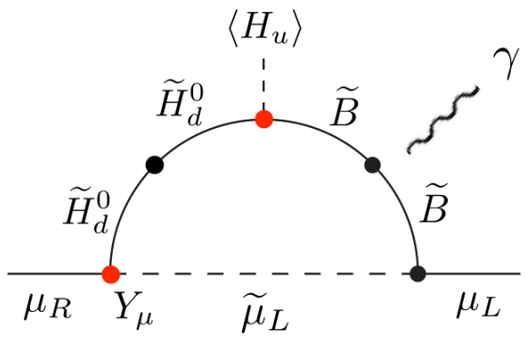
RPV

- No DM constraints
- LHC constraints from multijet + lepton

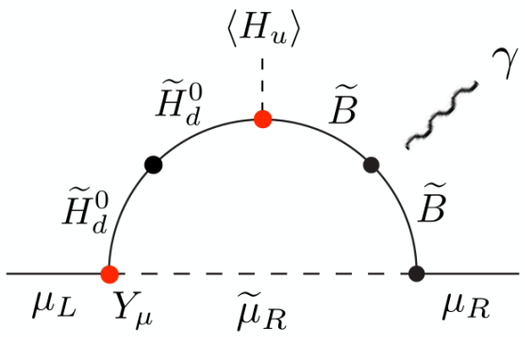
Short Summary



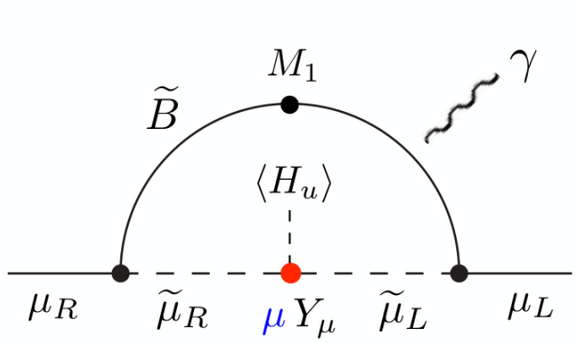
WHL



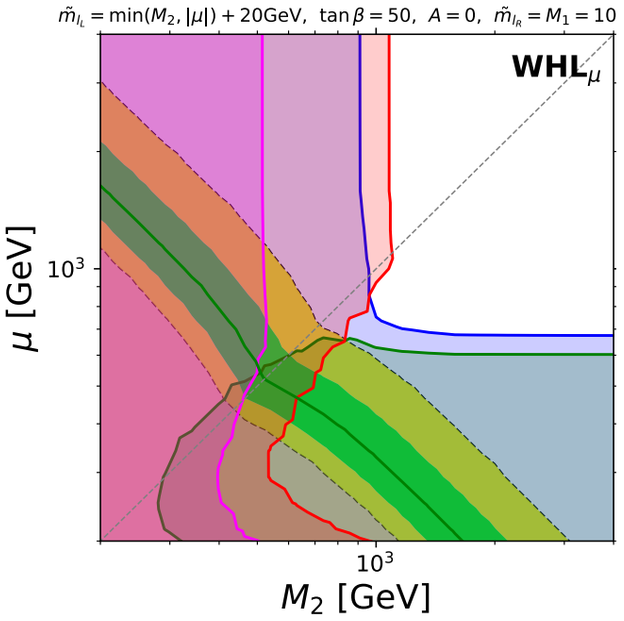
BHL

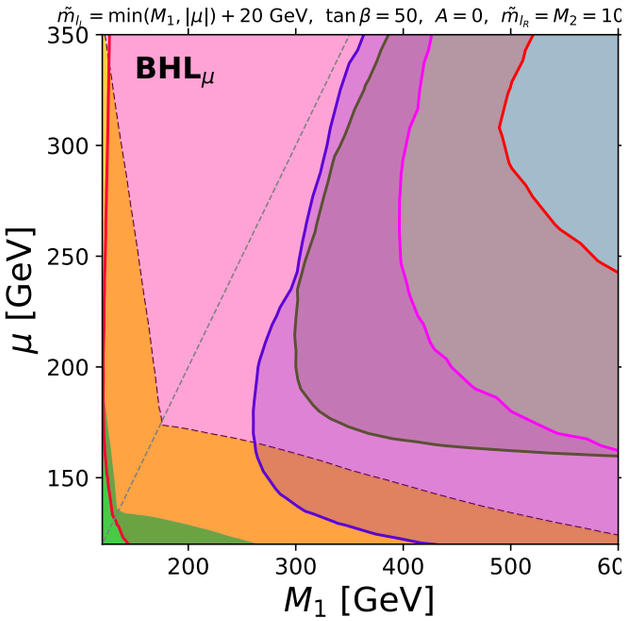


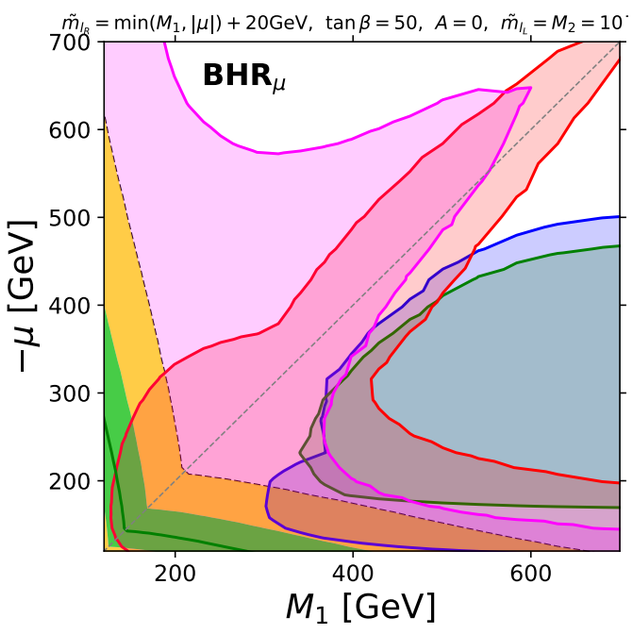
BHR

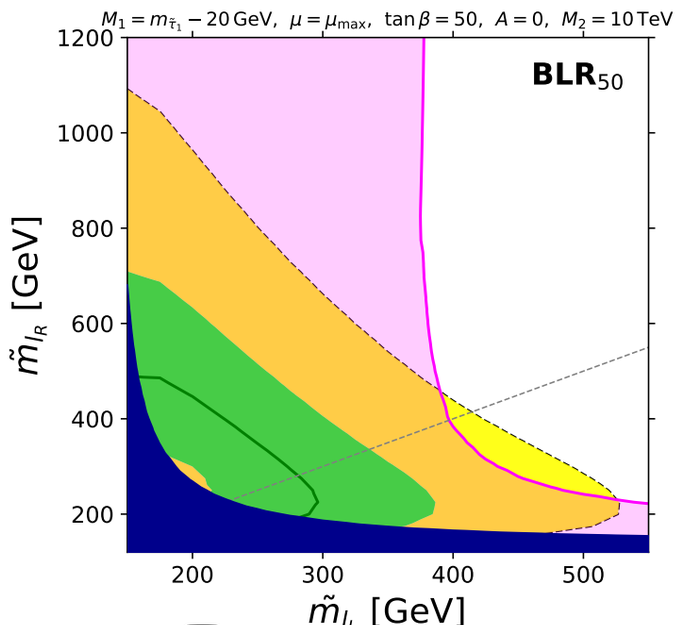


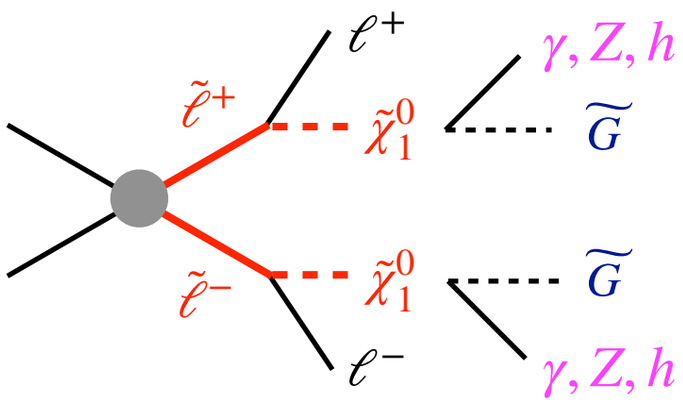
BLR









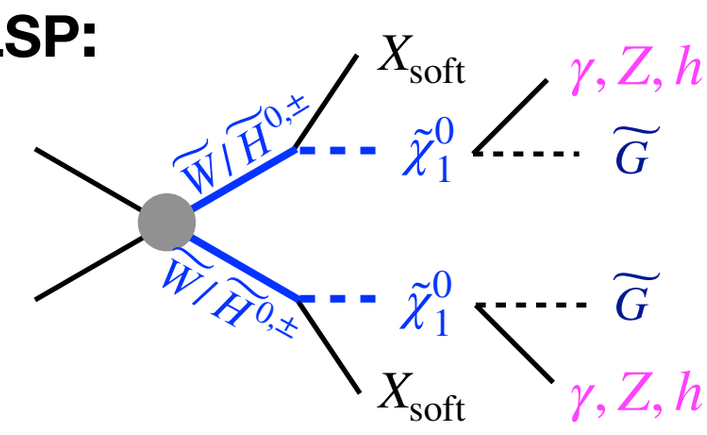


Gravitino LSP

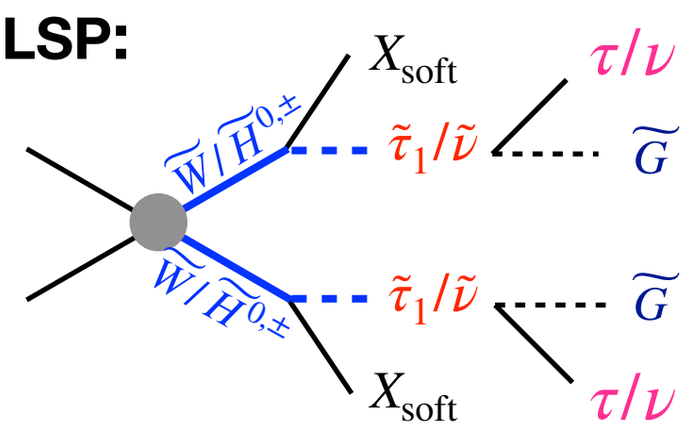
- No DM constraints
- all g-2 region is excluded mainly by $\gamma + \not{E}_T$

Gravitino LSP scenario really excluded?

$\tilde{\chi}_1^0$ **NLSP:**

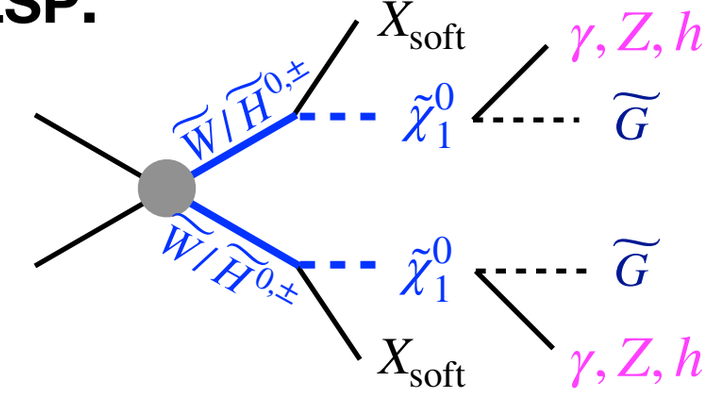


$\tilde{\tau}_1/\tilde{\nu}$ **NLSP:**

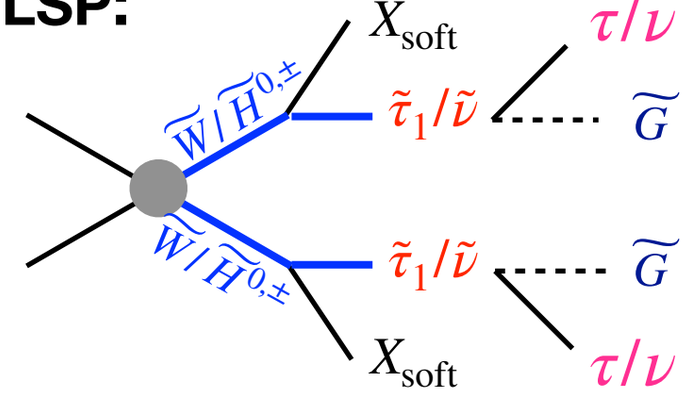


Gravitino LSP scenario really excluded?

$\tilde{\chi}_1^0$ **NLSP:**



$\tilde{\tau}_1/\tilde{\nu}$ **NLSP:**



WHL plane:

$(M_2 \text{ vs } \mu)$ with $\tilde{m}_{l_L} = \min(M_2, \mu) + 20\,\text{GeV} \implies m_{l_L} = \min(M_2, \mu) - 20\,\text{GeV}$

BHL plane:

$(M_1 \text{ vs } \mu)$ with $\tilde{m}_{l_L} = \min(M_1, \mu) + 20\,\text{GeV} \implies m_{l_L} = \min(M_2, \mu) - 20\,\text{GeV}$

} $\tilde{\nu}_L$ **NLSP**

BHR plane:

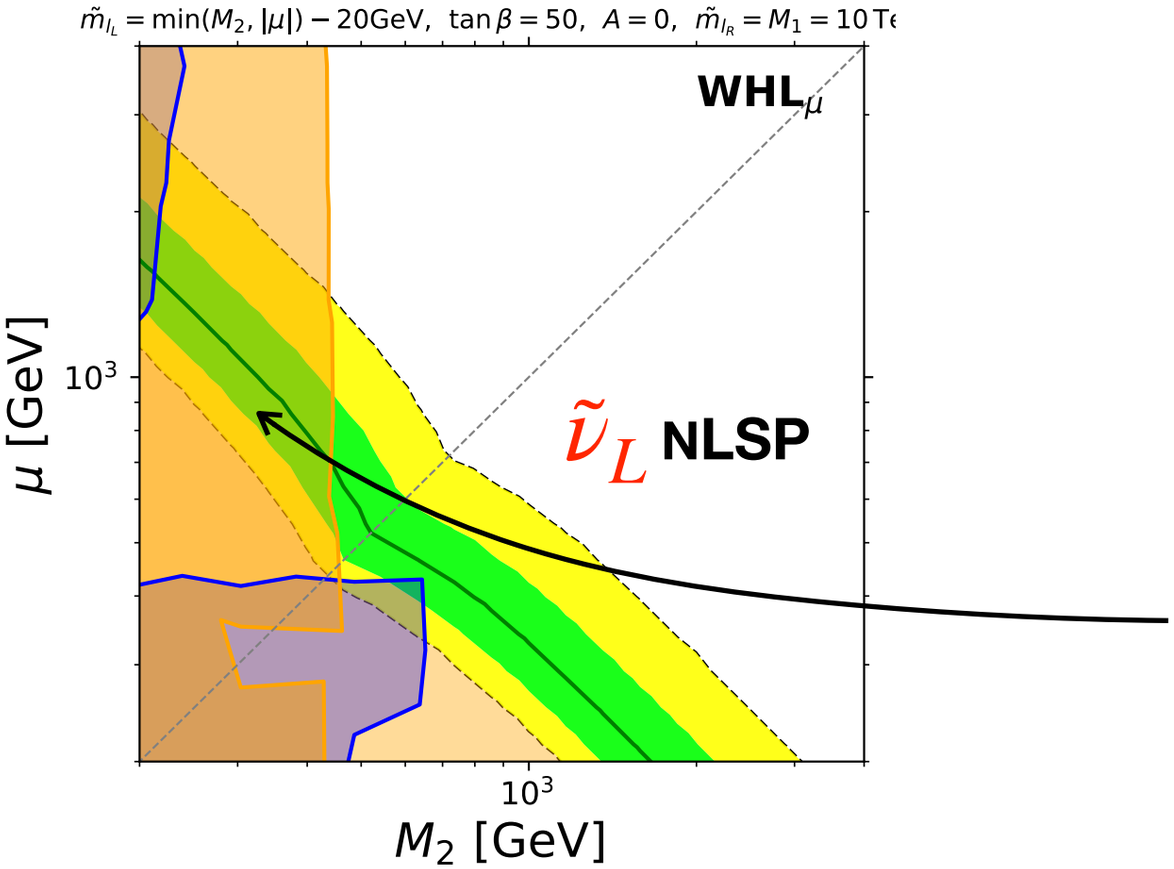
$(M_1 \text{ vs } \mu)$ with $\tilde{m}_{l_R} = \min(M_1, |\mu|) + 20\,\text{GeV} \implies m_{l_R} = \min(M_1, \mu) - 20\,\text{GeV}$

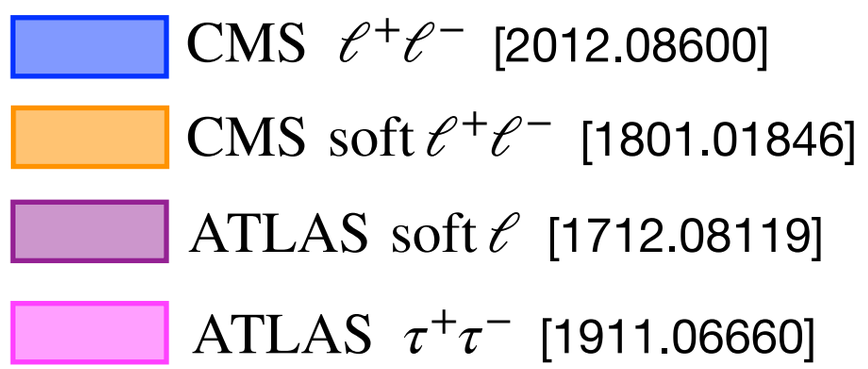
} $\tilde{e}_R, \tilde{\mu}_R, \tilde{\tau}_R$ **NLSP**

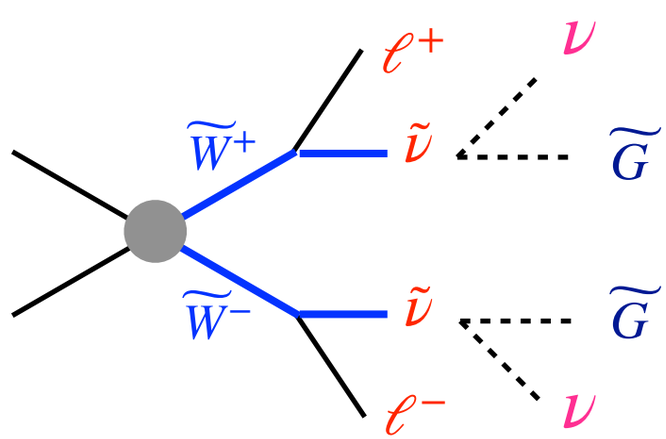
BLR plane:

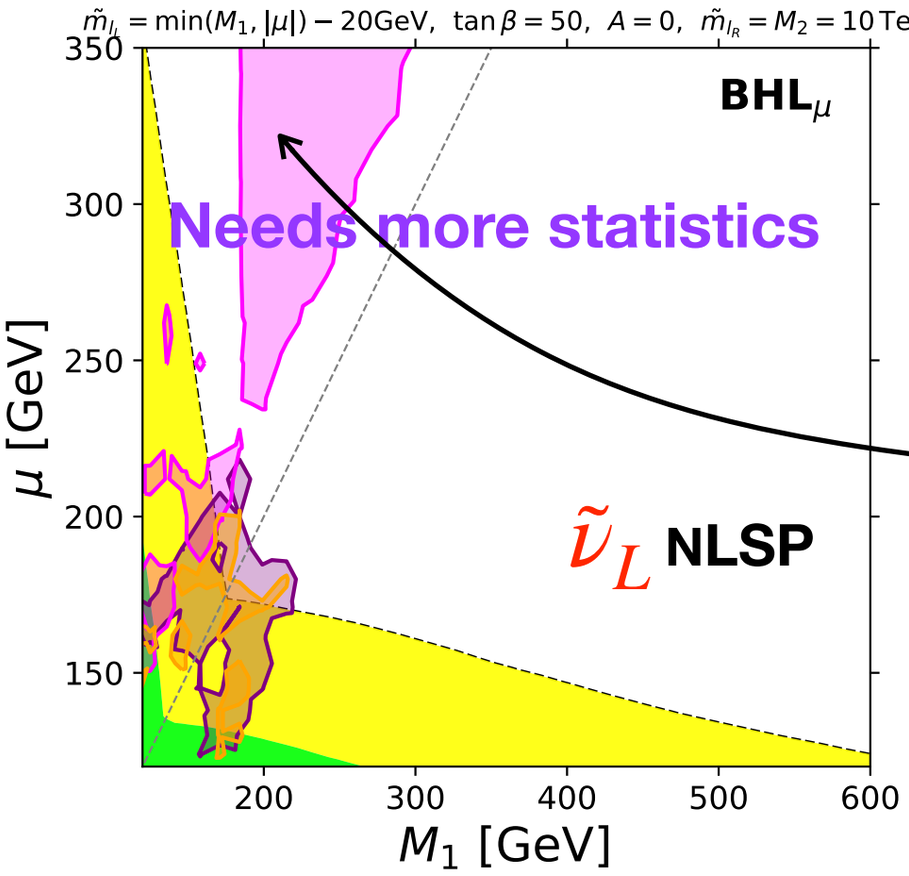
$(\tilde{m}_{l_L} \text{ vs } \tilde{m}_{l_R})$ with $M_1 = m_{\tilde{\tau}_1} - 20\,\text{GeV} \implies M_1 = m_{\tilde{\tau}_1} + 20\,\text{GeV}$

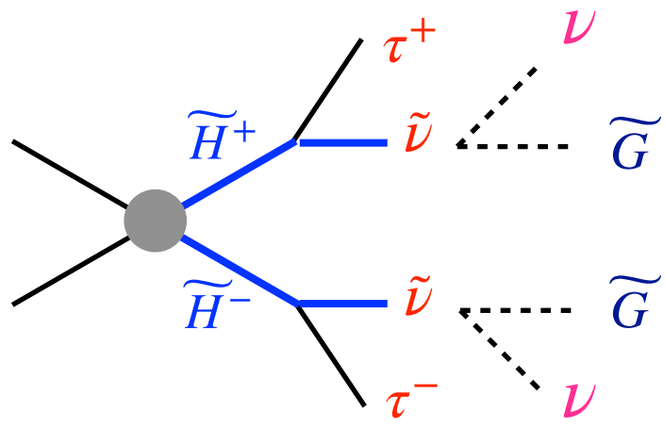
} $\tilde{\tau}_1$ **NLSP**

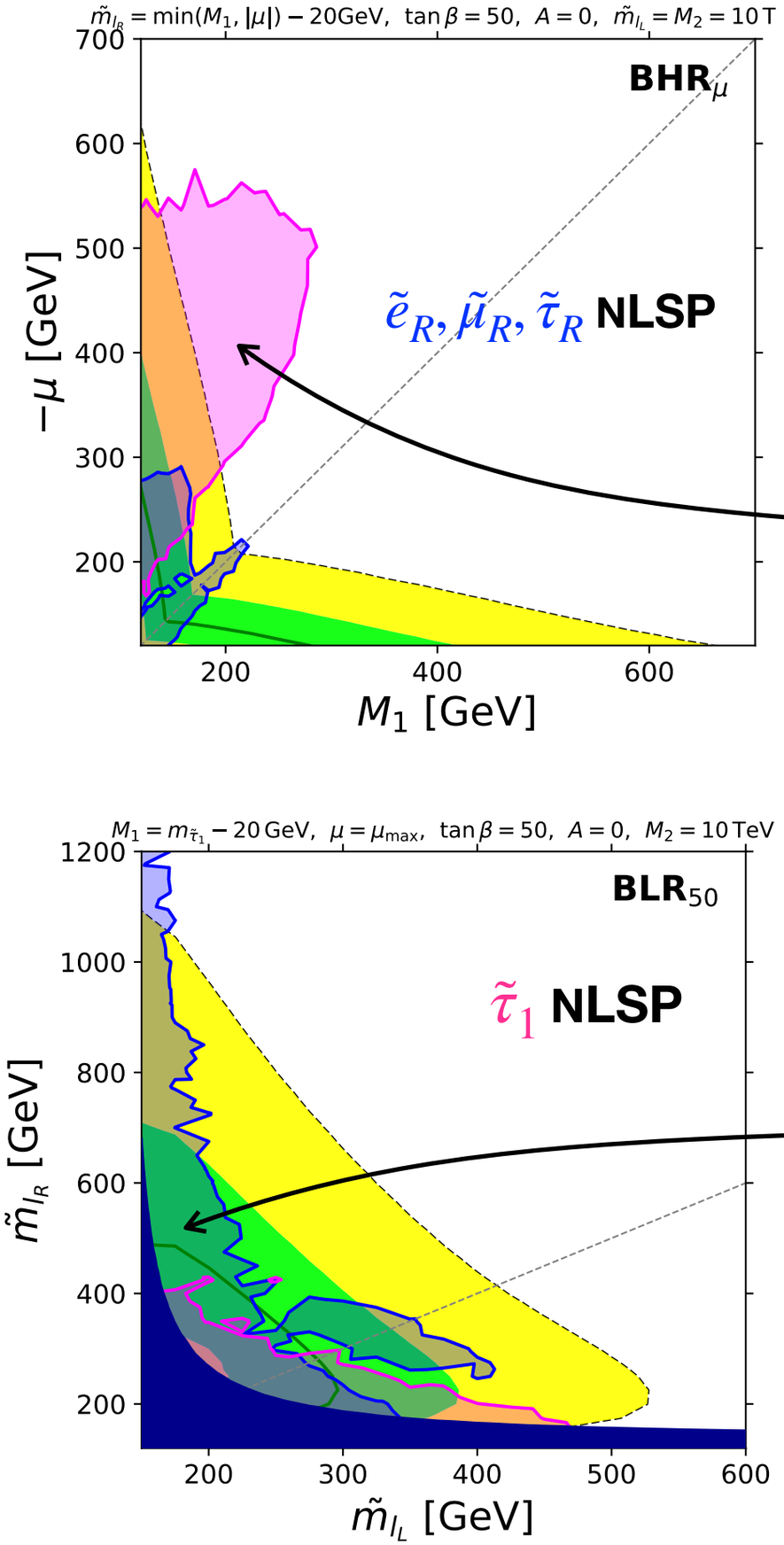

$\tilde{m}_{l_L} = \min(M_2, |\mu|) - 20\text{GeV},\ \tan\beta = 50,\ A = 0,\ \tilde{m}_{l_R} = M_1 = 10\,\text{Te}$
WHL$_\mu$
$\tilde{\nu}_L$ NLSP
μ [GeV]
10^3
10^3
M_2 [GeV]


CMS $\ell^+\ell^-$ [2012.08600]
CMS soft $\ell^+\ell^-$ [1801.01846]
ATLAS soft ℓ [1712.08119]
ATLAS $\tau^+\tau^-$ [1911.06660]


ℓ^+
ν
$\widetilde{W}^+$
$\tilde{\nu}$
$\widetilde{G}$
$\widetilde{W}^-$
$\tilde{\nu}$
$\widetilde{G}$
ℓ^-
ν


$\tilde{m}_{l_L} = \min(M_1, |\mu|) - 20\text{GeV},\ \tan\beta = 50,\ A = 0,\ \tilde{m}_{l_R} = M_2 = 10\,\text{Te}$
BHL$_\mu$
Needs more statistics
$\tilde{\nu}_L$ NLSP
μ [GeV]
M_1 [GeV]


τ^+
ν
$\widetilde{H}^+$
$\tilde{\nu}$
$\widetilde{G}$
$\widetilde{H}^-$
$\tilde{\nu}$
$\widetilde{G}$
τ^-
ν

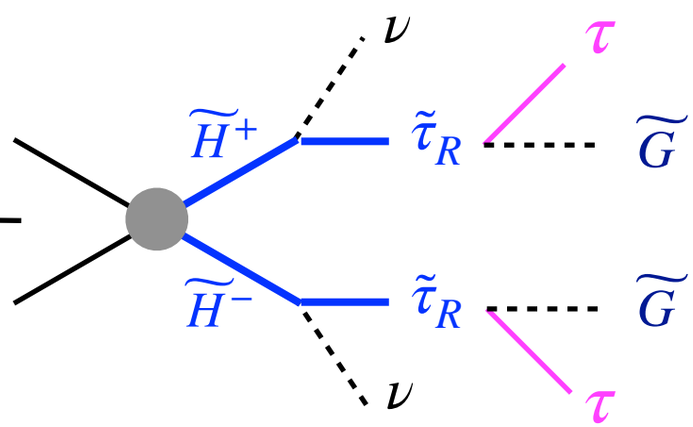


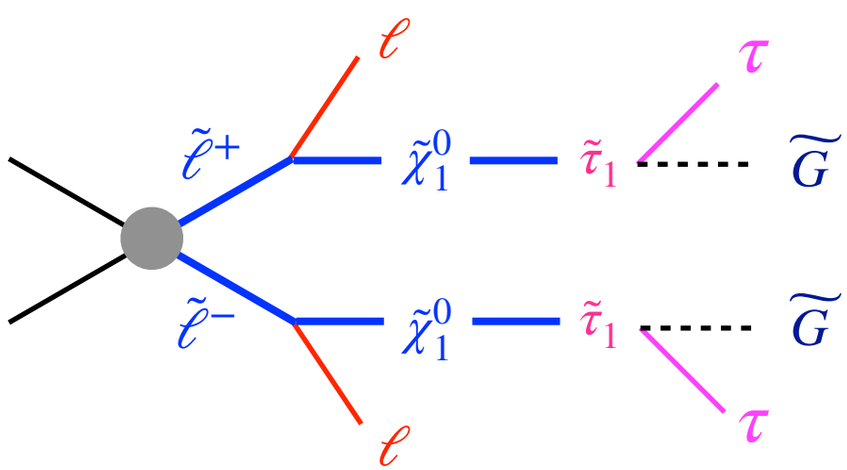
CMS $\ell^+\ell^-$ [2012.08600]

CMS soft $\ell^+\ell^-$ [1801.01846]

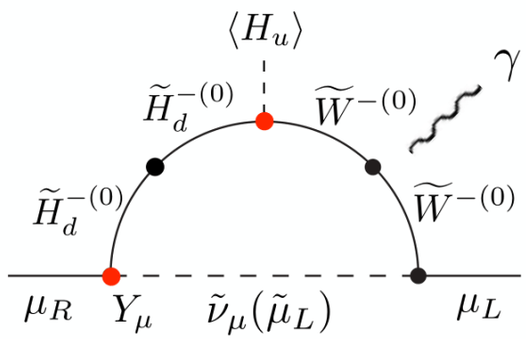
ATLAS soft ℓ [1712.08119]

ATLAS $\tau^+\tau^-$ [1911.06660]

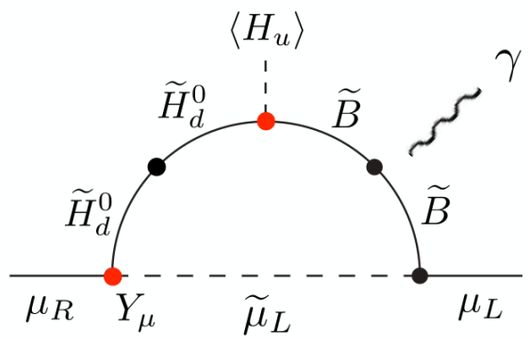




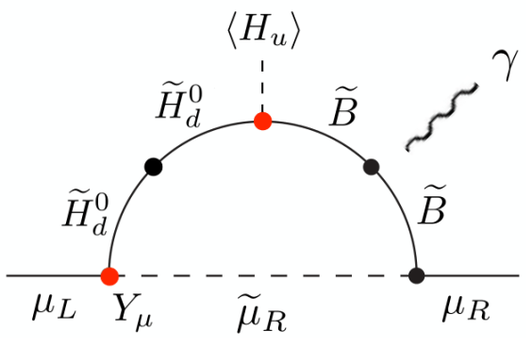
Non $\tilde{\chi}_1^0$ NLSP (Short Summary)



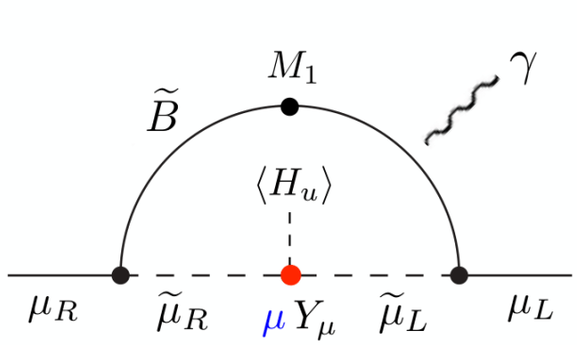
WHL



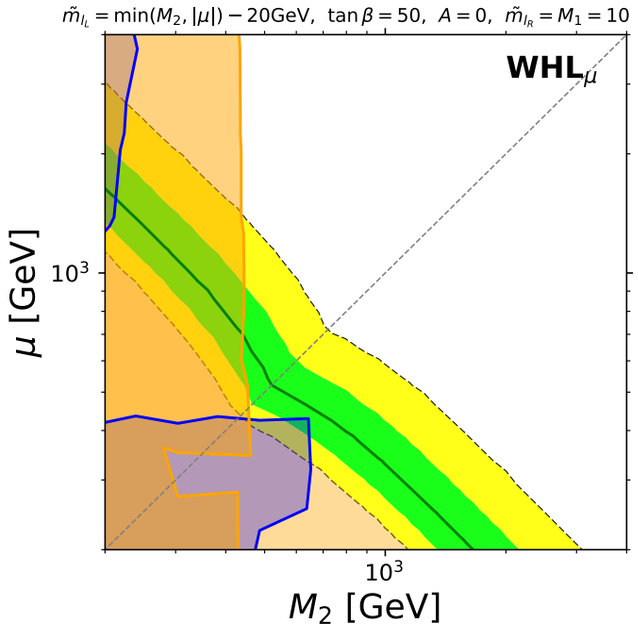
BHL

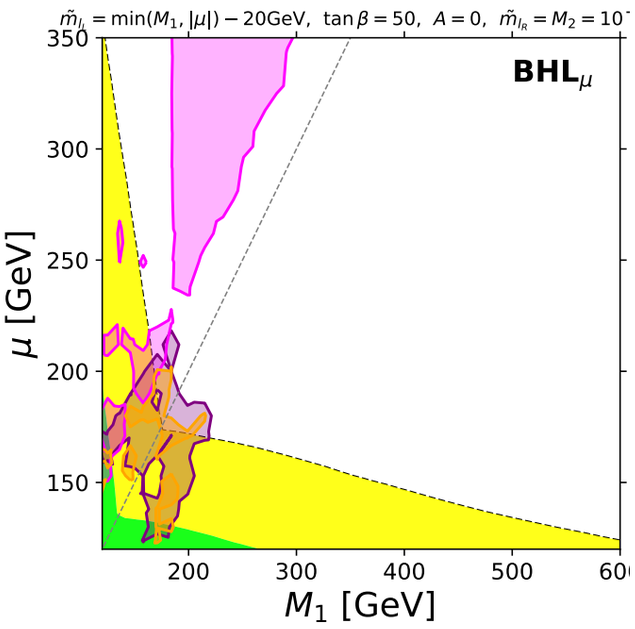


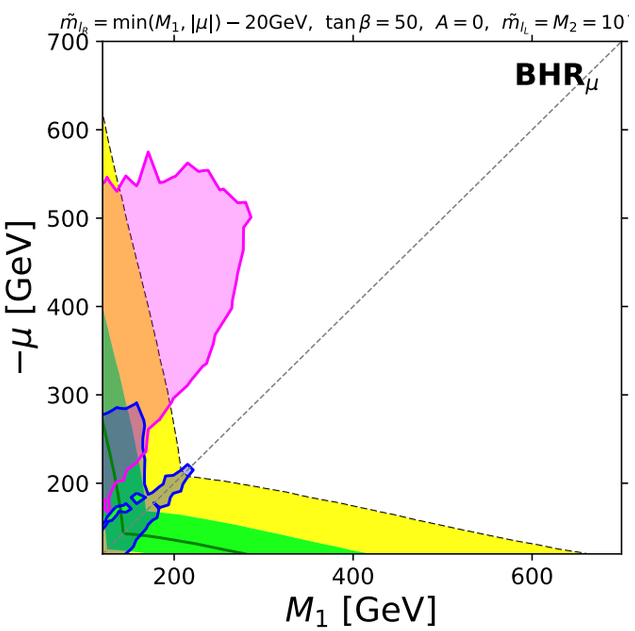
BHR

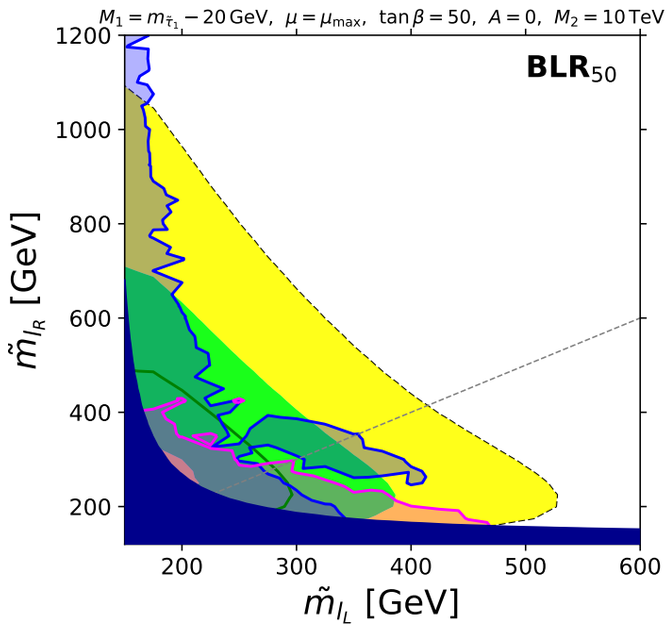


BLR









◉ small $|\mu|$ region is compatible with $(g\text{-}2)_\mu$

Summary

- SUSY might be a solution to the $(g\text{-}2)_\mu$ anomaly
  - stable LSP $\tilde{\chi}_1^0$ $\Longrightarrow$ **LHC constraints from large $\not{E}_T$ search**
  - slepton-gaugino-Higgsino are light $\Longrightarrow$ **stringent constraint from DM-DD detection**
  - LR slepton and Bino are light $\Longrightarrow$ **Bino overproduction**

- If $\tilde{\chi}_1^0$ is not stable LSP, DM constraints go away, and LHC signature changes.
  - ① RPV with UDD $\Longrightarrow$ LHC constraints from **multijet + lepton**
  - ② Gravitino LSP with $\tilde{\chi}_1^0$ NLSP $\Longrightarrow$ $(g\text{-}2)_\mu$ region excluded by $\gamma\not{+} E_T$ channel
  - ③ Gravitino LSP with ***non*** $\tilde{\chi}_1^0$ NLSP $\Longrightarrow$ LHC constraints from **soft lepton/tau**

Explanation for $(g\text{-}2)_\mu$ anomaly is possible for the scenarios ① and ③

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Understanding the Early Universe: interplay of theory and collider experiments

Joint research project between the University of Warsaw & University of Bergen