# ゲージヒッグス統一模型に <br> おける安定なヒッグスボソン <br> 田中実 <br> 大阪大学 <br> 於 富山大学，2010／12／10 

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Y．Hosotani，MT，N．Uekusa（arXiv：1010．6135v2，and in progress）

## Introduction

## Two big issues in particle physics

## Electro-Weak Symmetry Breaking

Higgs mechanism:
Not seen yet.


Naturalness and the hierarchy problem:

$$
\Lambda \sim M_{\mathrm{Pl}} \sim 10^{18} \mathrm{GeV} \quad \text { vs } \quad M_{\text {weak }} \sim 10^{3} \mathrm{GeV}
$$

## Radiative corrections to Higgs mass

$$
\begin{aligned}
& \quad m_{0}^{2}+\cdots \Lambda^{2} \\
& \sim O\left(\left(10^{18} \mathrm{GeV}\right)^{2}\right)-O\left(\left(10^{18} \mathrm{GeV}\right)^{2}\right) \sim O\left(\left(10^{3} \mathrm{GeV}\right)^{2}\right)
\end{aligned}
$$

A possible solution: Supersymmetry


An alternative solution:

## Gauge-Higgs unification

## Dark Matter

Rotation curves of galaxies: DM in galactic halo.


Other evidences:
cluster gas, gravitational lensing, colliding clusters

Cosmic microwave background:

$$
\text { WMAP } \quad \Omega_{\mathrm{CDM}} h^{2}=0.1131 \pm 0.0034
$$



How particle physics explains the dark matter?

Supersymmetry
Gauge-Higgs unification

Neutralino

## Stable Higgs as Dark Matter (Dark Higgs scenario)

Questions on the dark Higgs scenario
How is it realized?
a gauge-Higgs unification model
Does it explain the relic abundance?
a constraint on Higgs mass
How do we confirm it?
collider phenomenology

## Gauge-Higgs Unification

## Gauge field in higher dimensions

Five-dimensional space-time: $x^{M}=\left(x^{\mu}, y\right)$

$$
x^{\mu}=\left(x^{0}, x^{1}, x^{2}, x^{3}\right)
$$

Gauge field: $\left.A_{M}=\left(A_{\mu}\right), A_{y}\right)$

## 4D vector 4D scalar $\ni$ Higgs

5D gauge inv.
Massless $A_{M}$

A potential solution to the naturalness problem!

## Dynamical symmetry breaking

4D Higgs field: Wilson line (AB) phase
$M^{4} \times S^{1} \quad$ (multiply connected)


$$
\hat{\theta}_{H}(x) \sim g \int_{0}^{2 \pi R} A_{y} d y
$$

$\left\langle\hat{\theta}_{H}\right\rangle \neq 0$ at quantum level.
Nontrivial $V_{\text {eff }}\left(\hat{\theta}_{H}\right)$ at I-loop.
Hosotani mechanism, 1983
Gauge symmetry is dynamically broken.

## Flat space and warped space

$$
M^{4} \times\left(S^{1} / Z_{2}\right)
$$

## Randall-Sundrum



$$
d s^{2}=d x_{\mu} d x^{\mu} \nvdash d y^{2}
$$

Y. Hosotani

$$
\begin{equation*}
d s^{2}=e^{-2 k|y|} d x_{\mu} d x^{\mu}+d y^{2} \tag{5}
\end{equation*}
$$

Two fixed points: $y=0, y=\pi R \rightarrow$ Two branes. RS warped space

Realistic spectrum

## An SO(5)xU(I) model on RS warped space

Agashe, Contino,Pomarol, 2005. Hosotani, Sakamura, 2006. Medina, Shah,Wagner, 2007. Hosotani, Oda, Ohnuma, Sakamura, 2008.

Y. Hosotani, ICFP2009, 25 September 2009-5

## Origin of the Higgs doublet

$$
\underbrace{S O(4) \simeq S U(2)_{L} \times S U(2)}_{S O(5) \rightarrow\left(\begin{array}{lllll}
-1 & & & & \\
& -1 & & & \\
& & -1 & & \\
& & & -1 & \\
& & & & +1
\end{array}\right)}
$$


Y. Hosotani, ICFP2009, 25 September 2009-6

$$
A_{y}\left(x^{\mu}, y\right) \sim \hat{\theta}_{H}\left(x^{\mu}\right) h_{0}(y) \hat{T}^{4}+\cdots
$$

$$
h_{0}(y)=h_{0}(-y)
$$

## SO（5）xU（1）Model on RS

YH，Oda，Ohnuma，Sakamura 2008 （YH，Noda，Uekusa 2009）


At low energies $\quad \gamma, \underset{H}{\boldsymbol{H}}, \boldsymbol{Z} \quad\binom{t_{L}}{b_{L}} \quad \begin{array}{llll}t_{R}^{\prime} & b_{R}^{\prime} & \cdots\end{array}$

Y．Hosotani，物理学会， 12 September 2009－2

## Discrete symmetries

EWSB by Hosotani mechanism
4D Higgs field: Wilson line (AB) phase, $\hat{\theta}_{H}(x)$
Periodicity: $\mathcal{L}\left(\hat{\theta}_{H}\right)=\mathcal{L}\left(\hat{\theta}_{H}+2 \pi\right)$
Bulk fermions: vectors (and/or tensors) of SO(5), no spinors.
$\rightarrow$ Reduction of period: $\mathcal{L}\left(\hat{\theta}_{H}\right)=\mathcal{L}\left(\hat{\theta}_{H}+\pi\right)$
Mirror reflection symmetry

$$
y \rightarrow-y, A_{y} \rightarrow-A_{y}, \Psi \rightarrow \gamma_{5} \Psi
$$

Parity: $\mathcal{L}\left(\hat{\theta}_{H}\right)=\mathcal{L}\left(-\hat{\theta}_{H}\right)$

## Effective Lagrangian at the Weak Scale

$\mathcal{L}_{\text {eff }}=-V_{\text {eff }}\left(\hat{\theta}_{H}\right)-\sum_{f} m_{f}\left(\hat{\theta}_{H}\right) \bar{f} f$

$$
+m_{W}^{2}\left(\hat{\theta}_{H}\right) W^{+\mu} W_{\mu}^{-}+\frac{1}{2} m_{Z}^{2}\left(\hat{\theta}_{H}\right) Z^{\mu} Z \mu
$$

Symmetry implications:

$$
\begin{aligned}
& V_{\mathrm{eff}}\left(\hat{\theta}_{H}+\pi\right)=V_{\mathrm{eff}}\left(\hat{\theta}_{H}\right)=V_{\mathrm{eff}}\left(-\hat{\theta}_{H}\right) \\
& m_{W, Z}^{2}\left(\hat{\theta}_{H}+\pi\right)=m_{W, Z}^{2}\left(\hat{\theta}_{H}\right)=m_{W, Z}^{2}\left(-\hat{\theta}_{H}\right), \\
& m_{f}\left(\hat{\theta}_{H}+\pi\right)=-m_{f}\left(\hat{\theta}_{H}\right)=m_{f}\left(-\hat{\theta}_{H}\right)
\end{aligned}
$$

## EWSB

Vacuum: Minimize $V_{\text {eff }}\left(\theta_{H}\right)$ 0.si gauge

$$
\begin{aligned}
& \begin{array}{l}
\theta_{H}=\pi / 2 .
\end{array} \\
& \hat{\theta}_{H}(x)=\frac{\pi}{2}+\frac{H(x)}{f_{H}} . \\
& f_{H}=246 \mathrm{GeV}\left(\Leftarrow m_{W}=g f_{H} / 2\right)
\end{aligned}
$$

A new dynamical parity, H-parity,

$$
\begin{gathered}
\frac{\pi}{2}+\frac{H}{f_{H}} \xrightarrow[\hat{\theta} \rightarrow-\hat{\theta}]{ }-\frac{\pi}{2}-\frac{H}{f_{H}} \xrightarrow[\hat{\theta} \rightarrow \hat{\theta}+\pi]{ } \frac{\pi}{2}-\frac{H}{f_{H}} \\
H(x) \longrightarrow-H(x) .
\end{gathered}
$$

## Effective Interactions

Integrating out KK modes,

$$
\begin{aligned}
& m_{W}\left(\hat{\theta}_{H}\right) \sim \cos \theta_{W} m_{Z}\left(\hat{\theta}_{H}\right) \sim \frac{1}{2} g f_{H} \sin \hat{\theta}_{H}, \\
& m_{a}^{F}\left(\hat{\theta}_{H}\right) \sim \lambda_{a} \sin \hat{\theta}_{H} \\
& \mathcal{L}_{\text {int }}=-\frac{m_{W}^{2}}{f_{H}^{2}} H^{2} W^{+\mu} W_{\mu}^{-}-\frac{m_{Z}^{2}}{2 f_{H}^{2}} H^{2} Z^{\mu} Z_{\mu} \\
&+\sum_{f} \frac{m_{f}}{2 f_{H}^{2}} H^{2} \bar{f} f+\cdots .
\end{aligned}
$$

No odd powers of $H$.

## Higgs is STABLE!

A good candidate for WIMP DM.

## Dark Higgs

## Relic Abundance



Kolb and Turner, 1989

Annihilation processes:


## Relic Abundance



$$
\begin{array}{c|ccc}
10^{-27} \mathrm{~cm}^{3} / \mathrm{s} & b \bar{b} & W^{(*)} W^{(*)} & Z^{(*)} Z^{(*)} \\
\hline\left.\sigma v\right|_{v \rightarrow 0} & 7.3 & 11 & 1.5
\end{array}
$$

## Direct Detection $H N \rightarrow H N$



$$
\begin{aligned}
\mathcal{L}_{H N} & \simeq \frac{2+7 f_{N}}{9} \frac{m_{N}}{2 f_{H}^{2}} H^{2} \bar{N} N \\
f_{N} & =\sum_{q=u, d, s}\langle N| m_{q} \bar{q} q|N\rangle / m_{N} \simeq 0.1 \sim 0.3
\end{aligned}
$$

## Spin-Independent Cross Section

## CDMS II

 arXiv:09|2.3592Local DM density $\rho_{0}=0.3 \mathrm{GeV} / \mathrm{cm}^{3}$ assumed in exps.

For $m_{H}=70 \mathrm{GeV}$
Exp. bound:

$$
\sigma_{\mathrm{SI}} \lesssim 3.8 \times 10^{-44} \mathrm{~cm}^{2}
$$

$$
90 \% \text { CL }
$$

Dark Higgs
Prediction: $\sigma_{\text {SI }} \simeq(1.2-2.7) \times 10^{-43} \mathrm{~cm}^{2}$

## Collider Signals

## Higgs pair production at Linear Collider

Signal: $e^{+} e^{-} \rightarrow Z H H$

## H's are missing.

 total cross section for $m_{H}=70 \mathrm{GeV}$

$\sqrt{s}(\mathrm{GeV})$
$Z_{L}$ violates the unitarity unless $s / m_{\mathrm{KK}}^{2} \ll 1$. $m_{\mathrm{KK}} \sim 1.5 \mathrm{TeV}$
$\sqrt{s}=500 \mathrm{GeV}$
in the following.

## LC background $e^{+} e^{-} \rightarrow Z \nu \bar{\nu}$



Diagrams by MadGraph



BG cross section with $M_{\text {miss }} \geq 120 \mathrm{GeV}$ $\sigma_{\mathrm{BG}} \simeq 311 \mathrm{fb}$

Need polarizations!
beams and Z




## LC with polarizations

Ideal case: $e_{L}^{+} e_{R}^{-} \rightarrow Z_{L} H H, Z_{L} \nu \bar{\nu}$

$$
\sigma_{\text {signal }} \simeq 0.12 \mathrm{fb} \text { vs } \sigma_{\mathrm{BG}} \simeq 0.42 \mathrm{fb}
$$

$$
|\cos \theta|<0.6 \text { is applied. }
$$

Significance: $\mathcal{S} \equiv \frac{N_{\text {signal }}}{\sqrt{N_{\text {signal }}+N_{\mathrm{BG}}}}$

$$
\mathcal{S}=1.4 \sqrt{L / 100 \mathrm{fb}^{-1}}
$$

A few (or more) $\mathrm{ab}^{-1}$ is required!

## Higgs pair production at LHC

Signal: Weak boson fusion


Background: Wij, Zjj, jij
Similar as invisible Higgs search

## Signal cross section at LHC



$$
\frac{d \sigma_{H H}}{d m_{H H}^{2}}=\left.\frac{\bar{\beta}_{f}}{32 \pi^{2} v^{2}} \sigma_{h}\right|_{m_{h}^{2}=m_{H H}^{2}}
$$

in the SM

$$
\begin{gathered}
\sigma_{H H} \sim 1.5 \mathrm{fb} \\
\\
\sigma_{B G} \simeq 167 \mathrm{fb}
\end{gathered}
$$

$$
\mathcal{S} \sim 1.2 \sqrt{L / 100 \mathrm{fb}^{-1}}
$$

Éboli, Zeppenfeld

$$
\begin{aligned}
& p_{T}^{j}>40 \mathrm{GeV}, \quad\left|\eta_{j}\right|<5.0, \\
& \left|\eta_{j 1}-\eta_{j 2}\right|>4.4, \quad \eta_{j 1} \cdot \eta_{j 2}<0, \\
& p_{T}>100 \mathrm{GeV} . \\
& M_{j j}>1200 \mathrm{GeV}, \quad \phi_{j j}<1 .
\end{aligned}
$$

## More on H parity

$$
\begin{aligned}
& A_{M}=\sum_{I=1}^{10} A_{M}^{I} T^{I}=\sum_{a_{L}=1}^{3} A_{M}^{a_{L}} T^{a_{L}}+\sum_{a_{R}=1}^{3} A_{M}^{a_{R}} T^{a_{R}}+\sum_{\hat{a}=1}^{4} A_{M}^{\hat{a}} T^{\hat{a}} \\
& {\left[T^{a_{L}}, T^{b_{L}}\right]=i \epsilon^{a b c} T^{c_{L}}, \quad\left[T^{a_{R}}, T^{b_{R}}\right]=i \epsilon^{a b c} T^{c_{R}}, \quad\left[T^{a_{L}}, T^{b_{R}}\right]=0} \\
& {\left[T^{\hat{a}}, T^{\hat{b}}\right]=\frac{i}{2} \epsilon^{a b c}\left(T^{c_{L}}+T^{c_{R}}\right),} \\
& {\left[T^{\hat{a}}, T^{b_{L}}\right]=-\frac{i}{2} \delta^{a b} T^{\hat{4}}+\frac{i}{2} \epsilon^{a b c} T^{\hat{c}}, \quad\left[T^{\hat{a}}, T^{b_{R}}\right]=+\frac{i}{2} \delta^{a b} T^{\hat{4}}+\frac{i}{2} \epsilon^{a b c} T^{\hat{c}}} \\
& {\left[T^{a_{L}}, T^{\hat{4}}\right]=-\frac{i}{2} T^{\hat{a}}, \quad\left[T^{a_{R}}, T^{\hat{4}}\right]=+\frac{i}{2} T^{\hat{a}}, \quad\left[T^{\hat{a}}, T^{\hat{4}}\right]=\frac{i}{2}\left(T^{a_{L}}-T^{a_{R}}\right)} \\
& (a, b, c=1 \sim 3) .
\end{aligned}
$$

Invariant under $\Omega_{H}=\operatorname{diag}(1,1,1,-1,1) \in O(5)$

$$
\left\{T^{a_{L}}, T^{a_{R}}, T^{\hat{a}}, T^{\hat{4}}\right\} \longrightarrow\left\{T^{a_{R}}, T^{a_{L}}, T^{\hat{a}},-T^{\hat{4}}\right\}
$$

## Typical mode expansion

## 5D mode func.

$\tilde{A}_{\mu}(x, z)=\sum_{n=\lambda}^{\infty}{ }^{d} W_{\mu}^{(n)}\left\{N_{W}\left(\lambda_{n}\right) \frac{T^{-L}+T^{-R}}{2}+\cos \theta_{H} N_{W}\left(\lambda_{n}\right) \frac{T^{-L}-T^{-R}}{2}\right.$
field
$\left.-\frac{\sin \theta_{H}}{\sqrt{2}} D_{W}\left(\lambda_{n}\right) T^{\llcorner }\right\}+$h.c.

$$
\begin{aligned}
& \quad+\sum_{n=1}^{\infty} W_{\mu}^{\prime(n)}\left\{-\cos \theta_{H} N_{W^{\prime}}\left(\lambda_{n}\right) \frac{T^{-L}+T^{-R}}{2}+N_{W^{\prime}}\left(\lambda_{n}\right) \frac{T^{-L}-T^{-R}}{2}\right\}+\text { h.c. } \\
& \quad+\sum_{n=0}^{\infty} s A_{\mu}^{\gamma(n)} h_{\gamma}\left(\lambda_{n}\right)\left(T^{3_{L}}+T^{3 R}\right)+\sum_{n=1}^{\infty} A_{\mu}^{\hat{4}(n)} h_{A}\left(\lambda_{n}\right) T^{4}+\cdots \\
& \tilde{A}_{z}(x, z)=\sum_{n=1}^{\infty} \sum_{a=1}^{3} S^{S^{a(n)} h_{S}^{L R}\left(\lambda_{n}\right) \frac{T^{a_{L}}+T^{a_{R}}}{\sqrt{2}}+\sum_{n=0}^{\infty} H^{s(n)} h_{H}\left(\lambda_{n}\right) T^{4}+\cdots} \\
& \theta_{H}=\pi / 2 \\
& \quad W_{\mu}^{(n)}, A_{\mu}^{\gamma(n)}, S^{a(n)} \quad P_{H} \text { even } \\
& W_{\mu}^{\prime(n)}, A_{\mu}^{\hat{4}(n)}, H^{(n)} \quad P_{H} \text { odd }
\end{aligned}
$$

## H-even KK particle production

## Model parameters

EW parameters: $k, g_{A}, g_{B}, z_{L}=e^{k L}$
EW inputs: $m_{Z}, \alpha, \sin ^{2} \theta_{W}$

$$
z_{L} \longrightarrow m_{H}
$$

| $z_{L}=e^{k L}$ | $\sin ^{2} \theta_{W}$ | $k(\mathrm{GeV})$ | $m_{\mathrm{KK}}(\mathrm{GeV})$ | $c_{\text {top }}$ | $m_{H}(\mathrm{GeV})$ | $m_{W}^{\text {tree }}(\mathrm{GeV})$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $10^{15}$ | 0.2312 | $4.666 \times 10^{17}$ | 1,466 | 0.432 | 135 | 79.82 |
| $10^{10}$ | 0.23 | $3.799 \times 10^{12}$ | 1,194 | 0.396 | 108 | 79.82 |
| $10^{5}$ | 0.2285 | $2.662 \times 10^{7}$ | 836 | 0.268 | 72 | 79.70 |

## Spectrum

Table 14: KK gluon masses $m_{G^{(n)}}$ in unit of GeV .
KK gluon

| $z_{L} \backslash n$ | 1 | 2 | 3 | 4 | 5 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $10^{15}$ | 1143.4 | 2597.79 | 4060.29 | 5524.61 | 6989.61 |
| $10^{10}$ | 939.287 | 2123.35 | 3313.67 | 4505.36 | 5697.54 |
| $10^{5}$ | 676.998 | 1508.23 | 2342.77 | 3177.87 | 4013.1 |

Table 15: KK $W$ boson masses $m_{W^{(n)}}$ in unit of GeV .

| $z_{L} \backslash n$ | 1 | 2 | 3 | 4 | 5 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $10^{15}$ | 1132.69 | 1799.15 | 2586.69 | 3284.74 | 4049.02 |
| $10^{10}$ | 926.031 | 1468.74 | 2109.46 | 2677.61 | 3299.47 |
| $10^{5}$ | 657.626 | 1038.84 | 1487.22 | 1885.54 | 2320.8 |

KK Z
Table 16: KK $Z$ boson masses $m_{Z^{(n)}}$ in unit of GeV .

| $z_{L} \backslash n$ | 1 | 2 | 3 | 4 | 5 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $10^{15}$ | 1129.49 | 1802.53 | 2583.37 | 3288.13 | 4045.64 |
| $10^{10}$ | 922.087 | 1472.93 | 2105.3 | 2681.86 | 3295.21 |
| $10^{5}$ | 651.946 | 1045.02 | 1480.99 | 1892.00 | 2314.27 |

Focus on the first KK Z.

## Couplings

Table 25: The couplings of the first KK $Z$ boson with charged leptons, $g_{f I}^{\left(Z_{1}\right)} \sqrt{L} / g_{A}$.

| $z_{L}$ | $e L$ | $\mu L$ | $\tau L$ | $e R$ | $\mu R$ | $\tau R$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $10^{15}$ | 0.0310237 | 0.0310238 | 0.0310529 | 2.52033 | 2.42011 | 2.35629 |
| $10^{10}$ | 0.0382222 | 0.0382244 | 0.0382616 | 2.13663 | 2.03326 | 1.96297 |
| $10^{5}$ | 0.0549348 | 0.0549354 | 0.0550174 | 1.62351 | 1.53169 | 1.45818 |

Table 26: The couplings of the first KK $Z$ boson with left-handed quarks, $g_{f L}^{\left(Z_{1}\right)} \sqrt{L} / g_{A}$.

| $z_{L}$ | $u$ | $c$ | $t$ | $d$ | $s$ | $b$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $10^{15}$ | -0.0399184 | -0.0399209 | -0.206095 | 0.0488131 | 0.048804 | -0.558474 |
| $10^{10}$ | -0.0491807 | -0.0491842 | -0.256412 | 0.0601393 | 0.0601274 | -0.672188 |
| $10^{5}$ | -0.0706849 | -0.0706938 | -0.386896 | 0.0864351 | 0.0864104 | -0.927167 |

Table 27: The couplings of the first KK $Z$ boson with right-handed quarks, $g_{f R}^{\left(Z_{1}\right)} \sqrt{L} / g_{A}$.

| $z_{L}$ | $u$ | $c$ | $t$ | $d$ | $s$ | $b$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $10^{15}$ | -1.65847 | -1.58714 | -1.4692 | 0.829233 | 0.793569 | 0.723936 |
| $10^{10}$ | -1.40259 | -1.32685 | -1.1796 | 0.701297 | 0.663427 | 0.579202 |
| $10^{5}$ | -1.06424 | -0.991935 | -0.754189 | 0.532119 | 0.495967 | 0.376702 |

Table 24: The couplings of the first KK $W$ boson with leptons, $g_{f L}^{\left(W_{1}\right)} \sqrt{L} / g_{A}$ and the couplings of the first KK $Z$ boson with neutrinos, $g_{f L}^{\left(Z_{1}\right)} \sqrt{L} / g_{A}$.

| $z_{L}$ | $e \nu_{e}$ | $\mu \nu_{\mu}$ | $\tau \nu_{\tau}$ | $\nu_{e}$ | $\nu_{\mu}$ | $\nu_{\tau}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $10^{15}$ | -0.138009 | -0.138008 | -0.137939 | -0.0577078 | -0.0577075 | -0.0576242 |
| $10^{10}$ | -0.170013 | -0.170012 | -0.169923 | -0.0710978 | -0.0710974 | -0.0709898 |
| $10^{5}$ | -0.244187 | -0.244186 | -0.24403 | -0.102185 | -0.102184 | -0.101988 |

## Decay width and BR

Table 28: First KK $Z$ boson decay: the branching fraction and the total width.

| $z_{L}$ | $10^{15}$ | $10^{10}$ | $10^{5}$ |
| :---: | :---: | :---: | :---: |
| $e(\%)$ | 14.1396 | 14.18 | 13.253 |
| $\mu(\%)$ | 13.0376 | 12.8416 | 11.798 |
| $\tau(\%)$ | 12.3591 | 11.9693 | 10.6941 |
| $\nu_{e}+\nu_{\mu}+\nu_{\tau}(\%)$ | 0.0222139 | 0.0470403 | 0.157124 |
| $(u+c) / 2(\%)$ | 17.6028 | 17.3854 | 16.0203 |
| $(d+s+b) / 3(\%)$ | 3.68474 | 4.40884 | 7.27081 |
| $c(\%)$ | 16.8299 | 16.4225 | 14.9003 |
| $b(\%)$ | 5.58161 | 7.3338 | 15.0894 |
| $t(\%)$ | 14.1818 | 12.9648 | 10.2446 |
| $u+d+s+c(\%)$ | 40.6781 | 40.6636 | 38.7638 |
| total width $(\mathrm{GeV})$ | 371.761 | 217.536 | 95.0912 |

## KK Z at Tevatron: $p \bar{p} \rightarrow Z^{(1)} X \rightarrow e^{-} e^{+} X$

 Background: $p \bar{p} \rightarrow e^{-} e^{+} X$




## Significance at Tevatron $\quad L=2.5 \mathrm{fb}^{-1}$



## KK Z at LHC: $p p \rightarrow Z^{(1)} X \rightarrow e^{-} e^{+} X$

Background: $p p \rightarrow e^{-} e^{+} X$



## Significance at LHC $\quad \sqrt{s}=7 \mathrm{TeV}$

$$
\mathcal{S}=5.1 \sqrt{\frac{L}{10 \mathrm{pb}^{-1}}}
$$

## Summary

Stable Higgs in gauge-Higgs unifiction is a viable candidate of dark matter.

Dark Higgs scenario
$m_{H} \sim 70 \mathrm{GeV}$ is predicted.
Direct detection is likely.
Exp. limits depend on the local DM density, $\rho_{0}$.

$$
\rho_{0} \simeq 0.04 \sim 0.6 \mathrm{GeV} / \mathrm{cm}^{3}
$$

We need a few $\mathrm{ab}^{-1}$ or more. both for LHC and LC.

The first KK Z production at Tevatron suggests a larger warp factor. $\quad z_{L} \sim 10^{15}$

Dark Higgs seems difficult at the present model.

$$
m_{H}=135 \mathrm{GeV} \text { for } z_{L}=10^{15}
$$

The first KK Z production may be discovered at LHC with $10 \mathrm{pb}^{-1}$ even for $z_{L}=10^{15}$.

Thank you.

## Backup Slides

## Spin-Independent Cross Section


Local DM density $\rho_{0}=0.3 \mathrm{GeV} / \mathrm{cm}^{3}$ assumed in exps.

For $m_{H}=70 \mathrm{GeV}$
Prediction: $\quad \sigma_{\text {SI }} \simeq(1.2-2.7) \times 10^{-43} \mathrm{~cm}^{2}$
Exp. bound: $\sigma_{\mathrm{SI}} \lesssim 3.8 \times 10^{-44} \mathrm{~cm}^{2}$

## Uncertainties in the direct detection

Local density of CDM (not measured)
$\rho_{0}=0.3 \mathrm{GeV} / \mathrm{cm}^{3}$ assumed in the experiments.
$\rho_{0}=0.2 \sim 0.6 \mathrm{GeV} / \mathrm{cm}^{3}$ reasonable for smooth halo.
$\rho_{0} \sim 0.04 \mathrm{GeV} / \mathrm{cm}^{3}$ (Kamionkowski and Koushiappas) possible for non-smooth halo.

Effective Higgs coupling $H H \bar{f} f$ may be altered in more general models.

## Astrophysical Signals

$H H \rightarrow \gamma \gamma, \gamma Z$ in the Galactic halo.
Two (nearly) monochromatic gamma lines.

$$
\begin{aligned}
& E_{\gamma}=m_{H}(\simeq 70 \mathrm{GeV}), m_{H}-m_{Z}^{2} /\left(4 m_{H}\right)(\simeq 40 \mathrm{GeV}) \\
& \left.\sigma_{\gamma \gamma(\gamma Z)} v\right|_{v \rightarrow 0} \simeq 4.3(5.4) \times 10^{-29} \mathrm{~cm}^{3} / \mathrm{s}
\end{aligned}
$$



## Stable Higgs as Dark Matter (Dark Higgs scenario)



## Yomiuri newspaper, the front page on Jan. 5, 2010.

Table 3: The couplings of $Z$ boson with left-handed quarks, $g_{f L}^{(Z)} \sqrt{L} / g_{A}$.

| $z_{L}$ | $u$ | $c$ | $t$ | $d$ | $s$ | $b$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $10^{15}$ | 0.348452 | 0.348132 | 0.32172 | -0.425887 | -0.425887 | -0.42639 |
| $10^{10}$ | 0.349467 | 0.349467 | 0.307934 | -0.427336 | -0.427336 | -0.428457 |
| $10^{5}$ | 0.352916 | 0.352914 | 0.253315 | -0.431553 | -0.431553 | -0.435986 |

Table 4: The couplings of $Z$ boson with right-handed quarks, $g_{f R}^{(Z)} \sqrt{L} / g_{A}$.

| $z_{L}$ | $u$ | $c$ | $t$ | $d$ | $s$ | $b$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $10^{15}$ | -0.15643 | -0.156388 | -0.183737 | 0.0782151 | 0.0781938 | 0.0781582 |
| $10^{10}$ | -0.15765 | -0.157568 | -0.200882 | 0.0788248 | 0.0787836 | 0.0786987 |
| $10^{5}$ | -0.161498 | -0.161279 | -0.268141 | 0.0807492 | 0.0806393 | 0.0802678 |

Table 6: The couplings of $Z$ bosons with charged leptons, $g_{f I}^{(Z)} \sqrt{L} / g_{A}$.

| $z_{L}$ | $e L$ | $\mu L$ | $\tau L$ | $e R$ | $\mu R$ | $\tau R$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $10^{15}$ | -0.270677 | -0.270677 | -0.270674 | 0.234664 | 0.234605 | 0.234569 |
| $10^{10}$ | -0.271598 | -0.271598 | -0.271594 | 0.236509 | 0.236398 | 0.236324 |
| $10^{5}$ | -0.274278 | -0.274278 | -0.274267 | 0.242328 | 0.242053 | 0.24183 |

Table 5: The couplings of $W$ boson with leptons, $g_{f L}^{(W)} \sqrt{L} / g_{A}$ and the couplings of $Z$ boson with neutrinos, $g_{f L}^{(Z)} \sqrt{L} / g_{A}$.

| $z_{L}$ | $e \nu_{e}$ | $\mu \nu_{\mu}$ | $\tau \nu_{\tau}$ | $\nu_{e}$ | $\nu_{\mu}$ | $\nu_{\tau}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $10^{15}$ | 1.00533 | 1.00533 | 1.00533 | 0.503492 | 0.503492 | 0.503492 |
| $10^{10}$ | 1.00792 | 1.00792 | 1.00792 | 0.505205 | 0.505205 | 0.505206 |
| $10^{5}$ | 1.01535 | 1.01535 | 1.01534 | 0.51019 | 0.51019 | 0.510191 |

