

New physics contributions in $B \rightarrow \pi \tau \bar{\nu}$ and $B \rightarrow \tau \bar{\nu}$

Minoru Tanaka
Osaka U

in collaboration with R. Watanabe, arXiv:1608.05207

Flavor Physics Workshop 2016, Niigata, Oct. 28, 2016.

Introduction

$$\bar{B} \rightarrow D^{(*)} \tau \bar{\nu}$$

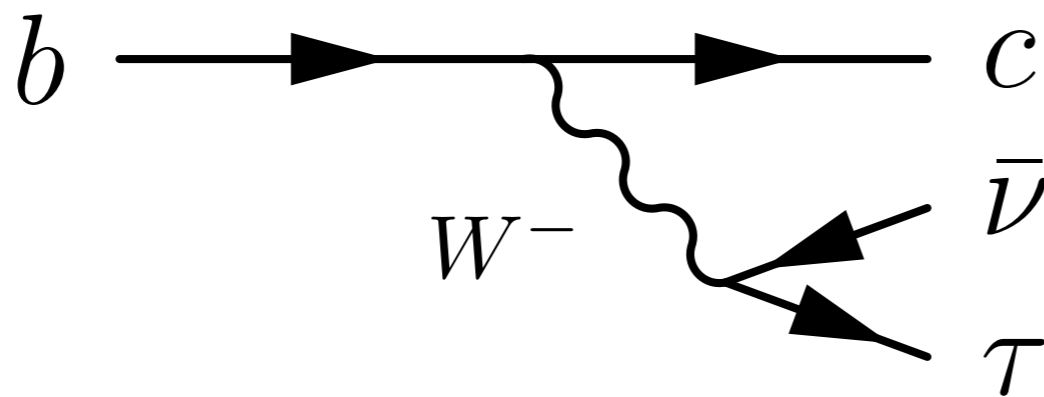
Br \sim 0.7+1.3 % in the SM

Not rare, but two or more missing neutrinos

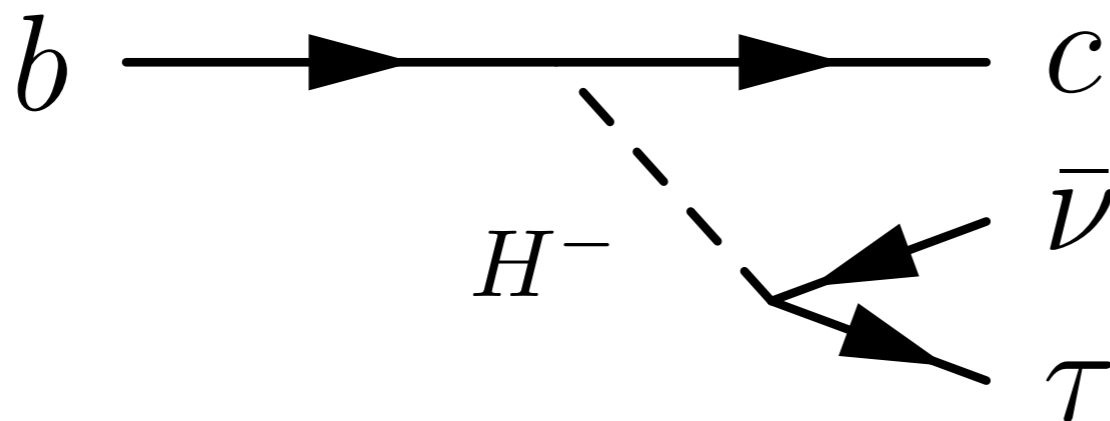
Data available since 2007 (Belle, BABAR, LHCb)

Theoretical motivation

W.S. Hou and B. Grzadkowski (1992)



SM: gauge coupling
lepton universality

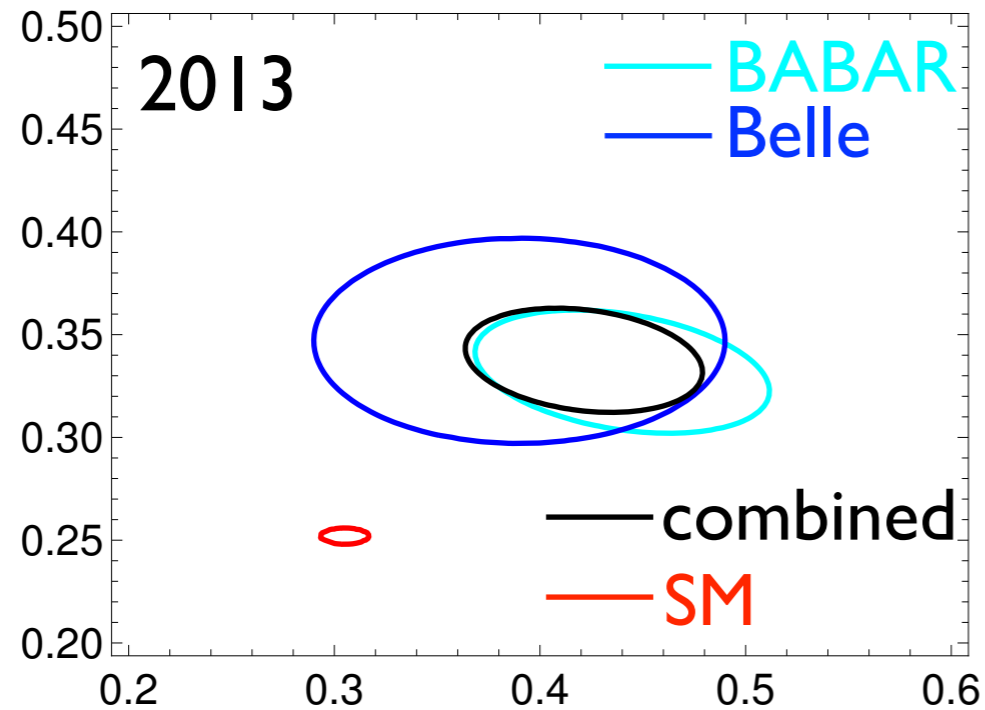


Type-II 2HDM (SUSY)
Yukawa coupling
 $\propto m_b m_\tau \tan^2 \beta$

Experiments

$$R(D^{(*)}) \equiv \frac{\mathcal{B}(\bar{B} \rightarrow D^{(*)} \tau \bar{\nu}_\tau)}{\mathcal{B}(\bar{B} \rightarrow D^{(*)} \ell \bar{\nu}_\ell)}$$

$R(D^*)$



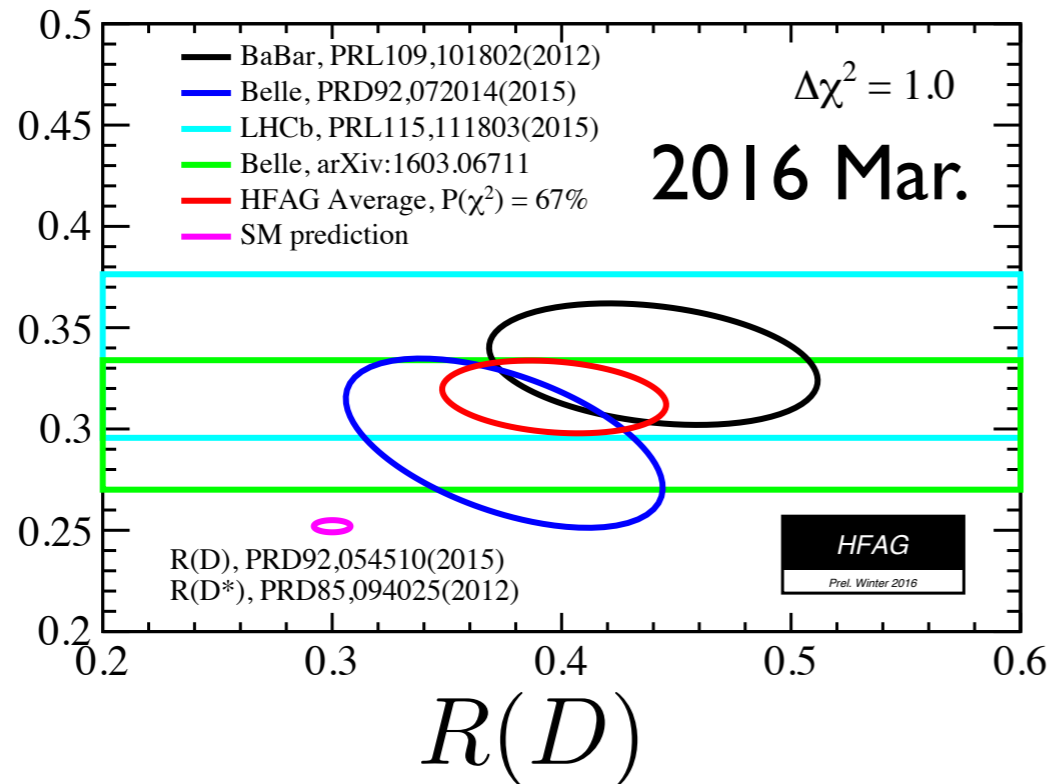
$$R(D) = 0.421 \pm 0.058$$

$$R(D^*) = 0.337 \pm 0.025$$

$\sim 3.5\sigma$

Y. Sakaki, MT, A. Tayduganov, R. Watanabe

$R(D^*)$



$$R(D) = 0.397 \pm 0.040 \pm 0.028$$

$$R(D^*) = 0.316 \pm 0.016 \pm 0.010$$

$\sim 4.0\sigma$

HFAG

With Belle ICHEP2016

$$R(D^*) = 0.310 \pm 0.017$$

What about $b \rightarrow u\tau\bar{\nu}$?

Semitauonic $\bar{B} \rightarrow (\pi, \rho, \dots)\tau\bar{\nu}$

Pure tauonic $B^- \rightarrow \tau\bar{\nu}$

Experimental data

$$\mathcal{B}(\bar{B}^0 \rightarrow \pi^+\tau^-\bar{\nu}) = (1.52 \pm 0.72 \pm 0.13) \times 10^{-4}$$

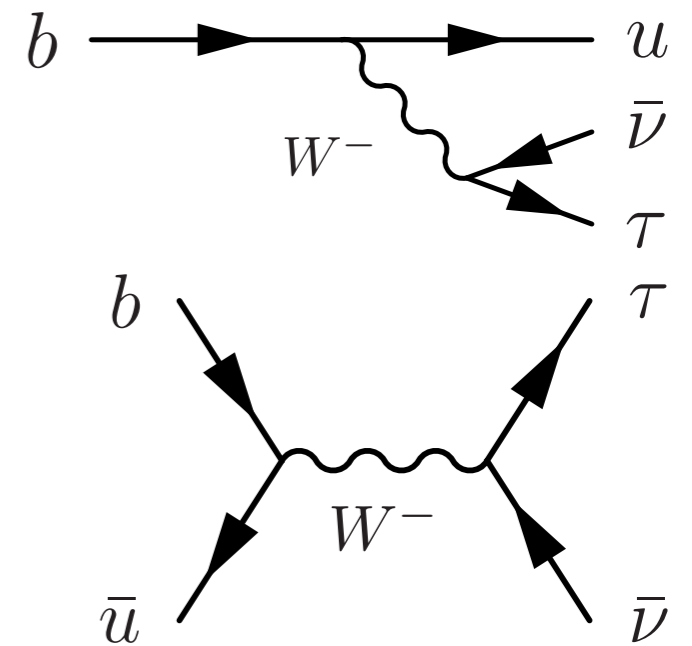
Belle 2015

$$\sim 0.7 \times 10^{-4} \text{ in SM}$$

a good target of Belle II

$$\mathcal{B}(B^- \rightarrow \tau^-\bar{\nu}) = (1.14 \pm 0.22) \times 10^{-4}$$

HFAG 2014



Plan of talk


1. Introduction
2. $B \rightarrow \pi\tau\bar{\nu}$
3. $B \rightarrow \tau\bar{\nu}$
4. Status and prospect
5. Summary

$$B \rightarrow \pi \tau \bar{\nu}$$

Model-independent analysis of $\bar{B} \rightarrow \pi\tau\bar{\nu}$

Effective Lagrangian for $b \rightarrow u\tau\bar{\nu}$

$$-\mathcal{L}_{\text{eff}} = 2\sqrt{2}G_F V_{ub} \left[(1 + C_{V_1})\mathcal{O}_{V_1} + C_{V_2}\mathcal{O}_{V_2} + C_{S_1}\mathcal{O}_{S_1} + C_{S_2}\mathcal{O}_{S_2} + C_T\mathcal{O}_T \right]$$


SM

$$\mathcal{O}_{V_1} = (\bar{u}\gamma^\mu P_L b)(\bar{\tau}\gamma_\mu P_L \nu_\tau),$$

SM-like, RPV, LQ, W'

$$\mathcal{O}_{V_2} = (\bar{u}\gamma^\mu P_R b)(\bar{\tau}\gamma_\mu P_L \nu_\tau),$$

RH current

$$\mathcal{O}_{S_1} = (\bar{u}P_R b)(\bar{\tau}P_L \nu_\tau),$$

charged Higgs II, RPV, LQ

$$\mathcal{O}_{S_2} = (\bar{u}P_L b)(\bar{\tau}P_L \nu_\tau),$$

charged Higgs III, LQ

$$\mathcal{O}_T = (\bar{u}\sigma^{\mu\nu} P_L b)(\bar{\tau}\sigma_{\mu\nu} P_L \nu_\tau),$$

LQ

$|V_{ub}|$ and form factors  **uncertainty**

$$R_\pi = \frac{\mathcal{B}(\bar{B}^0 \rightarrow \pi^+ \tau^- \bar{\nu})}{\mathcal{B}(\bar{B}^0 \rightarrow \pi^+ \ell^- \bar{\nu})}$$

smaller uncertainty

Form factors

Vector: $f_+(q^2)$, $f_0(q^2)$

$$\langle \pi(p_\pi) | \bar{u} \gamma^\mu b | \bar{B}(p_B) \rangle = f_+(q^2) \left[(p_B + p_\pi)^\mu - \frac{m_B^2 - m_\pi^2}{q^2} q^\mu \right] + f_0(q^2) \frac{m_B^2 - m_\pi^2}{q^2} q^\mu$$

$\bar{B} \rightarrow \pi \ell \bar{\nu}$ **exp. data + lattice** Bailey et al. PRD92, 014024 (2015)

Scalar: $f_S(q^2)$

$$\langle \pi(p_\pi) | \bar{u} b | \bar{B}(p_B) \rangle = (m_B + m_\pi) f_S(q^2)$$

eq. of motion $f_S(q^2) = \frac{m_B - m_\pi}{m_b - m_u} f_0(q^2)$

$$m_b \simeq 4.2 \text{ GeV}$$

Tensor: $f_T(q^2)$

$$\langle \pi(p_\pi) | \bar{u} i \sigma^{\mu\nu} b | B(p_B) \rangle = \frac{2}{m_B + m_\pi} f_T(q^2) [p_B^\mu p_\pi^\nu - p_B^\nu p_\pi^\mu]$$

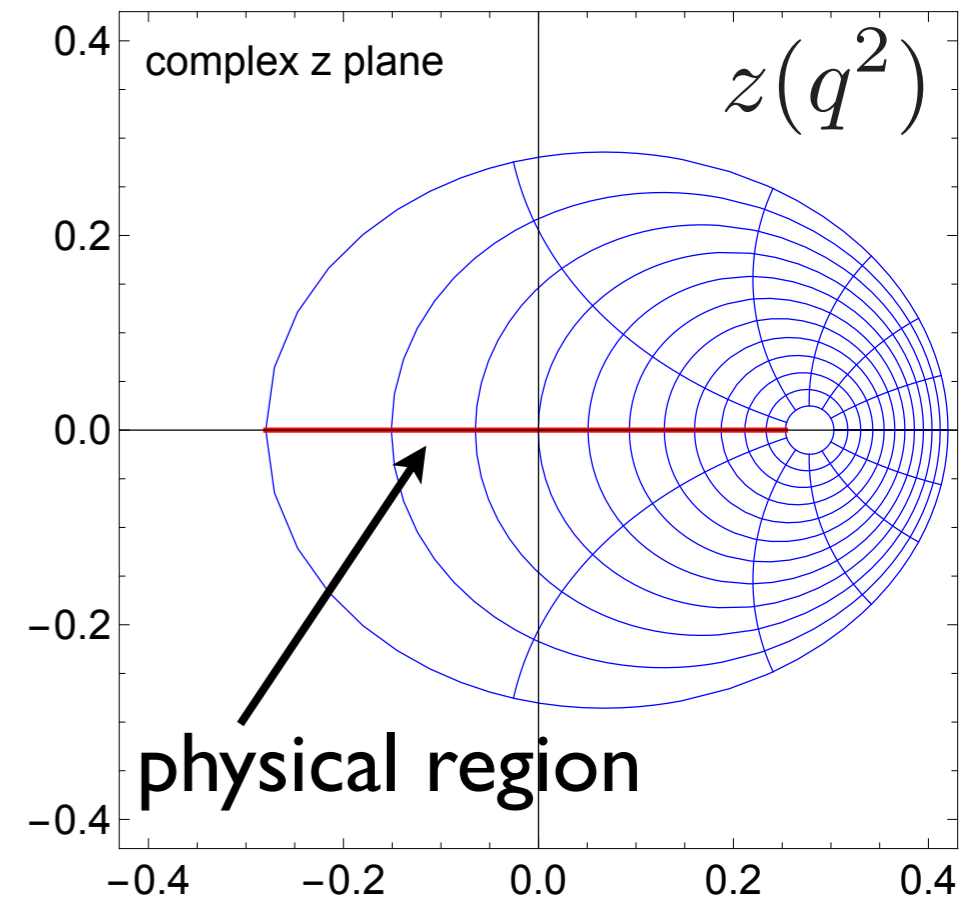
lattice Bailey et al. PRL115, 152002 (2015)

BCL expansion

Bourenly, Caprini, Lellouch, PRD79, 013008 (2009)

Series expansion in terms of

$$z := \frac{\sqrt{t_+ - q^2} - \sqrt{t_+ - t_0}}{\sqrt{t_+ - q^2} + \sqrt{t_+ - t_0}}$$



$$f_j(q^2) = \frac{1}{1 - q^2/m_{B^*}^2} \sum_{n=0}^{N_z-1} b_n^j \left[z^n - (-1)^{n-N_z} \frac{n}{N_z} z^{N_z} \right] \quad \begin{array}{l} j = +, T \\ N_z = 4 \end{array}$$

B* pole $m_{B^*} = 5.325 \text{ GeV}$

$$f_0(q^2) = \sum_{n=0}^{N_z-1} b_n^0 z^n$$

Ratio of branching fraction

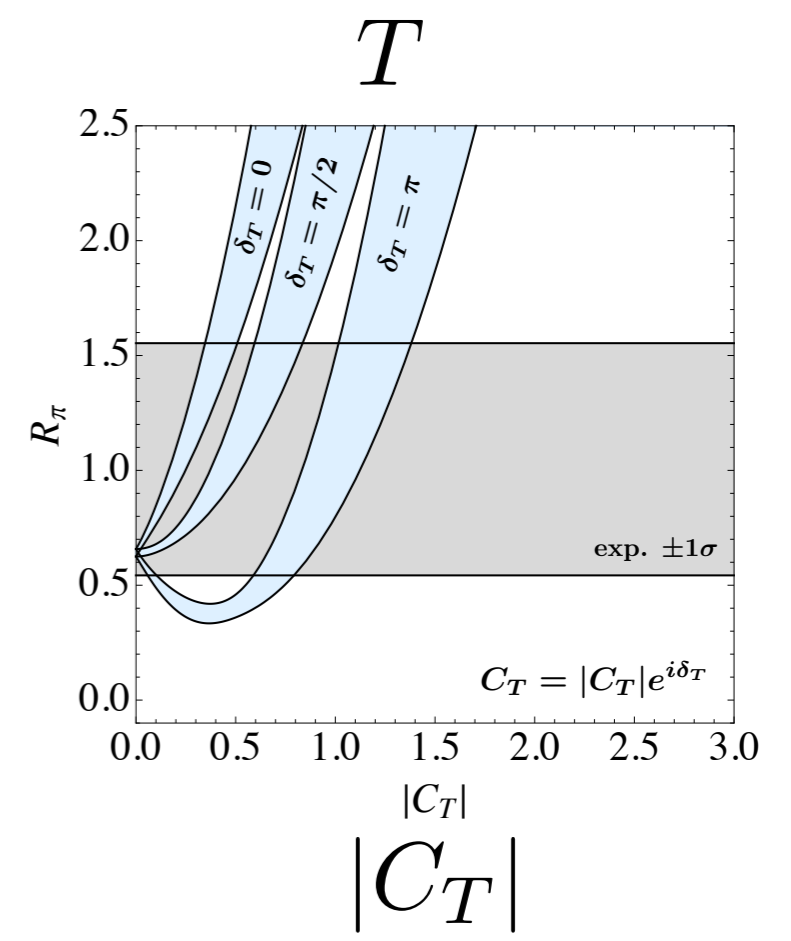
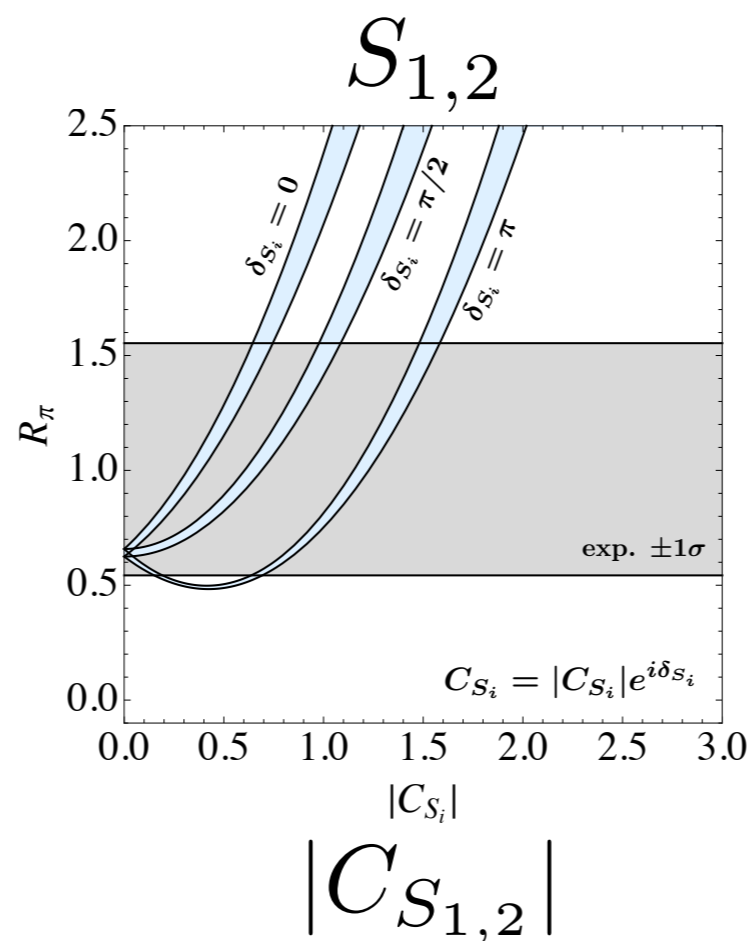
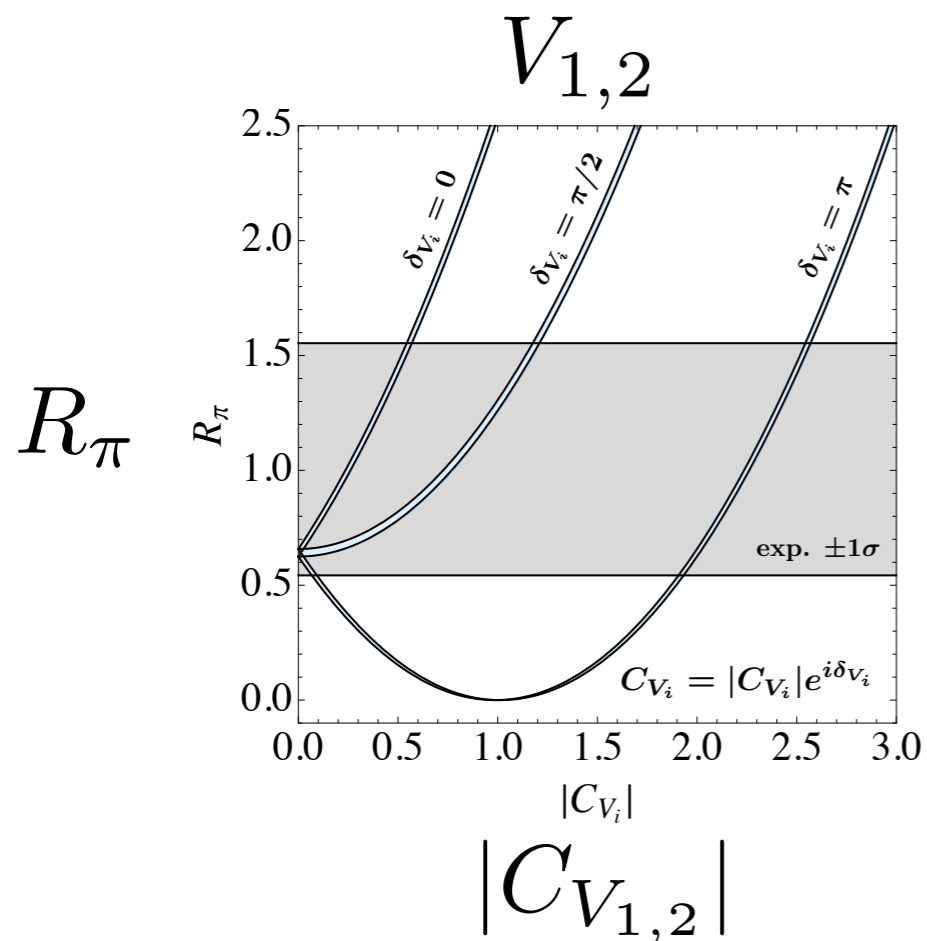
$$R_\pi = \frac{\mathcal{B}(\bar{B}^0 \rightarrow \pi^+ \tau^- \bar{\nu})}{\mathcal{B}(\bar{B}^0 \rightarrow \pi^+ \ell^- \bar{\nu})}$$

$$R_\pi^{\text{exp}} = 1.05 \pm 0.51$$

$$\mathcal{B}(B \rightarrow \pi \ell \bar{\nu}) = (1.45 \pm 0.02 \pm 0.04) \times 10^{-4}$$

HFAG

$$R_\pi^{\text{SM}} = 0.641 \pm 0.016$$



$$B \rightarrow \tau \bar{\nu}$$

Pure- to semi- leptonic ratio

$B^- \rightarrow \tau^- \bar{\nu}$ described by $\mathcal{L}_{\text{eff}}(b \rightarrow u\tau\bar{\nu})$

$$\mathcal{B}(B \rightarrow \tau\bar{\nu}_\tau) = \frac{\tau_{B^-} G_F^2 |V_{ub}|^2 f_B^2}{8\pi} m_B m_\tau^2 \left(1 - \frac{m_\tau^2}{m_B^2}\right)^2 |1 + r_{\text{NP}}|^2$$

$$r_{\text{NP}} = C_{V_1} - C_{V_2} + \frac{m_B^2}{m_b m_\tau} (C_{S_1} - C_{S_2}) \text{ No tensor contrib.}$$

Uncertainties: $|V_{ub}|$, f_B

Taking a ratio to eliminate $|V_{ub}|$

$$R_{\text{ps}} = \frac{\Gamma(B^- \rightarrow \tau^- \bar{\nu}_\tau)}{\Gamma(\bar{B}^0 \rightarrow \pi^+ \ell^- \bar{\nu}_\ell)} = \frac{\tau_{B^0} \mathcal{B}(B^- \rightarrow \tau^- \bar{\nu}_\tau)}{\tau_{B^-} \mathcal{B}(\bar{B}^0 \rightarrow \pi^+ \ell^- \bar{\nu}_\ell)}$$

Fajfer et al. PRL 109, 161801 (2012)

+ lattice $f_B = 192.0 \pm 4.3 \text{ MeV}$ FLAG 1607.00299

$$R_{\text{ps}}^{\text{SM}} = 0.574 \pm 0.046$$

$$R_{\text{ps}}^{\text{exp}} = 0.73 \pm 0.14$$

$$\mathcal{B}(B^- \rightarrow \tau^- \bar{\nu}) = (1.14 \pm 0.22) \times 10^{-4}$$

Another ratio

$$R_{\text{pl}} = \frac{\mathcal{B}(B \rightarrow \tau \bar{\nu}_\tau)}{\mathcal{B}(B \rightarrow \mu \bar{\nu}_\mu)} = \frac{m_\tau^2 (1 - m_\tau^2/m_B^2)^2}{m_\mu^2 (1 - m_\mu^2/m_B^2)^2} |1 + r_{\text{NP}}|^2 \simeq 222 |1 + r_{\text{NP}}|^2$$

practically no uncertainty in the SM prediction

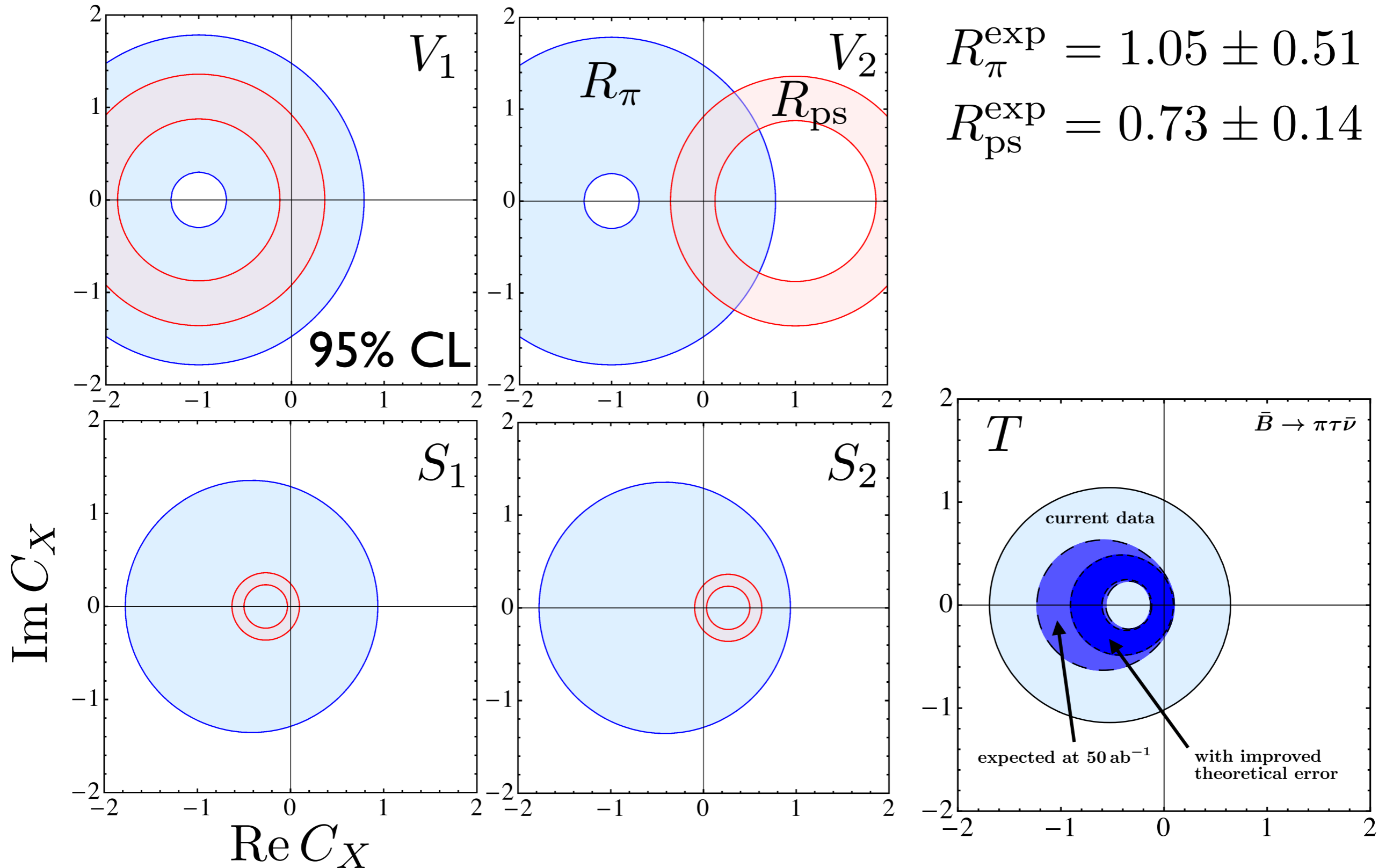
$$\mathcal{B}(B \rightarrow \mu \bar{\nu}_\mu)^{\text{exp.}} < 1 \times 10^{-6} \text{ at } 90\% \text{ CL} \quad \text{BaBar, Belle}$$

$$\mathcal{B}(B \rightarrow \mu \bar{\nu}_\mu)^{\text{SM}} = (0.41 \pm 0.05) \times 10^{-6}$$

likely to be observed at Belle II

Status and prospect

Present status

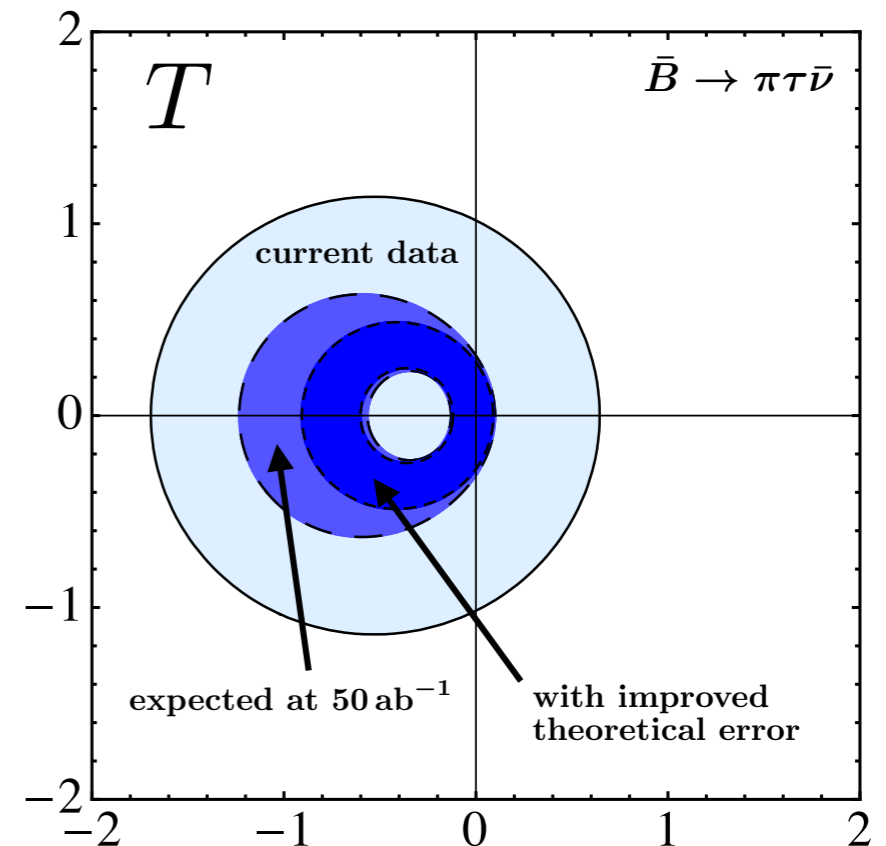
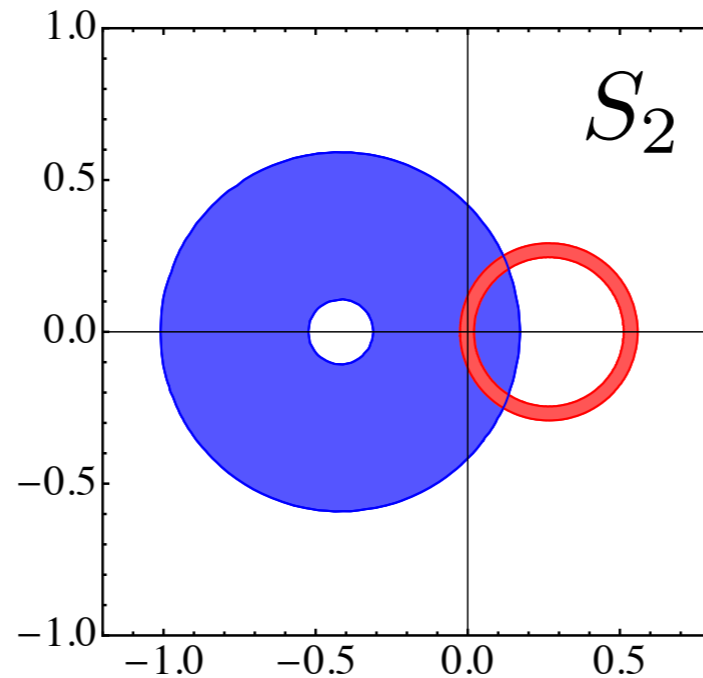
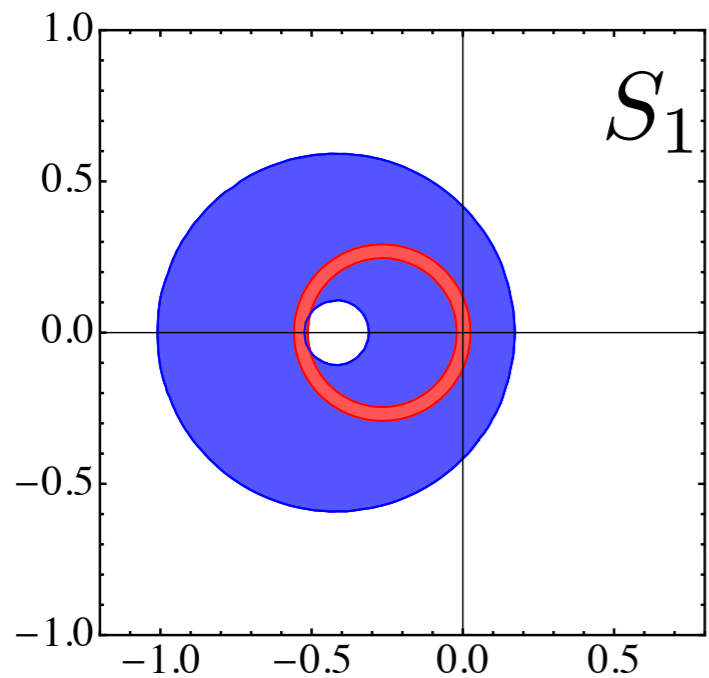
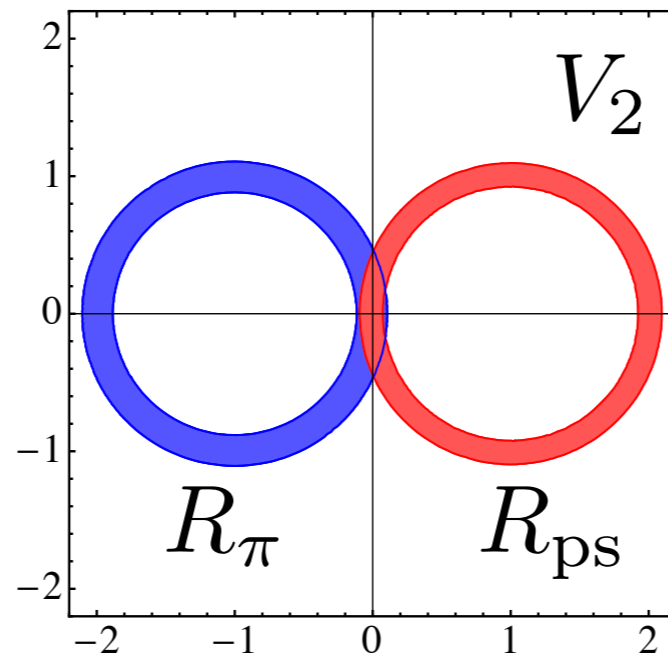
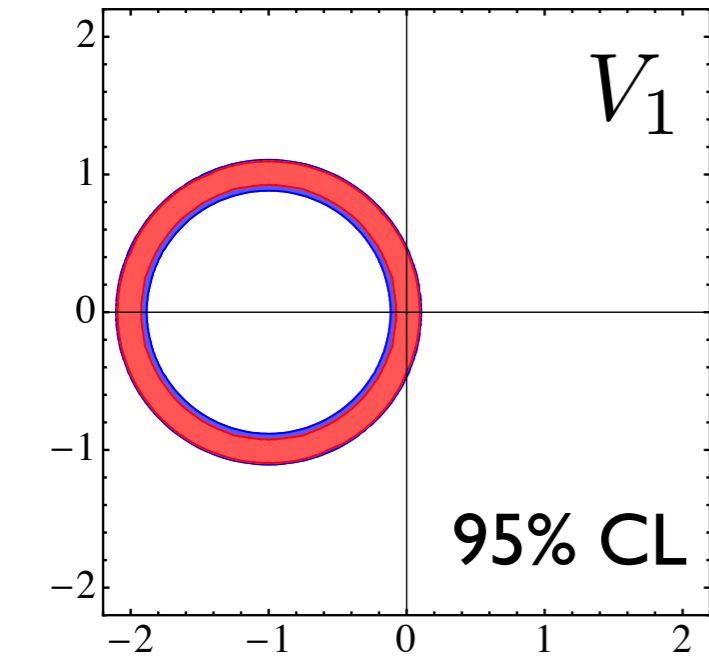


Future prospect

Belle II $\sim 50/\text{ab}$ cf. Belle $\sim 1/\text{ab}$

Scaling the present errors as $1/\sqrt{\mathcal{L}}$

the central values = SM



Real Cx

NP scenario	$R_{\pi}^{\text{Belle II}} = 0.641 \pm 0.071$ and $R_{\text{ps}}^{\text{Belle II}} = 0.574 \pm 0.020$	$R_{\text{pl}}^{\text{Belle II}} = 222 \pm 47$
C_{V_1}	$[-0.08, 0.09]; [-2.09, -1.92]$	$[-0.23, 0.19]; [-2.19, -1.77]$
C_{V_2}	$[-0.09, 0.08]$	$[-0.19, 0.23]; [1.77, 2.19]$
C_{S_1}	$[-0.03, 0.03]; [-0.55, -0.52]$	$[-0.06, 0.05]; [-0.58, -0.47]$
C_{S_2}	$[-0.03, 0.03]$	$[-0.05, 0.06]; [0.47, 0.58]$
C_T	$[-0.13, 0.10]; [-1.23, -0.56]$	-



SM like



large negative interference

vectors, tensor $\sim O(0.1)$

scalars ~ 0.03

Summary

■ Model-independent analysis of $b \rightarrow u\tau\bar{\nu}$

$$B \rightarrow \pi\tau\bar{\nu}, \tau\bar{\nu}$$

■ Observables of less uncertainties

$$R_{\text{ps}} = \frac{\tau_{B^0} \mathcal{B}(B^- \rightarrow \tau^- \bar{\nu}_\tau)}{\tau_{B^-} \mathcal{B}(\bar{B}^0 \rightarrow \pi^+ \ell^- \bar{\nu}_\ell)} \quad \text{most sensitive}$$

$$R_\pi = \frac{\mathcal{B}(\bar{B}^0 \rightarrow \pi^+ \tau^- \bar{\nu})}{\mathcal{B}(\bar{B}^0 \rightarrow \pi^+ \ell^- \bar{\nu})} \quad \begin{array}{l} \text{sensitive to tensor} \\ \text{complementary to } R_{\text{ps}} \end{array}$$

$$R_{\text{pl}} = \frac{\mathcal{B}(B \rightarrow \tau\bar{\nu}_\tau)}{\mathcal{B}(B \rightarrow \mu\bar{\nu}_\mu)} \quad \begin{array}{l} \text{no theoretical uncertainty} \\ \text{need more statistics ?} \end{array}$$

■ Other observables

q2 distribution, $B \rightarrow \rho\tau\bar{\nu}$