ゲージヒッグス統一模型に おける安定なヒッグスボソン





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Introduction

Two big issues in particle physics

Electro-Weak Symmetry Breaking

Higgs mechanism:

Not seen yet.



Naturalness and the hierarchy problem:

 $\Lambda \sim M_{\rm Pl} \sim 10^{18} \,{\rm GeV}$ vs $M_{\rm weak} \sim 10^3 \,{\rm GeV}$

Radiative corrections to Higgs mass



 $\sim O((10^{18} \,\mathrm{GeV})^2) - O((10^{18} \,\mathrm{GeV})^2) \sim O((10^3 \,\mathrm{GeV})^2)$



An alternative solution:

Gauge-Higgs unification

Dark Matter

Rotation curves of galaxies: DM in galactic halo.



Other evidences: cluster gas, gravitational lensing, colliding clusters

Cosmic microwave background: $\label{eq:cosm} {\rm WMAP} \qquad \Omega_{\rm CDM} h^2 = 0.1131 \pm 0.0034$



How particle physics explains the dark matter? Supersymmetry Neutralino Gauge-Higgs unification ? Stable Higgs as Dark Matter (Dark Higgs scenario)

Questions on the dark Higgs scenario

How is it realized?

a gauge-Higgs unification model

Does it explain the relic abundance? a constraint on Higgs mass

How do we confirm it?

collider phenomenology

Gauge-Higgs Unification

Gauge field in higher dimensions Five-dimensional space-time: $x^{M} = (x^{\mu}, y)$ $x^{\mu} = (x^0, x^1, x^2, x^3)$ Gauge field: $A_M = (A_\mu, A_y)$ 4D vector 4D scalar \ni Higgs **5D** gauge inv. Massless A_M

A potential solution to the naturalness problem!

Dynamical symmetry breaking 4D Higgs field: Wilson line (AB) phase $M^4 \times S^1$ (multiply connected) $y = 2\pi R$ y = 0 $\hat{\theta}_H(x) \sim g \int_0^{2\pi R} A_y \, dy$

 $\langle \hat{\theta}_H \rangle \neq 0$ at quantum level. Nontrivial $V_{\text{eff}}(\hat{\theta}_H)$ at I-loop.

Hosotani mechanism, 1983

Gauge symmetry is dynamically broken.

Flat space and warped space



An SO(5)xU(1) model on RS warped space

Agashe, Contino, Pomarol, 2005. Hosotani, Sakamura, 2006. Medina, Shah, Wagner, 2007. Hosotani, Oda, Ohnuma, Sakamura, 2008.





 $h_0(y) = h_0(-y)$



Discrete symmetries EWSB by Hosotani mechanism 4D Higgs field: Wilson line (AB) phase, $\theta_H(x)$ Periodicity: $\mathcal{L}(\hat{\theta}_H) = \mathcal{L}(\hat{\theta}_H + 2\pi)$ Bulk fermions: vectors (and/or tensors) of SO(5), no spinors. Reduction of period: $\mathcal{L}(\hat{\theta}_H) = \mathcal{L}(\hat{\theta}_H + \pi)$ Mirror reflection symmetry $y \to -y, A_y \to -A_y, \Psi \to \gamma_5 \Psi$ Parity: $\mathcal{L}(\hat{\theta}_H) = \mathcal{L}(-\hat{\theta}_H)$

Effective Lagrangian at the Weak Scale $\mathcal{L}_{eff} = -V_{eff}(\hat{\theta}_H) - \sum_f m_f(\hat{\theta}_H) \bar{f}f$ $+ m_W^2(\hat{\theta}_H) W^{+\mu} W^{-}_{\mu} + \frac{1}{2} m_Z^2(\hat{\theta}_H) Z^{\mu} Z \mu$

Symmetry implications:

$$V_{\text{eff}}(\hat{\theta}_H + \pi) = V_{\text{eff}}(\hat{\theta}_H) = V_{\text{eff}}(-\hat{\theta}_H),$$

$$m_{W,Z}^2(\hat{\theta}_H + \pi) = m_{W,Z}^2(\hat{\theta}_H) = m_{W,Z}^2(-\hat{\theta}_H),$$

$$m_f(\hat{\theta}_H + \pi) = -m_f(\hat{\theta}_H) = m_f(-\hat{\theta}_H).$$





Effective Interactions

Integrating out KK modes,

$$m_W(\hat{\theta}_H) \sim \cos \theta_W m_Z(\hat{\theta}_H) \sim \frac{1}{2} g f_H \sin \hat{\theta}_H ,$$

$$m_a^F(\hat{\theta}_H) \sim \lambda_a \sin \hat{\theta}_H ,$$

$$\mathcal{L}_{\text{int}} = -\frac{m_W^2}{f_H^2} H^2 W^{+\mu} W_{\mu}^- - \frac{m_Z^2}{2f_H^2} H^2 Z^{\mu} Z_{\mu} + \sum_f \frac{m_f}{2f_H^2} H^2 \bar{f} f + \cdots .$$

No odd powers of H. Higgs is STABLE!

A good candidate for WIMP DM.

Dark Higgs





Direct Detection $HN \rightarrow HN$





Collider Signals





LC with polarizations Ideal case: $e_L^+ e_R^- \to Z_L H H$, $Z_L \nu \bar{\nu}$ $\sigma_{\rm signal} \simeq 0.12 \, {\rm fb}$ vs $\sigma_{\rm BG} \simeq 0.42 \, {\rm fb}$ $|\cos \theta| < 0.6$ is applied. Significance: $S \equiv \frac{N_{\text{signal}}}{\sqrt{N_{\text{signal}} + N_{\text{BG}}}}$

 $S = 1.4 \sqrt{L/100} \, \text{fb}^{-1}$

A few (or more) ab^{-1} is required!

Higgs pair production at LHC Signal: Weak boson fusion



Background: Wjj, Zjj, jjj

Similar as invisible Higgs search

Signal cross section at LHC



$$\begin{aligned} & \text{More on H parity} \qquad SO(5)/SO(4) \\ & \text{SO(5) algebra} \qquad \stackrel{SU(2)_L}{\downarrow} \qquad \stackrel{SU(2)_L}{\downarrow} \qquad \stackrel{SU(2)_R}{\downarrow} \qquad \stackrel{I}{\downarrow} \\ & A_M = \sum_{I=1}^{10} A_M^I T^I = \sum_{a_L=1}^{3} A_M^{a_L} T^{a_L} + \sum_{a_R=1}^{3} A_M^{a_R} T^{a_R} + \sum_{\hat{a}=1}^{4} A_M^{\hat{a}} T^{\hat{a}} \\ & [T^{a_L}, T^{b_L}] = i\epsilon^{abc} T^{c_L} , \quad [T^{a_R}, T^{b_R}] = i\epsilon^{abc} T^{c_R} , \quad [T^{a_L}, T^{b_R}] = 0 , \\ & [T^{\hat{a}}, T^{\hat{b}}] = \frac{i}{2} \epsilon^{abc} (T^{c_L} + T^{c_R}) , \\ & [T^{\hat{a}}, T^{\hat{b}}] = -\frac{i}{2} \delta^{ab} T^{\hat{4}} + \frac{i}{2} \epsilon^{abc} T^{\hat{c}} , \quad [T^{\hat{a}}, T^{b_R}] = +\frac{i}{2} \delta^{ab} T^{\hat{4}} + \frac{i}{2} \epsilon^{abc} T^{\hat{c}} , \\ & [T^{a_L}, T^{\hat{4}}] = -\frac{i}{2} T^{\hat{a}} , \quad [T^{a_R}, T^{\hat{4}}] = +\frac{i}{2} T^{\hat{a}} , \quad [T^{\hat{a}}, T^{\hat{4}}] = \frac{i}{2} (T^{a_L} - T^{a_R}) \\ & (a, b, c = 1 \sim 3) . \end{aligned}$$

$$\text{Invariant under} \ \Omega_H = \text{diag} (1, 1, 1, -1, 1) \in O(5) \end{aligned}$$

$$\{T^{a_L}, T^{a_R}, T^{\hat{a}}, T^{\hat{4}}\} \longrightarrow \{T^{a_R}, T^{a_L}, T^{\hat{a}}, -T^{\hat{4}}\}$$

$$\begin{aligned} & \text{Typical mode expansion} \\ & \tilde{A}_{\mu}(x,z) = \sum_{n=0}^{\infty} {}^{d} W_{\mu}^{(n)} \left\{ N_{W}(\lambda_{n}) \frac{T^{-L} + T^{-R}}{2} + \cos \theta_{H} N_{W}(\lambda_{n}) \frac{T^{-L} - T^{-R}}{2} \right. \\ & \left. + \cos \theta_{H} N_{W}(\lambda_{n}) \frac{T^{-L} - T^{-R}}{2} + \cos \theta_{H} N_{W}(\lambda_{n}) \frac{T^{-L} - T^{-R}}{2} \right\} + \text{h.c.} \\ & \left. + \sum_{n=1}^{\infty} {}^{s} W_{\mu}^{(n)} \left\{ -\cos \theta_{H} N_{W'}(\lambda_{n}) \frac{T^{-L} + T^{-R}}{2} + N_{W'}(\lambda_{n}) \frac{T^{-L} - T^{-R}}{2} \right\} + \text{h.c.} \\ & \left. + \sum_{n=0}^{\infty} {}^{s} A_{\mu}^{\gamma(n)} h_{\gamma}(\lambda_{n}) (T^{3_{L}} + T^{3_{R}}) + \sum_{n=1}^{\infty} {}^{s} A_{\mu}^{\dot{A}(n)} h_{A}(\lambda_{n}) T^{\dot{A}} + \cdots \right. \\ & \left. \tilde{A}_{z}(x, z) = \sum_{n=1}^{\infty} {}^{s} \sum_{a=1}^{3} S^{a(n)} h_{S}^{LR}(\lambda_{n}) \frac{T^{a_{L}} + T^{a_{R}}}{\sqrt{2}} + \sum_{n=0}^{\infty} {}^{s} H^{(n)} h_{H}^{\wedge}(\lambda_{n}) T^{\dot{A}} + \cdots \right. \\ & \left. \frac{\theta_{H}}{\mu} = \pi/2 \\ & W_{\mu}^{(n)}, A_{\mu}^{\gamma(n)}, S^{a(n)} P_{H} \text{ even} \\ & W_{\mu}^{\prime(n)}, A_{\mu}^{\dot{A}(n)}, H^{(n)} P_{H} \text{ odd} \end{aligned}$$

H-even KK particle production

Model parameters

EW parameters: $k, g_A, g_B, z_L = e^{kL}$ EW inputs: $m_Z, \alpha, \sin^2 \theta_W$

Spectrum KK gluor

Table 14: KK gluon masses $m_{G^{(n)}}$ in unit of GeV.

			•	9		
KK gluon	$z_L \setminus n$	1	2	3	4	5
0.0.0	10^{15}	1143.4	2597.79	4060.29	5524.61	6989.61
	10^{10}	939.287	2123.35	3313.67	4505.36	5697.54
	10^{5}	676.998	1508.23	2342.77	3177.87	4013.1
	Table 1	5: KK W	boson ma	asses $m_{W^{(r)}}$	$_{n)}$ in unit ϕ	of GeV.
KKW	$z_L \setminus n$	1	2	3	4	5
	10^{15}	1132.69	1799.15	2586.69	3284.74	4049.02
	10^{10}	926.031	1468.74	2109.46	2677.61	3299.47
	10^{5}	657.626	1038.84	1487.22	1885.54	2320.8
	Table	16: KK Z	boson ma	asses $m_{Z^{(n)}}$	in unit o	of GeV.
KK 7	$z_{I} \setminus n$	1	2	3	4	5

KK	Ζ
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$z_L \setminus n$	1	2	3	4	5
10^{15}	1129.49	1802.53	2583.37	3288.13	4045.64
10^{10}	922.087	1472.93	2105.3	2681.86	3295.21
10^{5}	651.946	1045.02	1480.99	1892.00	2314.27

Focus on the first KK Z.

Couplings

Table 25: The couplings of the first KK Z boson with charged leptons, $g_{fI}^{(Z_1)}\sqrt{L}/g_A$.

						J -
z_L	eL	μL	au L	eR	μR	au R
10^{15}	0.0310237	0.0310238	0.0310529	2.52033	2.42011	2.35629
10^{10}	0.0382222	0.0382224	0.0382616	2.13663	2.03326	1.96297
10^{5}	0.0549348	0.0549354	0.0550174	1.62351	1.53169	1.45818

Table 26: The couplings of the first KK Z boson with left-handed quarks, $g_{fL}^{(Z_1)}\sqrt{L}/g_A$.

z_L	u	С	t	d	S	b
10^{15}	-0.0399184	-0.0399209	-0.206095	0.0488131	0.048804	-0.558474
10^{10}	-0.0491807	-0.0491842	-0.256412	0.0601393	0.0601274	-0.672188
10^{5}	-0.0706849	-0.0706938	-0.386896	0.0864351	0.0864104	-0.927167

Table 27: The couplings of the first KK Z boson with right-handed quarks, $g_{fR}^{(Z_1)}\sqrt{L}/g_A$.

z_L	u	С	t	d	S	b
10^{15}	-1.65847	-1.58714	-1.4692	0.829233	0.793569	0.723936
10^{10}	-1.40259	-1.32685	-1.1796	0.701297	0.663427	0.579202
10^{5}	-1.06424	-0.991935	-0.754189	0.532119	0.495967	0.376702

Table 24: The couplings of the first KK W boson with leptons, $g_{fL}^{(W_1)}\sqrt{L}/g_A$ and the couplings of the first KK Z boson with neutrinos, $g_{fL}^{(Z_1)}\sqrt{L}/g_A$.

z_L	$e u_e$	μu_{μ}	$ au u_{ au}$	$ u_e $	$ u_{\mu}$	$ u_{ au}$
10^{15}	-0.138009	-0.138008	-0.137939	-0.0577078	-0.0577075	-0.0576242
10^{10}	-0.170013	-0.170012	-0.169923	-0.0710978	-0.0710974	-0.0709898
10^{5}	-0.244187	-0.244186	-0.24403	-0.102185	-0.102184	-0.101988

Decay width and BR

z_L	10^{15}	10^{10}	10^{5}	
e (%)	14.1396	14.18	13.253	
μ (%)	13.0376	12.8416	11.798	
au~(%)	12.3591	11.9693	10.6941	
$\nu_e + \nu_\mu + \nu_\tau \ (\%)$	0.0222139	0.0470403	0.157124	
$(u+c)/2 \ (\%)$	17.6028	17.3854	16.0203	
$(d+s+b)/3 \ (\%)$	3.68474	4.40884	7.27081	
c~(%)	16.8299	16.4225	14.9003	
$b \ (\%)$	5.58161	7.3338	15.0894	
t (%)	14.1818	12.9648	10.2446	
$u + d + s + c \ (\%)$	40.6781	40.6636	38.7638	
total width (GeV)	371.761	217.536	95.0912	

Table 28: First KK Z boson decay: the branching fraction and the total width.

KK Z at Tevatron: $p\bar{p} \rightarrow Z^{(1)}X \rightarrow e^-e^+X$ Background: $p\bar{p} \rightarrow e^-e^+X$









Significance at Tevatron
$$L = 2.5 \,\mathrm{fb}^{-1}$$

$$\frac{z_L}{|\mathcal{S}||} \frac{10^5 \quad 10^{10} \quad 10^{15}}{|121|} \frac{10^2 \quad 4}{|\mathcal{I}||}$$

$$\frac{10^5 \quad 121 \quad 22 \quad 4}{|\mathcal{I}||}$$
disfavored





Significance at LHC $\sqrt{s} = 7 \,\mathrm{TeV}$

$$\mathcal{S} = 5.1 \sqrt{\frac{L}{10 \,\mathrm{pb}^{-1}}}$$

Summary

 Stable Higgs in gauge-Higgs unifiction is a viable candidate of dark matter.
 Dark Higgs scenario

- * $m_H \sim 70 \,\mathrm{GeV}$ is predicted.
- * Direct detection is likely. Exp. limits depend on the local DM density, $ho_0 \cdot
 ho_0 \simeq 0.04 \sim 0.6 \,\mathrm{GeV/cm^3}$
- * We need a few ab^{-1} or more. both for LHC and LC.

- * The first KK Z production at Tevatron suggests a larger warp factor. $z_L \sim 10^{15}$
- * Dark Higgs seems difficult at the present model. $m_H = 135 \,\text{GeV}$ for $z_L = 10^{15}$
- ***** The first KK Z production may be discovered at LHC with 10 pb^{-1} even for $z_L = 10^{15}$.

Thank you.

Backup Slides

Spin-Independent Cross Section



Uncertainties in the direct detection

Local density of CDM (not measured) $\rho_0 = 0.3 \, {\rm GeV/cm^3}$ assumed in the experiments. $\rho_0 = 0.2 \sim 0.6 \, {\rm GeV/cm^3}$ reasonable for smooth halo. $ho_0 \sim 0.04 \, {
m GeV/cm^3}$ (Kamionkowski and Koushiappas) possible for non-smooth halo. Effective Higgs coupling HHffmay be altered in more general models.



Minoru TANAKA

Stable Higgs as Dark Matter (Dark Higgs scenario)



Yomiuri newspaper, the front page on Jan. 5, 2010.

Table 3: The couplings of Z boson with left-handed quarks, $g_{fL}^{(Z)}\sqrt{L}/g_A$.

z_L	u	С	t	d	s	b
10^{15}	0.348452	0.348132	0.32172	-0.425887	-0.425887	-0.42639
10^{10}	0.349467	0.349467	0.307934	-0.427336	-0.427336	-0.428457
10^{5}	0.352916	0.352914	0.253315	-0.431553	-0.431553	-0.435986

Table 4: The couplings of Z boson with right-handed quarks, $g_{fR}^{(Z)}\sqrt{L}/g_A$.

					J 10	•
z_L	u	С	t	d	S	b
10^{15}	-0.15643	-0.156388	-0.183737	0.0782151	0.0781938	0.0781582
10^{10}	-0.15765	-0.157568	-0.200882	0.0788248	0.0787836	0.0786987
10^{5}	-0.161498	-0.161279	-0.268141	0.0807492	0.0806393	0.0802678

Table 6: The couplings of Z bosons with charged leptons, $g_{fI}^{(Z)}\sqrt{L}/g_A$.

z_L	eL	μL	au L	eR	μR	au R
10^{15}	-0.270677	-0.270677	-0.270674	0.234664	0.234605	0.234569
10^{10}	-0.271598	-0.271598	-0.271594	0.236509	0.236398	0.236324
10^{5}	-0.274278	-0.274278	-0.274267	0.242328	0.242053	0.24183

Table 5: The couplings of W boson with leptons, $g_{fL}^{(W)}\sqrt{L}/g_A$ and the couplings of Z boson with neutrinos, $g_{fL}^{(Z)}\sqrt{L}/g_A$.

z_L	$e\nu_e$	μu_{μ}	$ au u_{ au}$	$ u_e $	$ u_{\mu}$	$ u_{ au}$
10^{15}	1.00533	1.00533	1.00533	0.503492	0.503492	0.503492
10^{10}	1.00792	1.00792	1.00792	0.505205	0.505205	0.505206
10^{5}	1.01535	1.01535	1.01534	0.51019	0.51019	0.510191